
Ultrashort X-ray Pulse Generation by Electron Beam Slicing in NSLS-II

Reporter: An He

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at Jlab Accelerator Division Seminar, 3/19/2015

outline

1, Introduction

2, Theory of electron beam slicing

3, Start to end design of this system

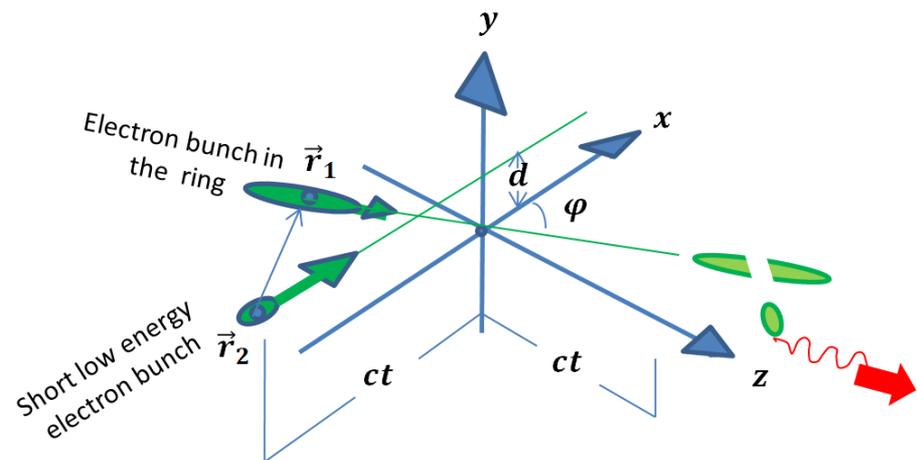
Simulation design of low energy compressor

Slice profile and radiation separation

Photon flux and repetition rate

Basic idea and characteristics

	Laser slicing	Crab cavity	X-ray FEL	Ebeam slicing
Source	Storage ring	Storage ring	FEL	Storage ring
Occupied ring space	large	large	large	?
Pulse length	~ 100 fs	~ ps	< 100 fs	?
Photon flux	~ 10^6 photons/sec/0.1%bw	~ 10^{14} photons/sec/0.1%bw	~ 10^{12} photons/sec/0.1%bw	?
Repetition rate	1 kHz	100 MHz	Low (120Hz for LCLS)	?
Pulse to pulse stability	good	good	poor	?



Basic Idea:

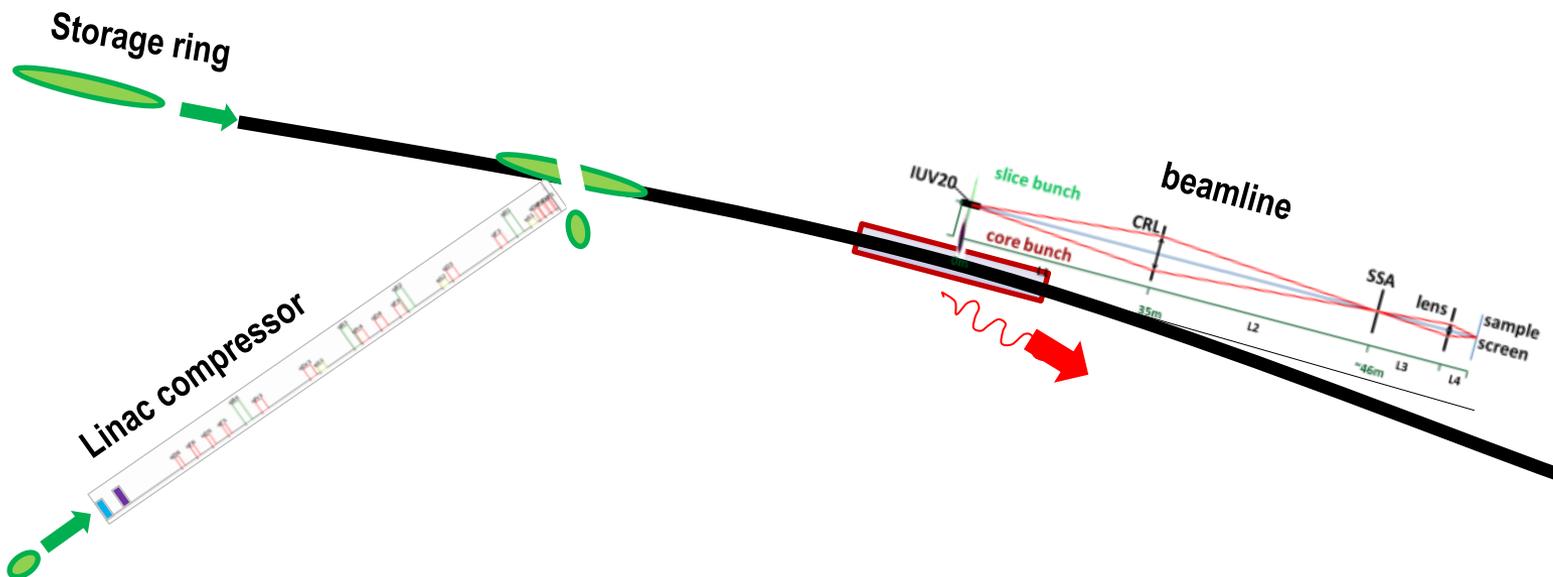
when a short electron bunch from a low energy linac passes above a storage ring bunch at a right angle, its Coulomb force will kick a short slice from the core of the storage ring bunch vertically.

The separated slice, when passing through an undulator, will radiate ultrashort x-ray pulse.

(Lihua Yu & Ferdinand Willeke)

Scheme of e-beam slicing

1. Analytical analysis of e-beam slicing (two bunches' interaction).
2. LINAC design, space charge dominated bunch compressor.
3. Choose interaction point at the storage ring.
4. Separate synchrotron radiations of the satellite from the core.
5. Photon flux and repetition rate of this e-beam slicing system.



Vertical angular kick function

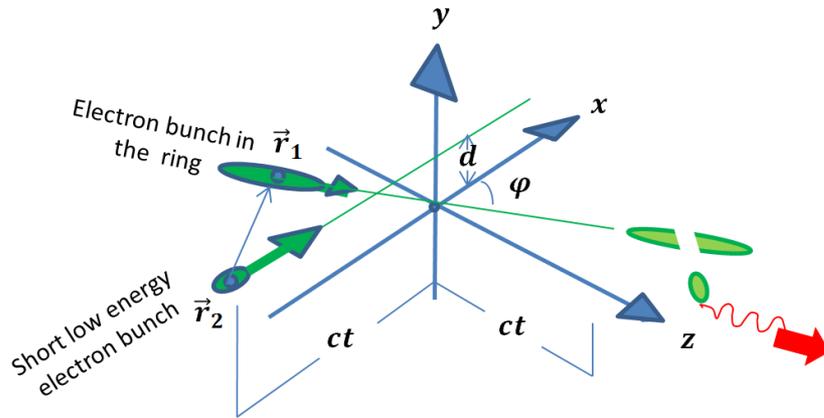
PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS 17, 120704 (2014)

