



# ***Phase Space Manipulations of Electron Beams Between Two Degree-of-Freedoms & Potential Applications***

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# Credits

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- Contributor on emittance exchange
  - P. Emma, Wei Gai, Z. Huang, K.-J. Kim, J. Power, Yin-e Sun, M. Rihaoui
- Contributor on flat beam generation
  - N Barov, K. Flottmann, D. Edwards, H. Edwards, D. Mihalcea, S. Lidia, Y.-e Sun, N. Vinogradov
- Experimental work is done as part of a collaboration between ANL/U. of Chicago, FNAL, NIU, and Tsinghua University.



# Outline

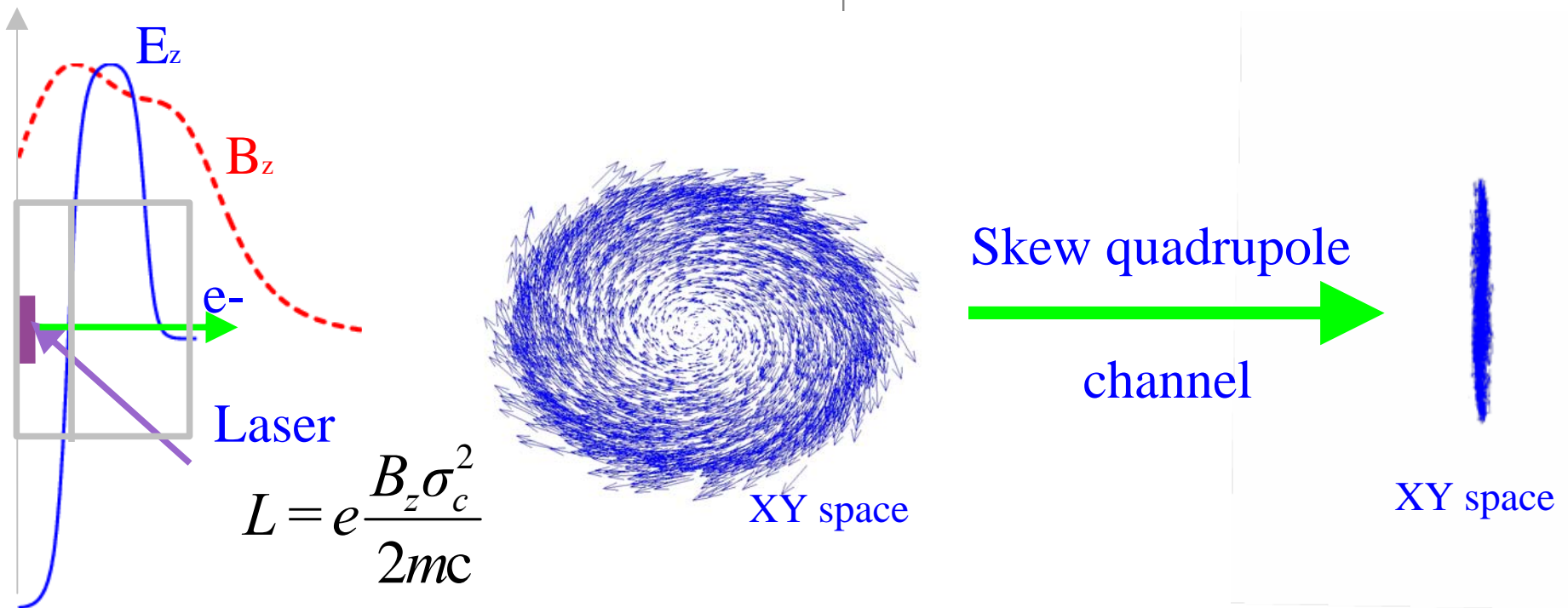
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- Motivations
- Flat beam transform
  - Theoretical background
  - Experimental measurements
    - Historical remarks
    - Potential applications
- Transverse-to-longitudinal emittance exchange
  - Theoretical background
  - Potential applications
  - Plans for proof-of-principle experiment
- Summary



# Production of flat beams

- Flat beam production relies on:
  - Generation of magnetized beam
  - A linear transformation devised by Ya. Derbenev to apply a torque on the beam



PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS, VOLUME 4, 053501 (2001)

## A low emittance, flat-beam electron source for linear colliders

R. Brinkmann, Y. Derbenev, and K. Flöttmann

DESY, D-22603 Hamburg, Germany

(Received 9 December 2000; published 18 May 2001)

We present a method to generate a flat (large horizontal to vertical emittance ratio) electron beam suitable for linear colliders. The concept is based on a round-beam rf photoinjector with finite solenoid field at the cathode together with a special beam optics adapter. Computer simulations of this new type of beam source show that the beam quality required for a linear collider may be obtainable without the need for an electron damping ring.

DOI: 10.1103/PhysRevSTAB.4.053501

PACS numbers: 29.17.+w, 41.75.Fr



# Production of flat beams

- A B-field on the photocathode imposes an averaged (over the beam) canonical angular momentum (CAM):

$$L_0 = \frac{eB}{2mc} \sigma_c^2$$

- Outside of the solenoid this CAM is converted into mechanical angular momentum (MAM)

$$L = \frac{eB}{2p_z} \sigma_c^2$$

- The MAM can then be removed by a properly design skew quadrupole channel (Derbenev's transform) to yield a flat beam

$$\varepsilon_{\pm} = \sqrt{L^2 + \varepsilon^2} \pm L, \text{ and } \varepsilon_+ \varepsilon_- = \varepsilon^2$$

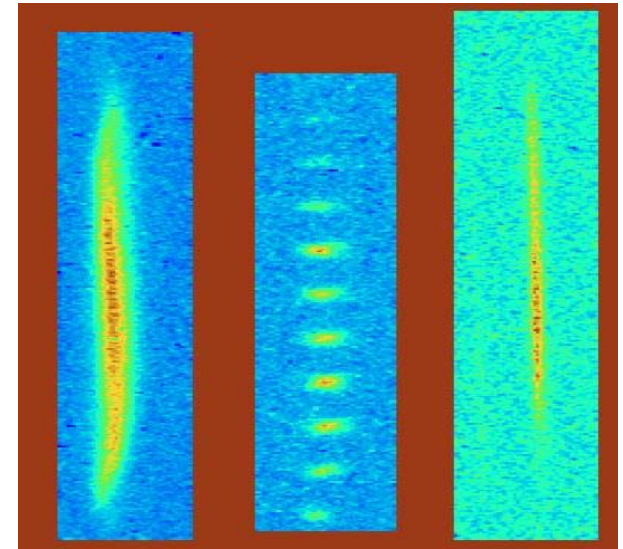
Angular momentum

Transverse uncorrelated emittance



# Historical notes

- 1988: *Reich et al.* partial decorrelation noted downstream of an ECR source using one skew quadrupole
- 1999: Proposal for a flat beam injector Brinkmann, Flottmann and Derbenev
- 2000: *D. Edwards et al.* total decorrelation and production of flat beam demonstrated at Fermilab
- 2004: *Y.-E Sun et al.*, generation and characterization of angular momentum-dominated beams
- 2006: *P. Piot et al.* demonstration of emittance ratio  $>100$