Dependence on crossing angle of electron beam slicing in storage rings

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(Received 3 June 2014; published 17 December 2014)



$$\Delta\theta_y(x_r, y_r, z_r) = \frac{eq_2 Z_0 c}{2\pi E_1} \frac{\gamma_2(1 - \beta_1\beta_2 \cos \varphi)}{\sqrt{\gamma_2^2(1 - \cos \varphi)^2 + \sin^2 \varphi}} \frac{1}{\sqrt{2}\sigma_y} \times \underbrace{f_y(\rho, \bar{u}_1, \bar{y}_1)}_{\substack{\uparrow \\ \text{Profile function gives scaled vertical} \\ \text{kick angle and slicing length}}} \leftarrow \text{need small } \sigma_y, \text{ large } q_2$$

Nominal kick angle

$$f_y(\rho, \bar{u}_1, \bar{y}_1) = \int_0^\infty \text{Re}[W(\bar{u}_1 + iy)][e^{-(\rho y - \bar{y}_1)^2} - e^{-(\rho y + \bar{y}_1)^2}] dy$$

Profile function gives scaled vertical kick angle and slicing length

$$\rho \equiv \sqrt{\frac{\gamma_2^2}{\gamma_2^2(1 - \cos \varphi)^2 + \sin^2 \varphi} \cdot \frac{\sigma_x^2 \sin^2 \varphi + \sigma_z^2(1 - \cos \varphi)^2}{\sigma_y^2}} \leftarrow \text{need large } \rho \text{ small } \sigma_y$$

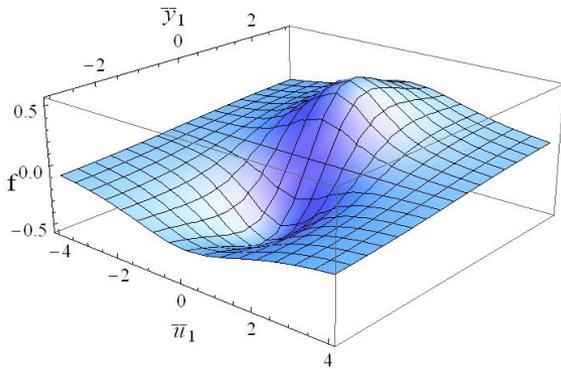
$$\bar{y}_1 \equiv \frac{d - y_r}{\sqrt{2}\sigma_y} \leftarrow \text{need small } d = \sqrt{2}\sigma_y$$

$$\bar{u}_1 \equiv \frac{z_r \sin \varphi + x_r(1 - \cos \varphi)}{\sqrt{2\sigma_x^2 \sin^2 \varphi + 2\sigma_z^2(1 - \cos \varphi)^2}} \leftarrow \text{need small } \sigma_x, \sigma_z \text{ to short pulse}$$

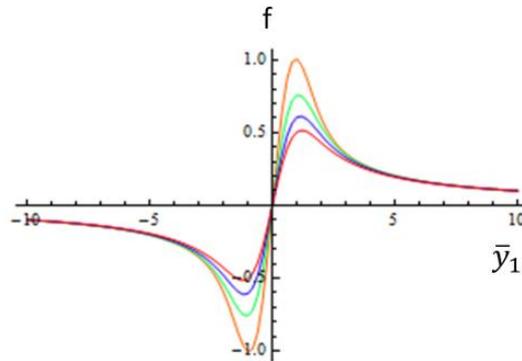
$$W(u) = e^{-u^2} \text{erfc}(-iu), \text{erfc}(x) = \frac{2}{\sqrt{\pi}} \int_x^{+\infty} e^{-x^2} dx$$

Kick profile and estimated slice width

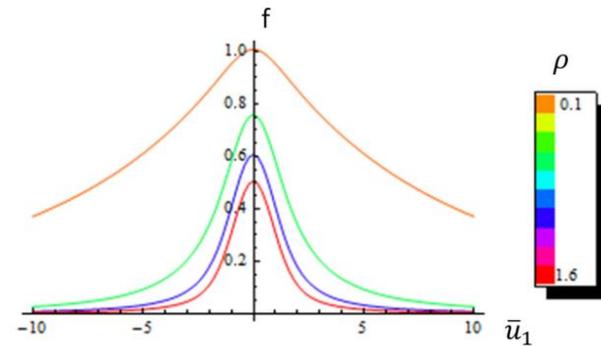
$$f(\rho, \bar{u}_1, \bar{y}_1) = \int_0^\infty \text{Re}[W(\bar{u}_1 + iy)][e^{-(\rho y - \bar{y}_1)^2} - e^{-(\rho y + \bar{y}_1)^2}] dy$$



Profile function f at $\rho = 1.4$



Profile on axis $\bar{u}_1 = 0$
maximum f locates at $\bar{y}_1 = 1, \bar{u}_1 = 0$



Profile on axis $\bar{y}_1 = 1$

$$z_r = \bar{u}_1 \sqrt{2\sigma_x^2 + 2\sigma_z^2 \left(\frac{1 - \cos \varphi}{\sin \varphi}\right)^2} + \left(\frac{\cos \varphi - 1}{\sin \varphi}\right) x_r$$

Estimated result



RMS value of satellite x-ray width
190 fs at 90° crossing angle
150 fs at 45° crossing angle

Estimated kick angle for NSLS-II

$$\Delta\theta_y(\varphi = 90^\circ) = \frac{eq_2 Z_0 c}{2\pi E_1} \frac{\gamma_2}{\sqrt{\gamma_2^2 + 1}} \frac{1}{\sqrt{2}\sigma_y} f(\rho, \bar{u}_1, \bar{y}_1)$$

NSLS-II bunch $\beta_x = 3.8$ m, $\beta_y = 25$ m, $\varepsilon_y = 10$ pm, $\sigma'_y = 0.6$ μ rad, $E_1 = 3$ GeV
 linac bunch $E_2 = 20$ MeV, $q_2 = 200$ pC, $\sigma_z = \sigma_y = \sigma_x = 35$ μ m

nominal kick angle

$$\Delta\theta_{y,0} = \frac{eq_2 Z_0 c}{2\pi E_1} \frac{\gamma_2}{\sqrt{\gamma_2^2 + 1}} \frac{1}{\sqrt{2}\sigma_y} = 24 \mu\text{rad}$$

profile function (assume $d = \sqrt{2}\sigma_y = 50$ μ m, $x_r = y_r = z_r = 0$)

$$f_{\max}(\rho = 1.4, \bar{y}_1 = 1, \bar{u}_1 = 0) = 0.54$$

kick angle

$$\Delta\theta_y = \Delta\theta_{y,0} \times f_{\max} = 24 \mu\text{rad} \times 0.54 = 13 \mu\text{rad}$$