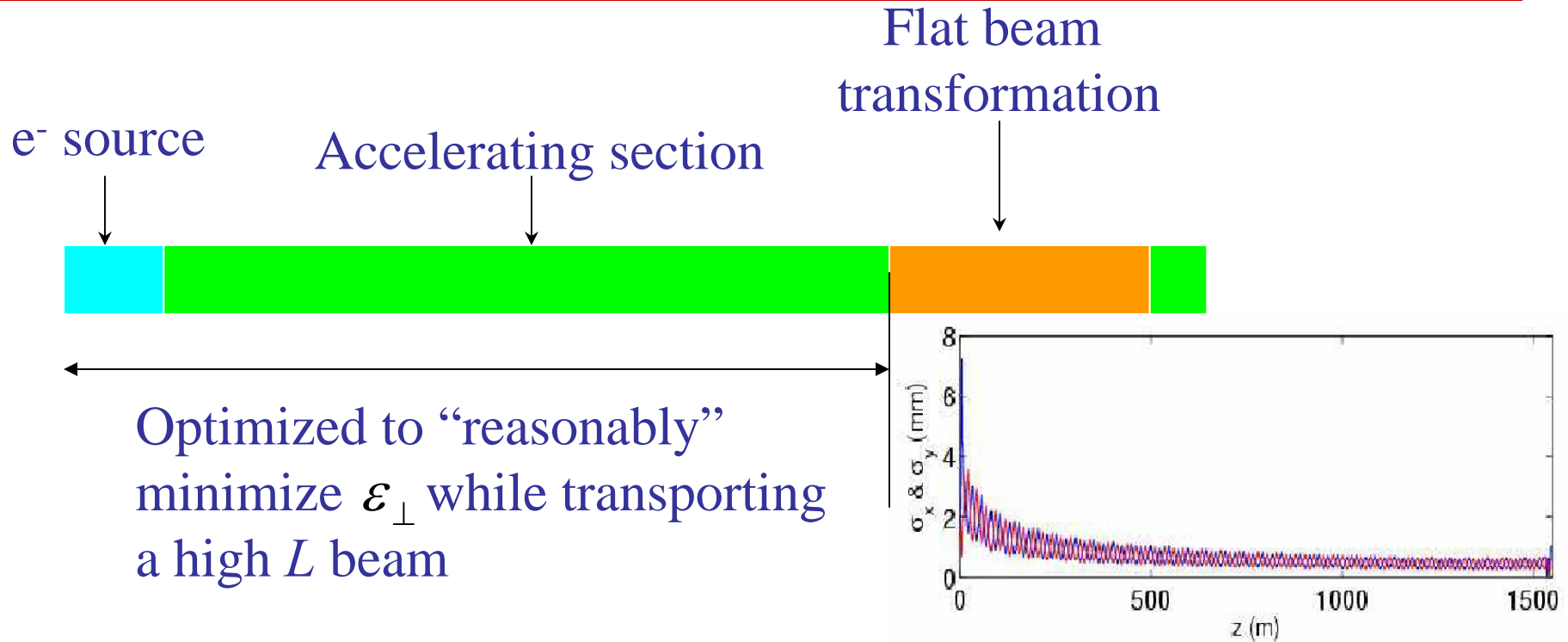


SPOT    YMS    XMS

*[D. Edwards et al. LINAC 2000  
Y.-E Sun Phd dissertation Univ.  
Of Chicago (2005)]*



# Applications: flat beam for linear collider? (1)



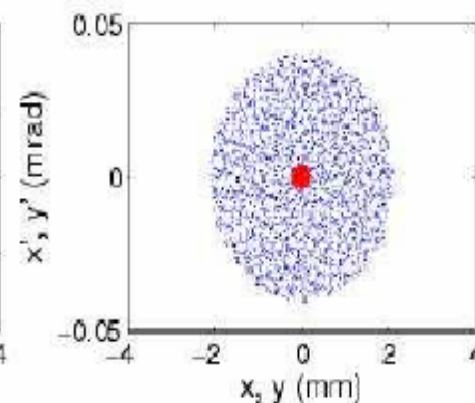
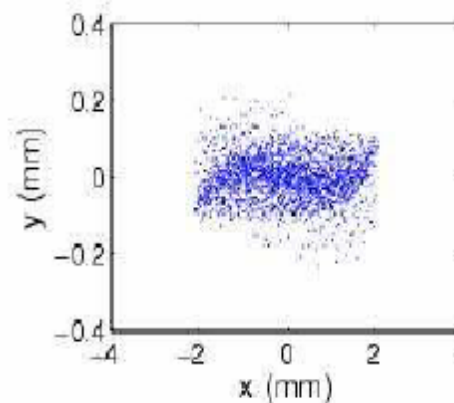
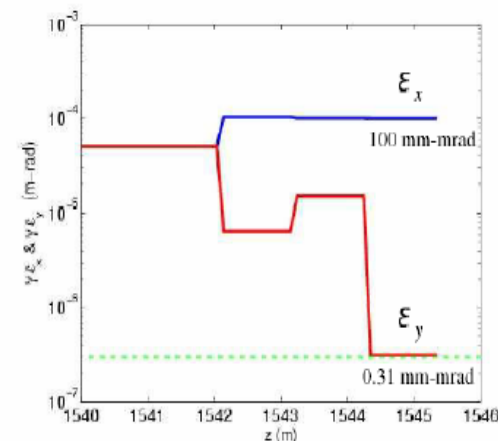
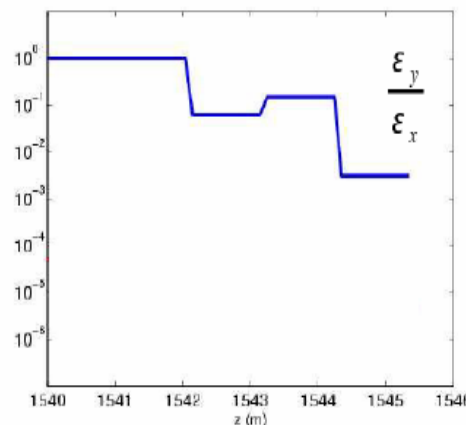
- Design and numerically optimize an injector capable of providing emittance ratio compatible with linear collider requirements
- Minimize 4D emittance





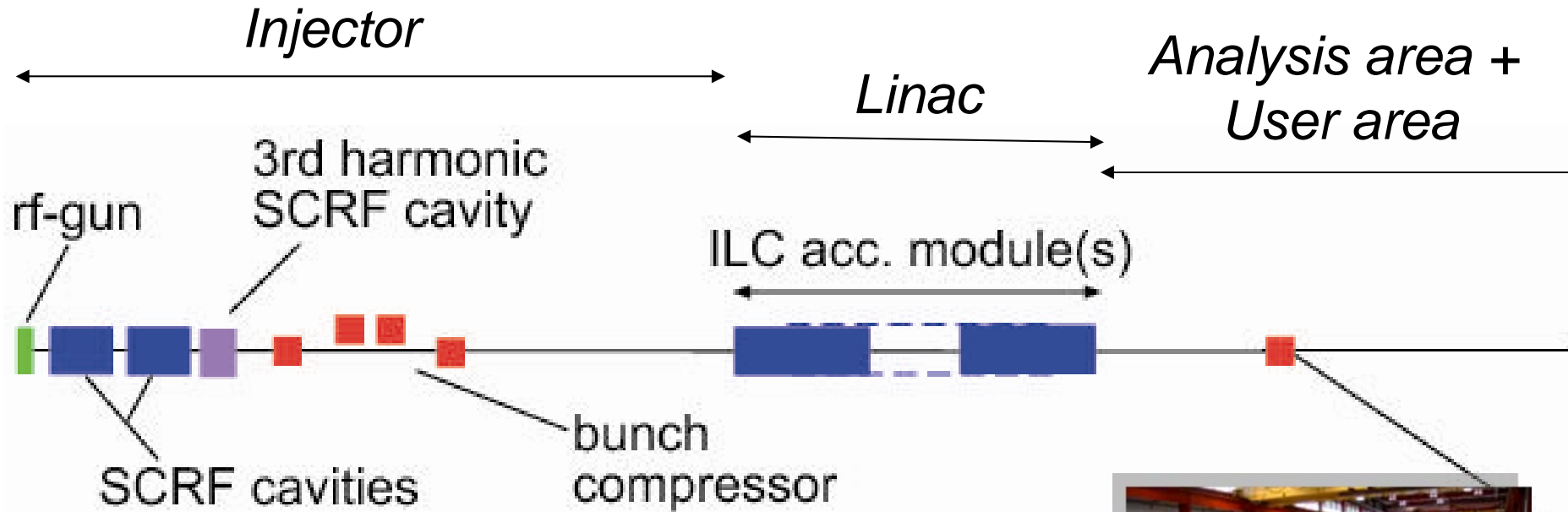
# Applications: flat beam for linear collider? (2)

- Flat beam transformer at 5 GeV yields: emittance ratio of 320
- However both emittances are too high
- A photoinjector cannot provide the adequate 4-D emittance at 3.2 nC
- Could add on a “cooling” to decrease both emittance by a factor  $\sim 10$ .