much larger than required $5\sigma'_y = 3$ μ rad

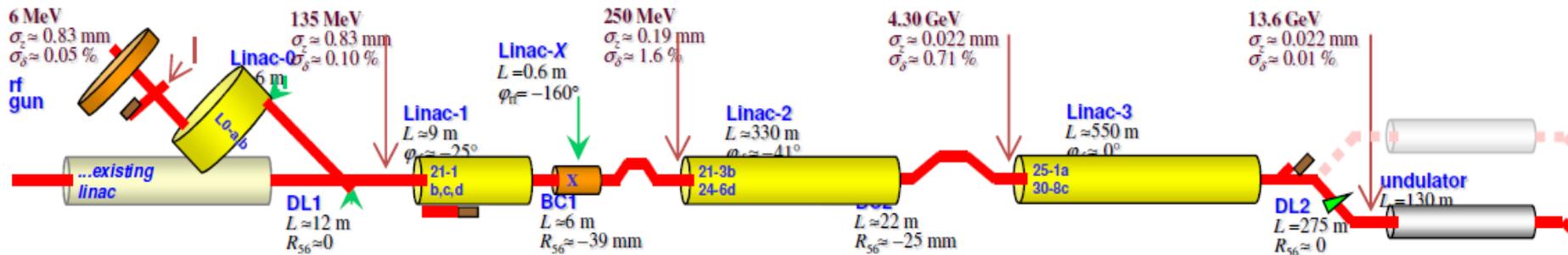
We need short and small (high current), low energy bunch with high charge

$$\begin{aligned} \sigma_x = \sigma_y = \sigma_z &= 35 \mu\text{m} \\ E_2 = 5 \text{ MeV}, q_2 = 50 \text{ pC} &\implies \Delta\theta_y = 3.2 \mu\text{rad}, \text{ x-ray } 150 \text{ fs} \\ E_2 = 20 \text{ MeV}, q_2 = 200 \text{ pC} &\implies \Delta\theta_y = 13 \mu\text{rad}, \text{ x-ray } 150 \text{ fs} \end{aligned}$$

Conventional bunch compressor

- Difficulty:
Space charge effects are very strong for low energy, high charge bunch.
- Conventional solution:
first accelerate bunch to high energy, then compress

LCLS, 1 km



Picture from S. Di Mitri's lecture of linac design for FEL

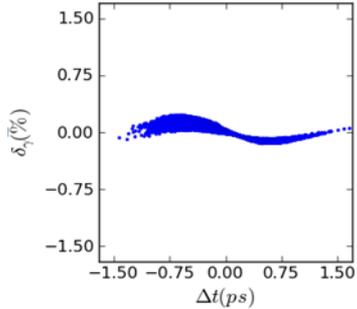
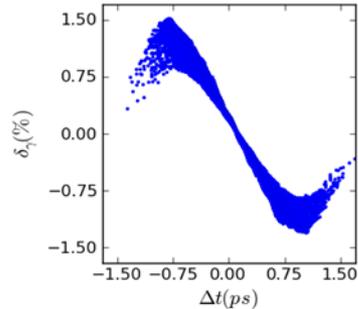
- But, we need a low cost (low energy) LINAC compressor

Unconventional low energy bunch compressor

- Try to compress bunch **without acceleration or with a short accelerating structure** after RF-gun
- Work at **low energy (5 MeV~22MeV)**, **space charge dominated regime**
- Bunch with **negative energy chirp** (head particle with higher energy)
- Compression section with **positive R_{56}**
- **designed two compressors (length<10m):**

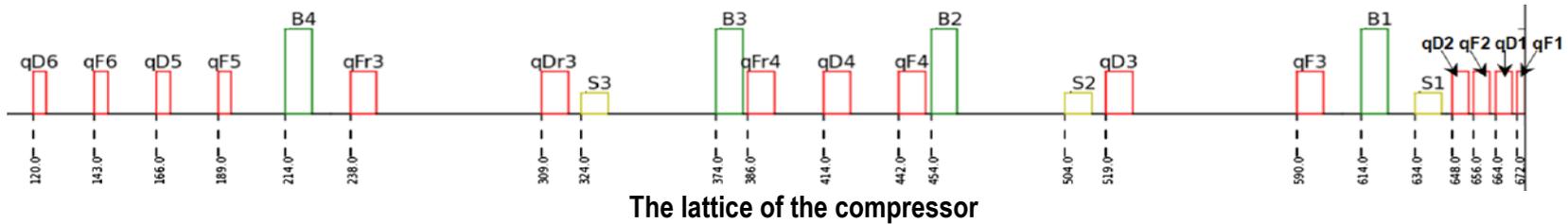
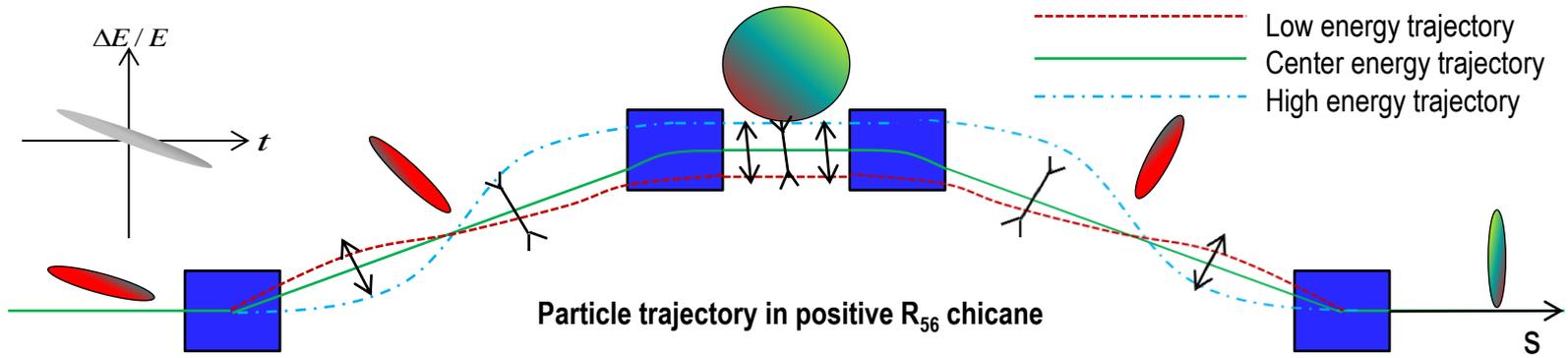
Gun	Optimized performances	Code	Optimizer
BNL RF gun (1~10 Hz)	~ 5 MeV, 50 pC, 166fs, 31um, 28um (1.27ps, 2mm, 2mm at cathode)	OptiM, ELEGANT, PARMELA	Genetic algorithm
LBNL VHF gun (at 186 MHz)	~ 22 MeV, 200 pC, 128 fs, 42 um, 25 um (8ps, 1.5mm, 1.5mm at cathode)	IMPACT-T, IMPACT-Z	Genetic algorithm