# Application to some Advanced Accelerator R&D topics at ILCTA



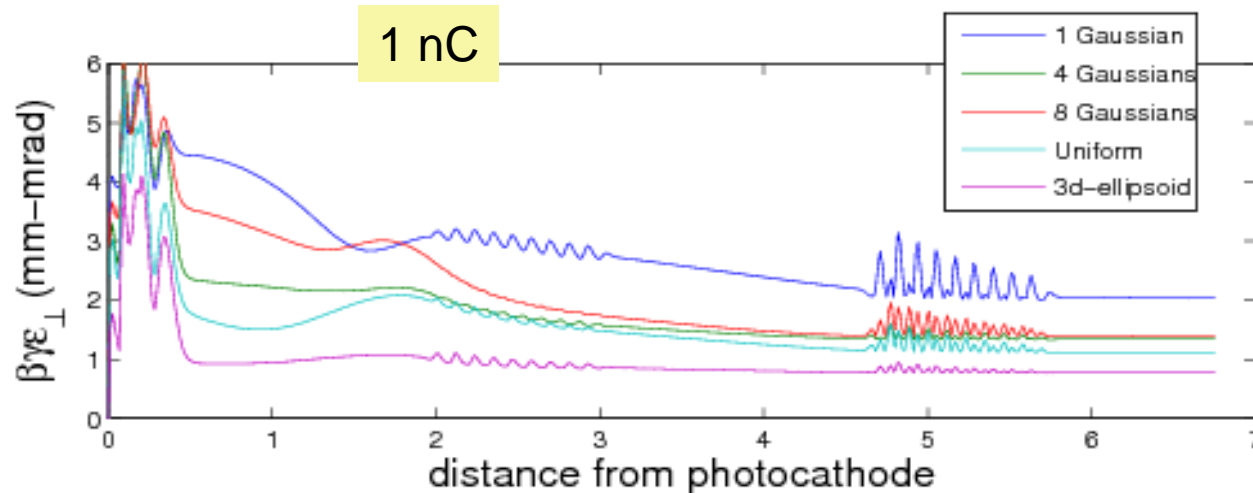
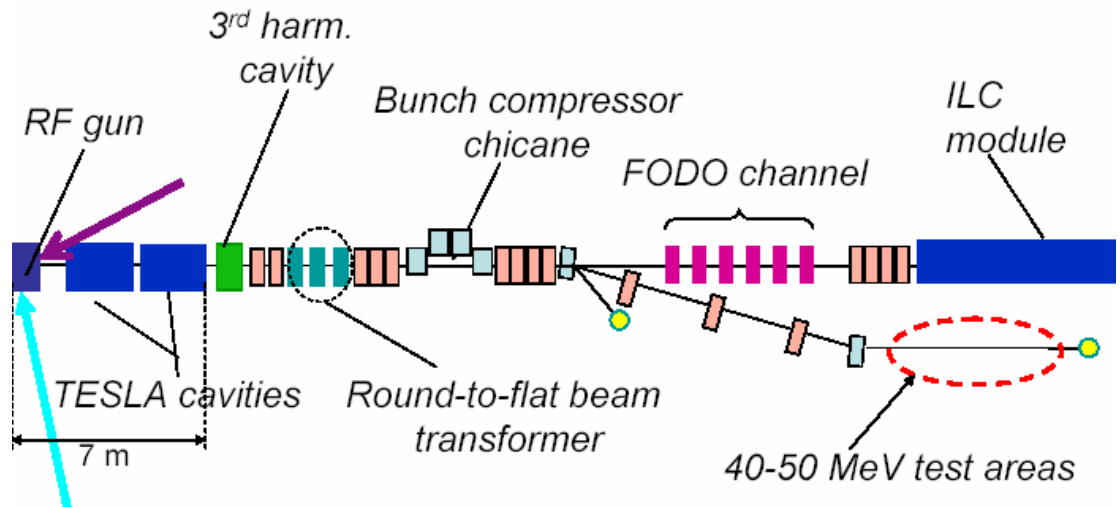
- Main goal: test ILC critical components
- Hidden agenda: do some advanced accelerator R&D and beam physics studies