Using focus to increase energy chirp

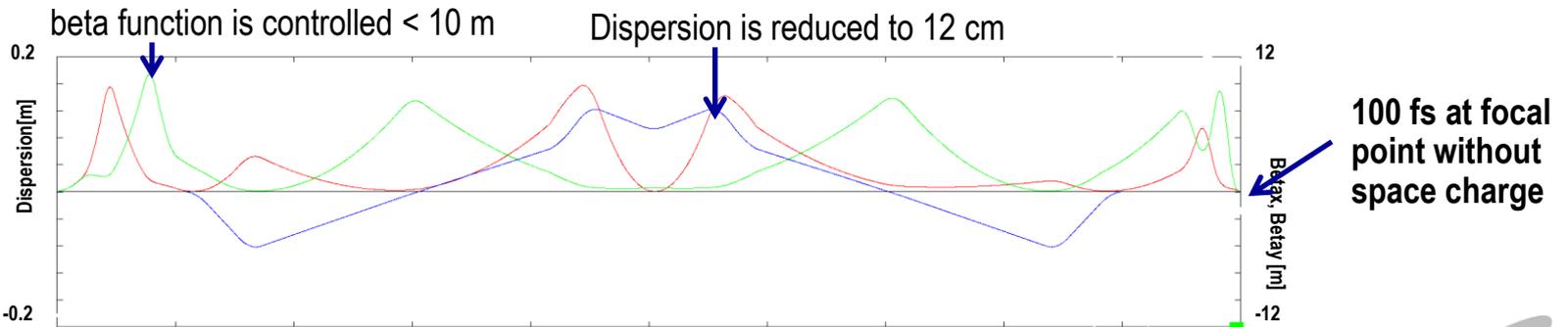
Chicane requirement 1: $\sigma_1 \approx \sqrt{(1 + hR_{56})^2 \sigma_0^2 + R_{56}^2 \sigma_\delta^2}$		$R_{56} = R_{56, \text{chicane}} + R_{56, \text{drift space}}$ $R_{56, \text{drift space}} = -s/\gamma^2$
$R_{56} = -1/h$		
Chirp at cathode -0.25%/ps (1/h=-120mm)	Chirp after focusing: -1.5%/ps (1/h=-20mm)	
$R_{56, \text{chicane}} = 170\text{mm}$	$R_{56, \text{chicane}} = 70\text{mm}$	
Large R_{56} -> longer compressed bunch length	Small R_{56} -> shorter compressed bunch length	
 <p>small negative chirp at the downstream of BNL RF-gun</p>	 <p>large negative chirp just at the upstream of chicane</p>	
Chicane requirement 2: (100fs final bunch length as a target) beta functions < 10m, dispersion function < 12cm, $R_{56, \text{chicane}} < 84\text{mm}$ energy chirp > 1% / ps		

- Space charge effects generate negative chirp---head particles has higher energy than tail's
- Focus the beam to increase space charge effects, then to increase the chirp

Positive R_{56} chicane

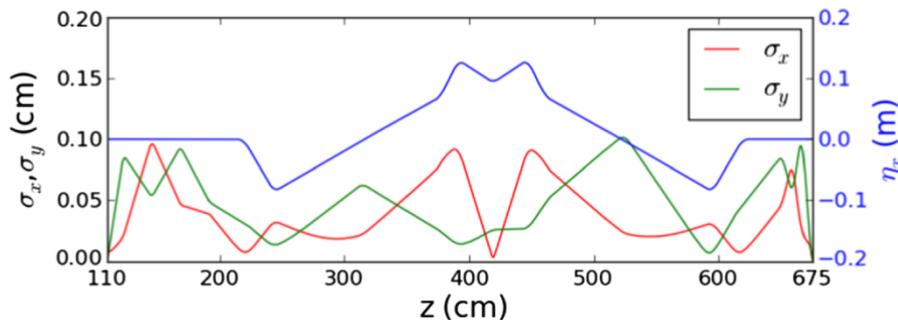


➤ Linear design result without space charge effects (OptiM, ELEGANT) -> 100 fs, 30 μm

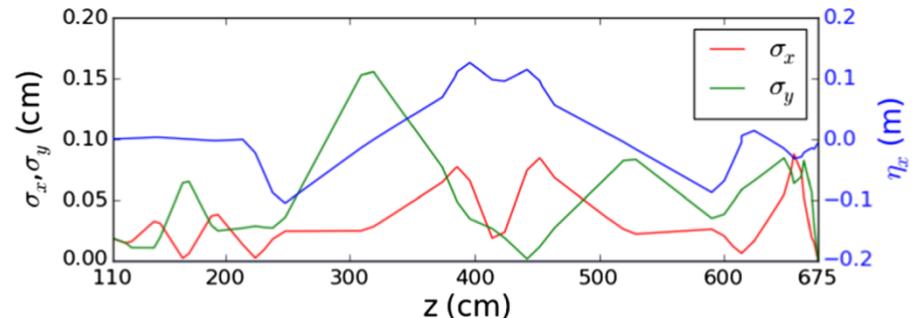


Redefine beta function and dispersion function in space charge dominated regime

- Turn on space charge: beta function and dispersion function loss meaning; 3-D blow up;
- Redefine:
 - equivalent **beta functions** using RMS beam size in **selected initial emittance ranges**
 - equivalent **dispersion** by averaging the trajectory in **selected initial energy ranges**
- Gradually increase charge and adjust quads to **restore “dispersion function” and “beta function”** to the same as the case without space charge
- 30 pC without blowing up, without losing particles (~ 700 fs)



Linear lattice functions along compressor without space charge effects from code OptiM



Nonlinear redefined functions with 50 pC space charge effects from code PARMELA

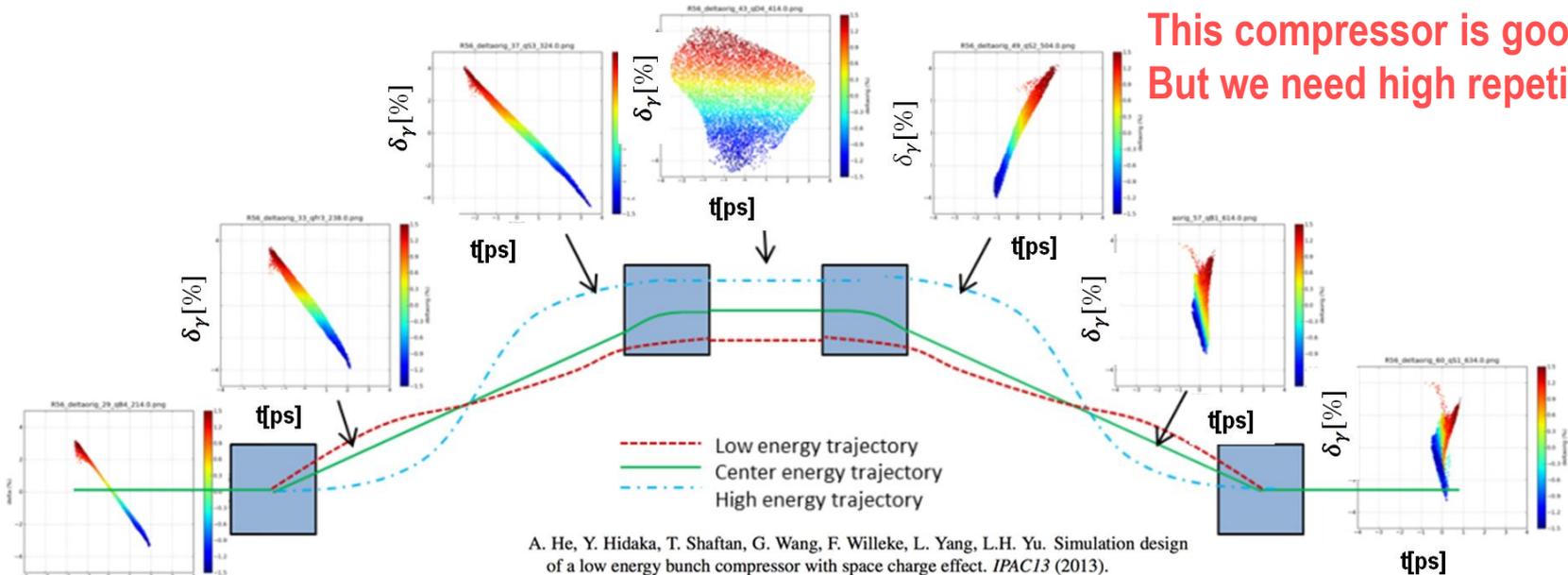
Global optimization using genetic algorithm

- **Variables:** laser pulse length, laser phase, solenoid strength, field strengths of magnets, etc.
- **Optimized objects:** bunch length, sum of transverse RMS beam sizes.
- **Constrains:** survival particle number

Thanks Dr. Lingyun Yang for the optimizer

- **Set the limits of variables** to reduce parameter scanning phase space.
- **Iterate the optimization** by using new range from last results.
- **Gradually increase charge** from 30 pC to 50 pC.
- **Result:** at 5MeV, 50pC, ~7m compressor ----> 1.27ps, 2mm, 2mm to **166 fs, 28 μ m, 31 μ m** .

Longitudinal phase space evolves during bunch compression



Benchmark and CSR effects

➤ Why design another compressor?

Thanks Dr. Ji Qiang for his generous guidance on the application of IMPACT-T & IMPACT-Z

High repetition rate: BNL RF-gun (1~10Hz) -> LBNL VHF RF-gun (186MHz)

CSR (coherent synchrotron radiation) effects: PARMELA -> IMPACT-T

bench mark the results between code PARMELA and IMPACT-T

➤ Verify our simulation results:

➤ Benchmark results between IMPACT-T and PAMELA for our linac compressor.

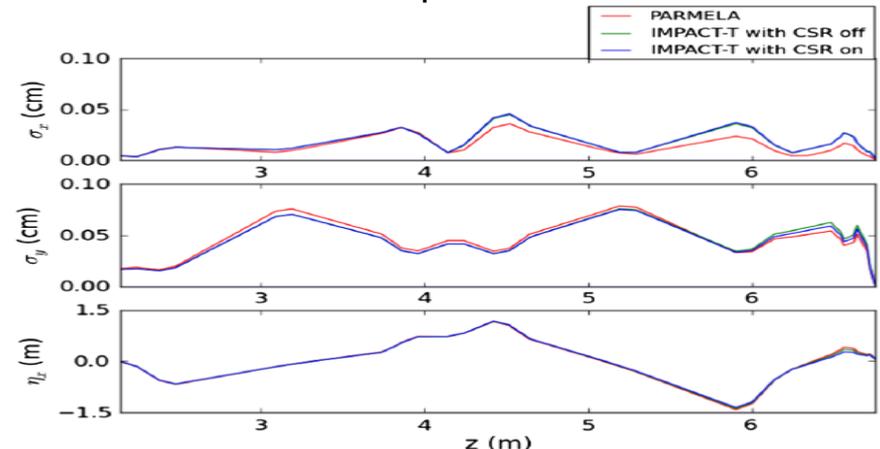
-> simulation results of two codes agree well

➤ Compare the simulation results when CSR effects turning on with that when turning off in IMPACT-T.

-> the CSR effects comparison shows that the bunch can be compressed and focused

TABLE III. The benchmark results of PARMELA against IMPACT-T and the comparison of CSR turning off with CSR turning on in IMPACT-T. We take the optimized 12 MeV, 150 pC bunch compressor of case 3 in Table II as an example to do the benchmark and comparison.

Code	CSR effects	σ_L^a [fs]	σ_H^a [μm]	σ_V^a [μm]
PARMELA	Off	145	35	24
IMPACT-T	Off	137	45	32
IMPACT-T	On	157	41	26



Low energy bunch compressor with VHF gun

- **Change gun** into LBNL's VHF gun (operated at 186MHz with 1MHz repetition rate), add two 1.3 GHz TESLA-like superconducting cavities.
- **Match beta functions** with those at the upstream of chicane at 13 MeV
- to increase bunch's charge and energy
- to scaling increase the strength of chicane magnets
- global optimization procedure using genetic algorithm**

TABLE I. Performances of the compressor.

Case	Charge [pC]	Energy [MeV]	σ_L^a [fs]	σ_H^b [μm]	σ_V^c [μm]
1	150	18	130	47	28
2	200	20	148	46	25
3	200	22	128	42	25

Optimized results of the two compressors

TABLE II. Examples of the optimized results for the two low energy compressor.

compressor	with BNL gun (6.77 m long)		with LBNL VHF gun (8.74 m long)		compressed ratio
	initial bunch	focused ^a bunch	initial bunch	focused ^a bunch	
longitudinal bunch length [fs]	1270 ^b	166 ^c	6783 ^d	128 ^c	26
horizontal beam size [μm]	2000 ^b	31 ^c	1994 ^d	42 ^c	47
vertical beam size [μm]	2000 ^b	28 ^c	1971 ^d	25 ^c	79
energy spread [%]	$\Delta E/E$ 0.09 ^e	0.93	0.0014 ^e /0.98 ^f	1.38	
average kinetic energy [MeV]	E 4.69 ^e	4.69	0.73 ^e /22 ^f	22	
horizontal emittance [μm]	ε_x 0.177 ^e	1.02	59 ^e /0.143 ^f	0.71	
vertical emittance [μm]	ε_y 0.189 ^e	0.84	58.5 ^e /0.142 ^f	0.19	
charge [pC]	Q 50	50	200	200	

^a be calculated for 90% of particles, with 10% tails cut off.

^b at cathode: longitudinal distribution is Gaussian with $2\sigma_z=1.27$ ps; transverse distribution is uniform with the same radius of 2 mm.

^c RMS value

^d at cathode: longitudinal distribution is flat-top with linear ramp at two ends total length from head to tail is 6.78 ps; transverse distribution is uniform ell with hard cut edge, the diameter of the ellipse in x and y is 1.99 mm.

^e at gun exit

^f after RF acceleration

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Design of low energy bunch compressors with space charge effects

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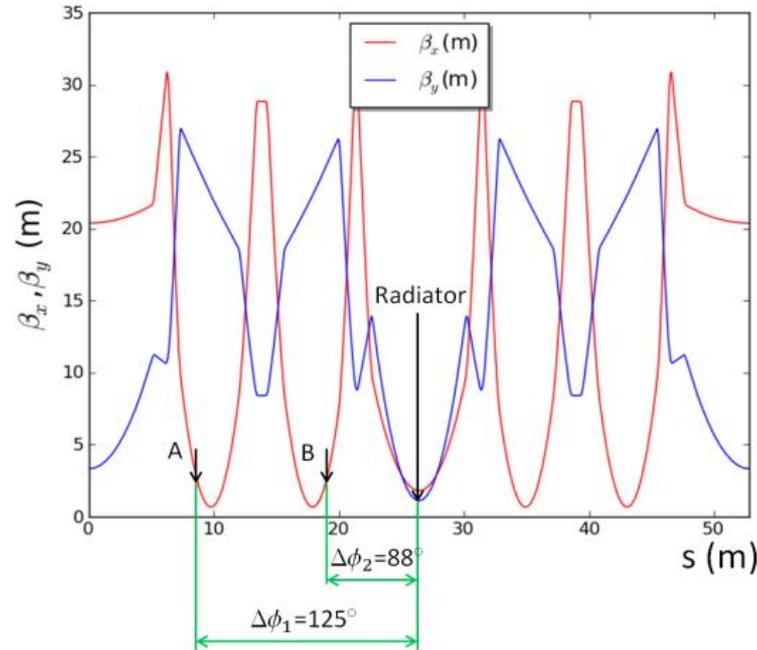
Low energy linac bunch compressor
to obtain a very short bunch with low =>
emittance at low energy