*(M. Church, S. Nagaitsev, P. Piot, PAC 2007)*



# Application to some Advanced Accelerator R&D topics at ILCTA

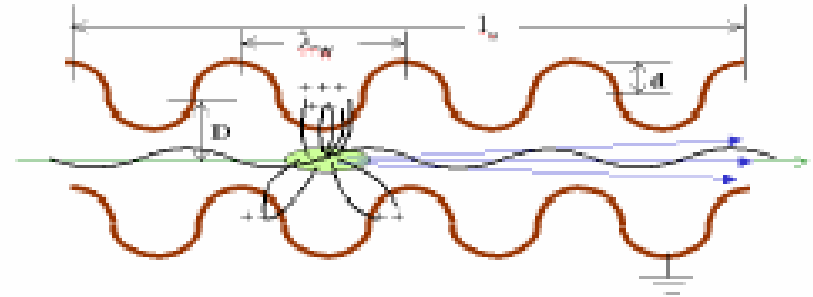
- A high brightness injector was designed (NIU/FNAL collaboration)
- Can achieve (simulation) the “canonical” 1 nC/ 1  $\mu\text{m}$  (without compression)



# Applications: Image charge undulator

- An e- propagating next to a grating emits radiation (so-called Smith-Purcell radiation)

$$\lambda = \frac{\lambda_w}{2\gamma^2} \left( 1 + \frac{K^2}{2} \right)$$



- $K$  is the “undulator parameter”

$$K = \frac{\lambda_w}{2\pi} \frac{eB}{mc}$$

(*Y. Zhang et al. PAC 2003 p. 941*)

(usually  $K = \frac{\lambda_w}{2\pi} \frac{eE}{mc^2}$ )

- A 8 GeV beam, with 300x4x100 μm at 10 nC passing through a grating with 10 μm period  $K=0.2$  (equivalent to a 60 T magneto-static undulator),  $\lambda=1$  Angstrom, and gain length is 2 cm -- **compare to TESLA X-ray FEL ~10 m with ~25 GeV linac**
- Scale down to optical regime 250 MeV and implement at ILCTA?  
Collaboration with JLab?



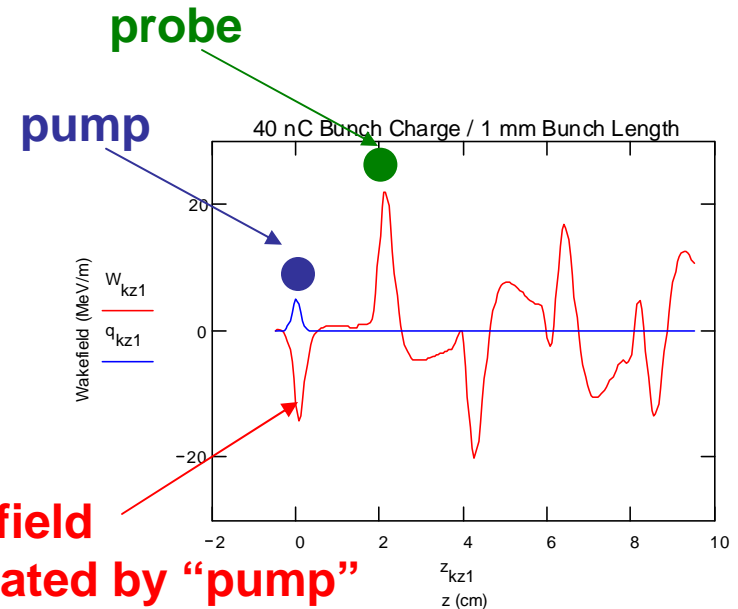
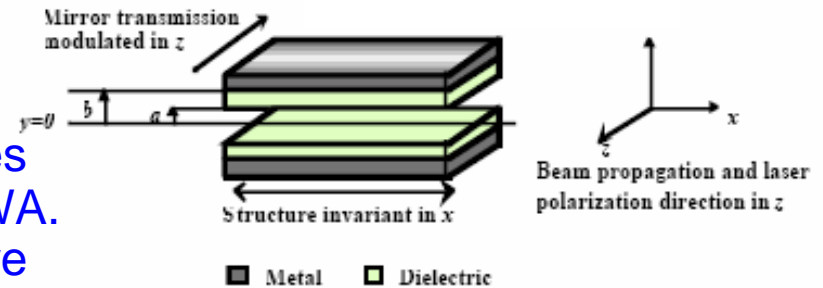
# Applications: Dielectric slab as accelerating structures