A breakthrough for FEL linac



Produce two bunches using one linac => HGHG FEL

Kick point in NSLS-II lattice



- Choose maximum β_y to maximize the angular separation of the slice from the core
- Choose minimum β_x to minimize the slice bunch length

point A: $\Delta\phi_A = 125^\circ$, $\beta_y = 25$ m, $\beta_x = 3.8$ m

point B: $\Delta\phi_B = 88^\circ$, $\beta_y = 25$ m, $\beta_x = 3.8$ m

Slice profile at kicker and radiator

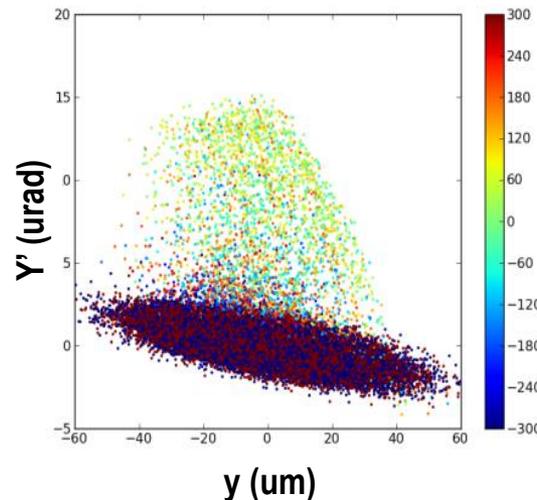
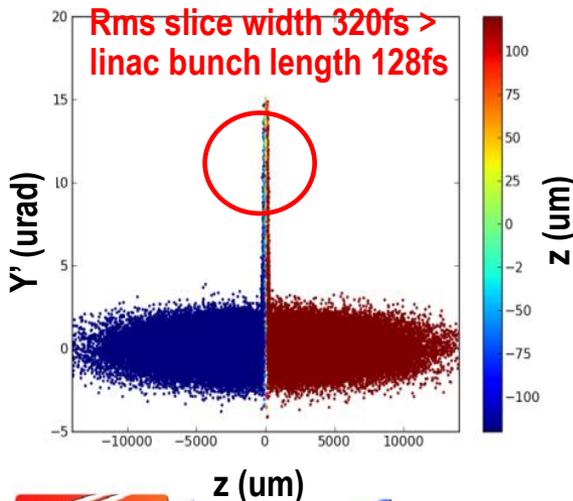
- Calculate slice profile:

Using 6D distribution at final focus point from our designed compressor as the simulated linac bunch

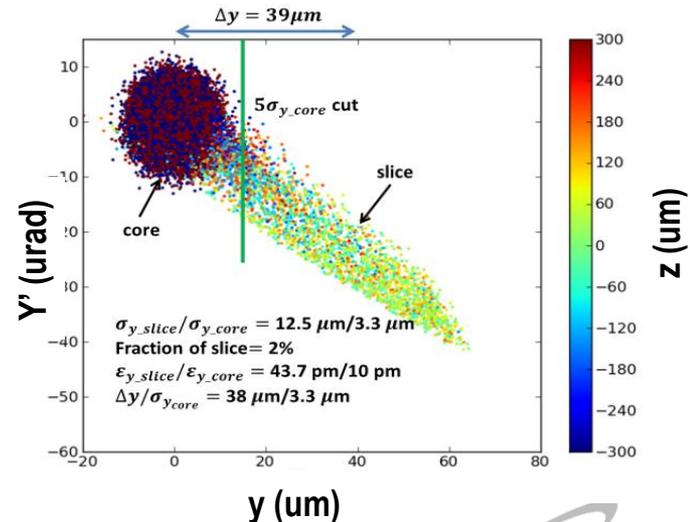
- code: ELEGANT (to track the transport of phase space distribution)
- particle number: 10,000 for low energy linac bunch

100,000 for high energy storage ring bunch

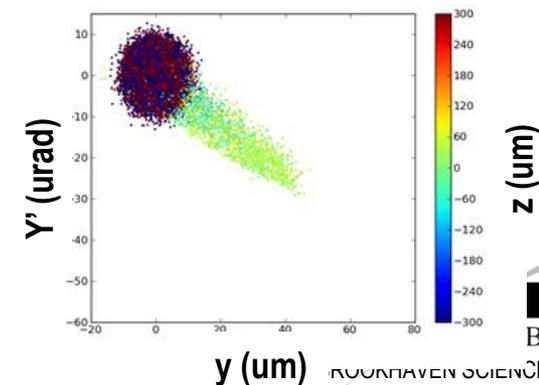
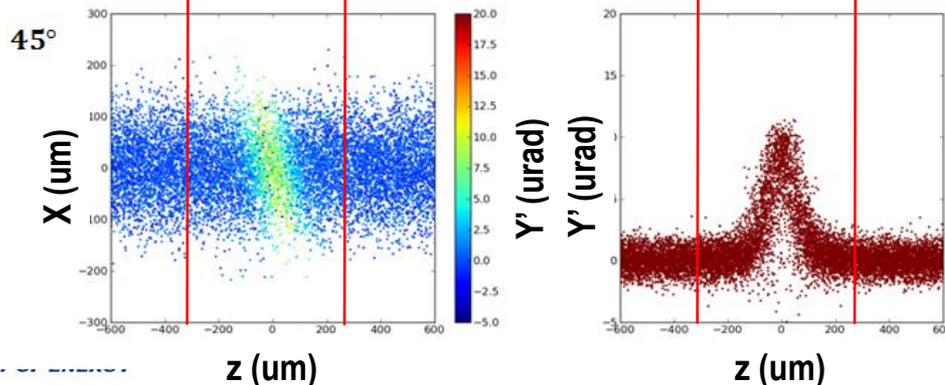
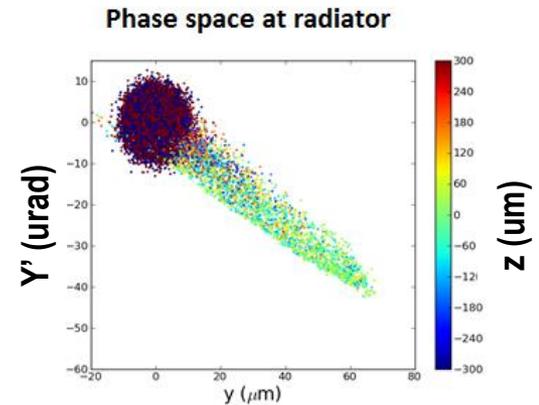
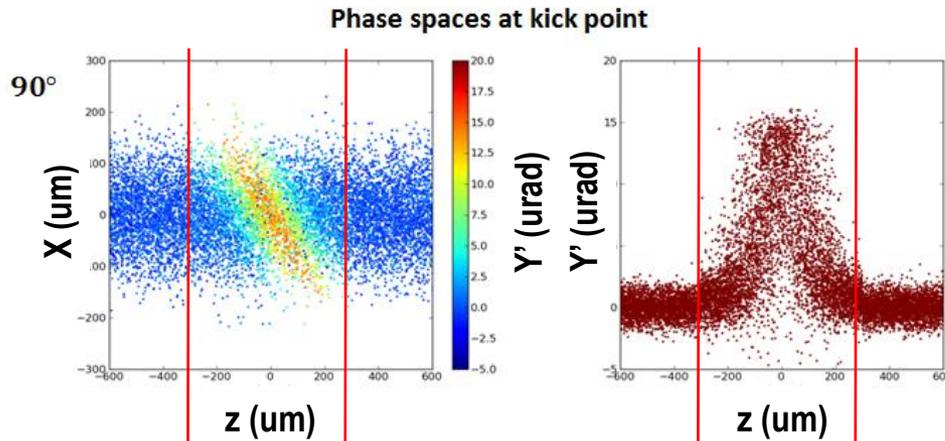
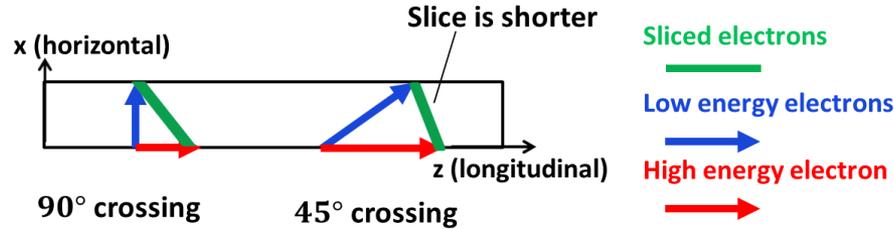
Phase spaces right after the kick



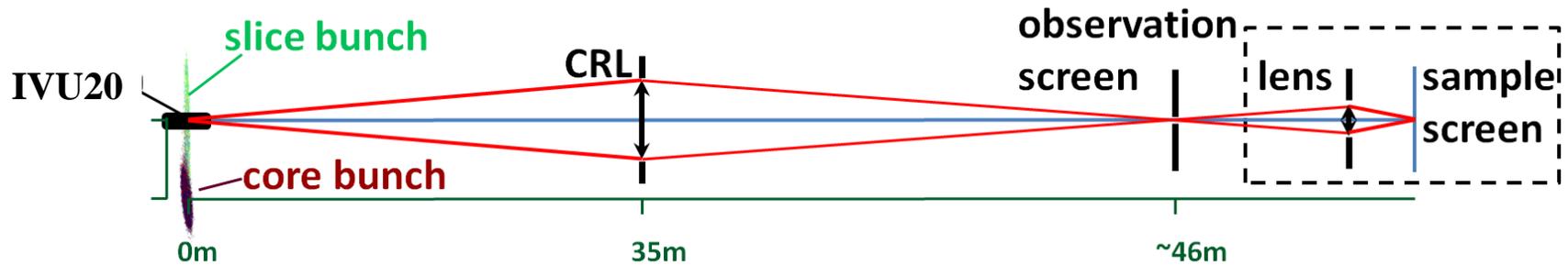
Phase space at the radiator



Reducing crossing angle to reduce slice pulse length



Beam line design for radiation separation



Thanks Dr. Oleg Chubar for his generous guidance on the use of SRW and the separation calculation.

A. He, O. Chubar, L.H. Yu. Separation of hard X-ray synchrotron radiation from electron beam slices. to be submitted in *Proc. SPIE* (2014).

- Angular + spatial hybrid separation
- Pure spatial separation
- Code: SRW (synchrotron radiation workshop)

TABLE III. Separation performances of hard x-ray synchrotron radiation from electron beam slices. Data are recorded at 7.8 KeV on the observation screen.

Crossing angle	Separate type	Flux/pulse ^a [photons/0.1%bw]	Flux ^b [photons/ sec /0.1%bw]	Peak intensity [photons/ sec /0.1%bw/mm ²]	SNR	Pulse length [fs]
90°	Spatial + angular	10×10^3	10×10^8	2.1×10^{10}	12	320
	Spatial	18×10^3	18×10^8	6.5×10^{10}	5	320
45°	Spatial + angular	5×10^3	5×10^8	1.1×10^{10}	8 ^c (2.6)	150
	Spatial	5×10^3	5×10^8	3.6×10^{10}	8 ^c (2.7)	150

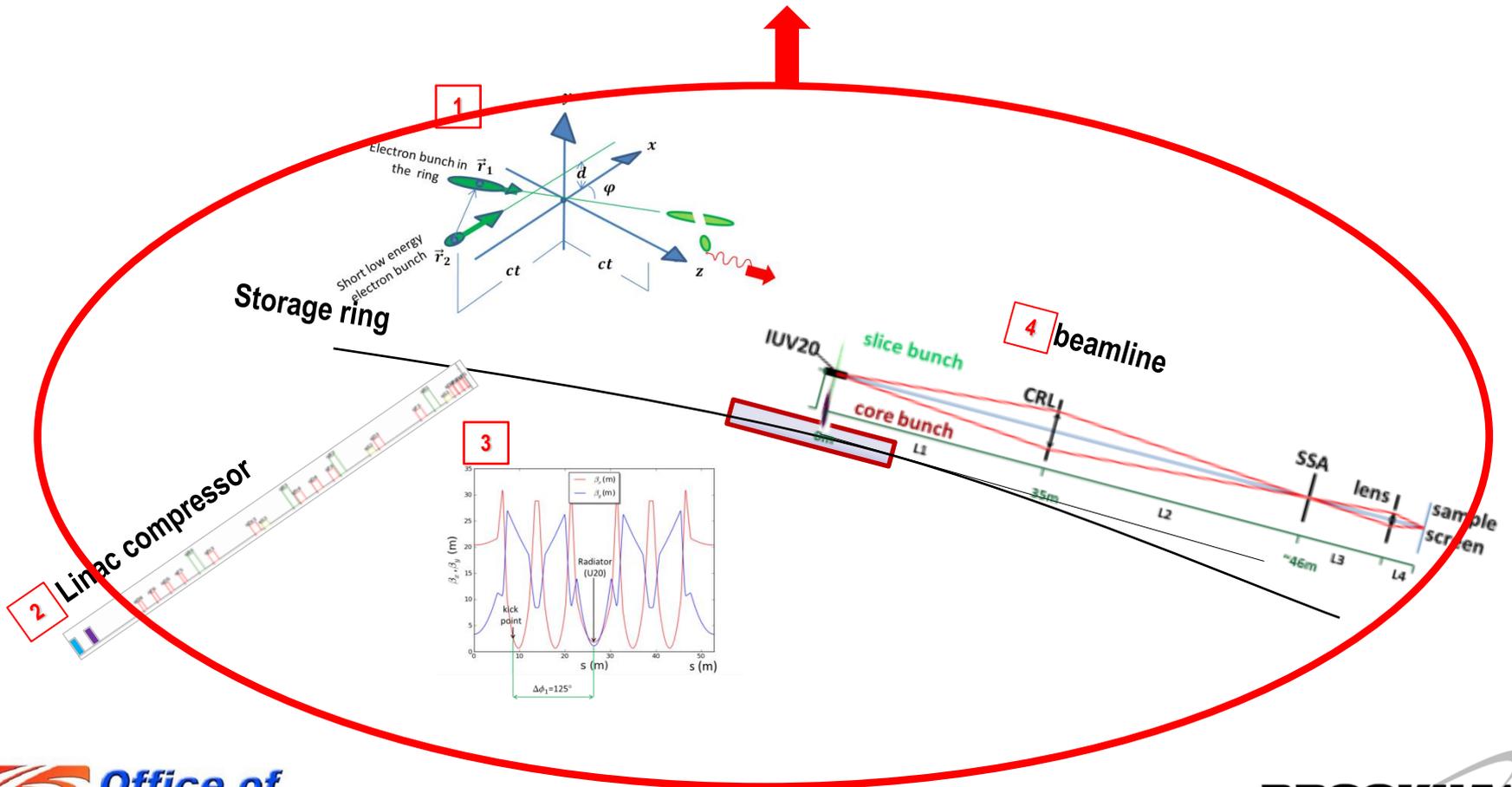
^aAssume NSLS-II's revolution time is about 2.6 μ s, then flux/pulse = power \times 2.6 μ s.

^bAssume the repetition rate of the low energy linac is 100 kHz, then flux = flux/pulse \times 100 kHz.

^cWith 10 ps of the detector's time resolution.

The last issue

System's photon flux and repetition rate ?



Photon flux

➤ Estimated photon flux

U20: 10^{15} photons/sec/0.1%BW (8 keV, 500mA)
 ring: current 500 mA, 1000 bunches;
 revolution time: 2.6 μ s
 slice fraction: 0.3 ps/30 ps

single pulse photon flux:

$$10^{15} \times 0.3 \text{ ps}/30 \text{ ps} \times 2.6 \text{ } \mu\text{s}/1000$$

$$= 2.6 \times 10^4 \text{ photons}/0.1\% \text{BW}$$

➤ Simulation results of photon flux (code: SRW)

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	Spatial	5×10^3	5×10^8	3.6×10^{10}	8 ^c (2.7)	150

^aAssume NSLS-II's revolution time is about 2.6 μ s, then flux/pulse = power \times 2.6 μ s.

^bAssume the repetition rate of the low energy linac is 100 kHz, then flux = flux/pulse \times 100 kHz.

^cWith 10 ps of the detector's time resolution.

Emittance increase and repetition rate

Estimated emittance increase for a single bunch

- 1) induced by one time angular kick: $0.3 \text{ ps}/30 \text{ ps} \times 5^2 \times 1/2\varepsilon_y = 12\%\varepsilon_y$
(assume $5\sigma'_y$ kick with a slice of 300 fs/ 30 ps)
- 2) due to the damping time in storage ring: $12\%\varepsilon_y \times \text{damping time (10 ms)}$
- 3) if a single bunch is kicked with 100 Hz repetition rate: $12\%\varepsilon_y \times 10 \text{ ms} \times 100 \text{ Hz} = 12\%\varepsilon_y$

Distribute the kicks uniformly over all 1000 bunches



Repetition rate 100 kHz, photon flux $\sim 10^9$ [photons/sec/0.1%bw]



Repetition rate limit 100 kHz \sim 1MHz, depending on tolerance of the vertical emittance increase

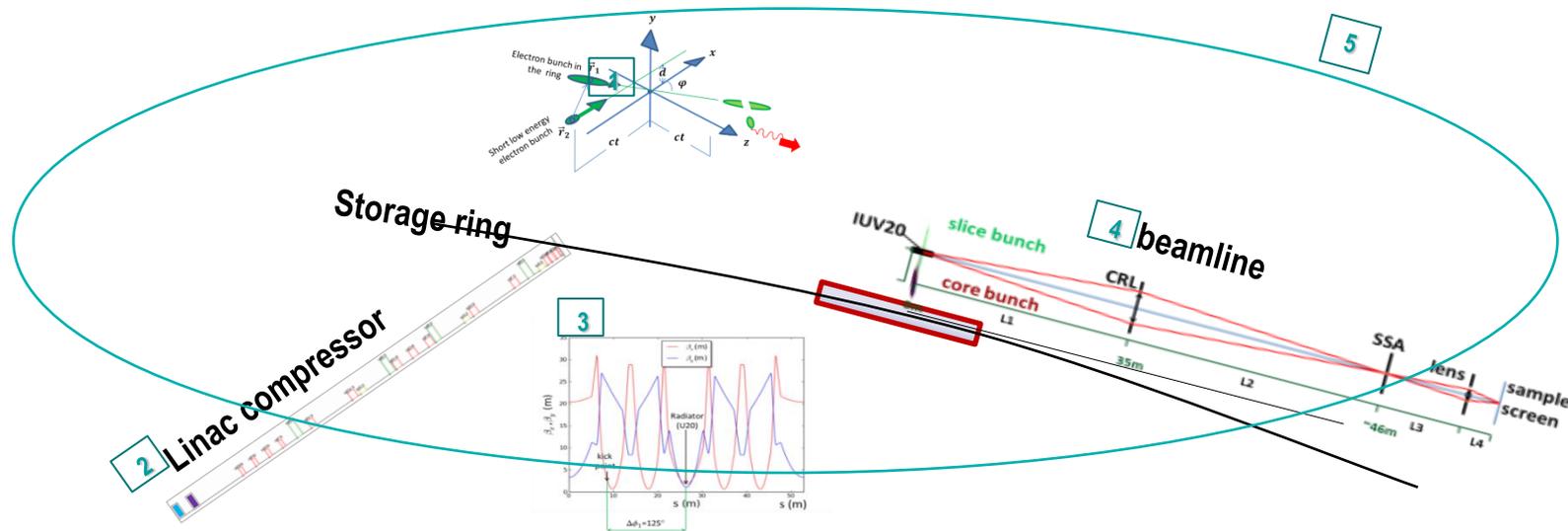
Summary

Ultrashort x-ray pulse generation by electron beam slicing in storage rings

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(Received 20 August 2013; published 4 April 2014)



	Laser slicing	Crab cavity	X-ray FEL	Ebeam slicing
source	Storage ring	Storage ring	FEL	Storage ring
Occupied ring space	large	large	large	small
Pulse length	~ 100 fs	~ ps	< 100 fs	~150 fs
Photon flux	~ 10 ⁶ photons/sec/0.1%bw	~ 10 ¹⁴ photons/sec/0.1%bw	~ 10 ¹² photons/sec/0.1%bw	~ 10 ¹⁰ photons/sec/0.1%bw
Repetition rate	1 kHz	100 MHz	Low (120Hz for LCLS)	1 MHz
Pulse to pulse stability	good	good	poor	good

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BOOK:

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