- Wakefield scales as:

$$W_{\parallel} \propto \frac{Q}{\sigma_z^2}$$

- Dielectric cylindrical-symmetric structures (MgTiO<sub>3</sub> ;  $\epsilon=16$ ) have been tested in AWA. Axial average gradient of 100 MV/m were measured
- Wakefield accelerators based on a probe-pump configuration
- Slab-type structure reduce transverse wakefield sensitivity
- With ILCTA parameters we contemplate gradients of the order of GeV/m

*(Courtesy of John Power and Wei Gai of Argonne Wakefield Accelerator)*

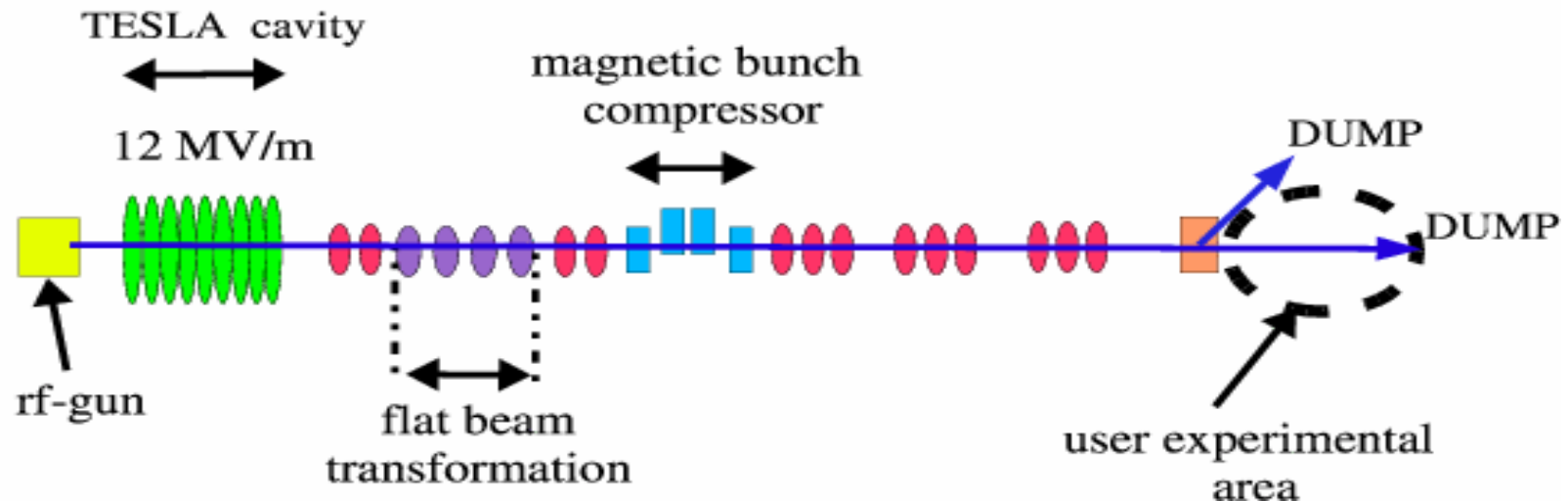


**Wakefield generated by "pump"**



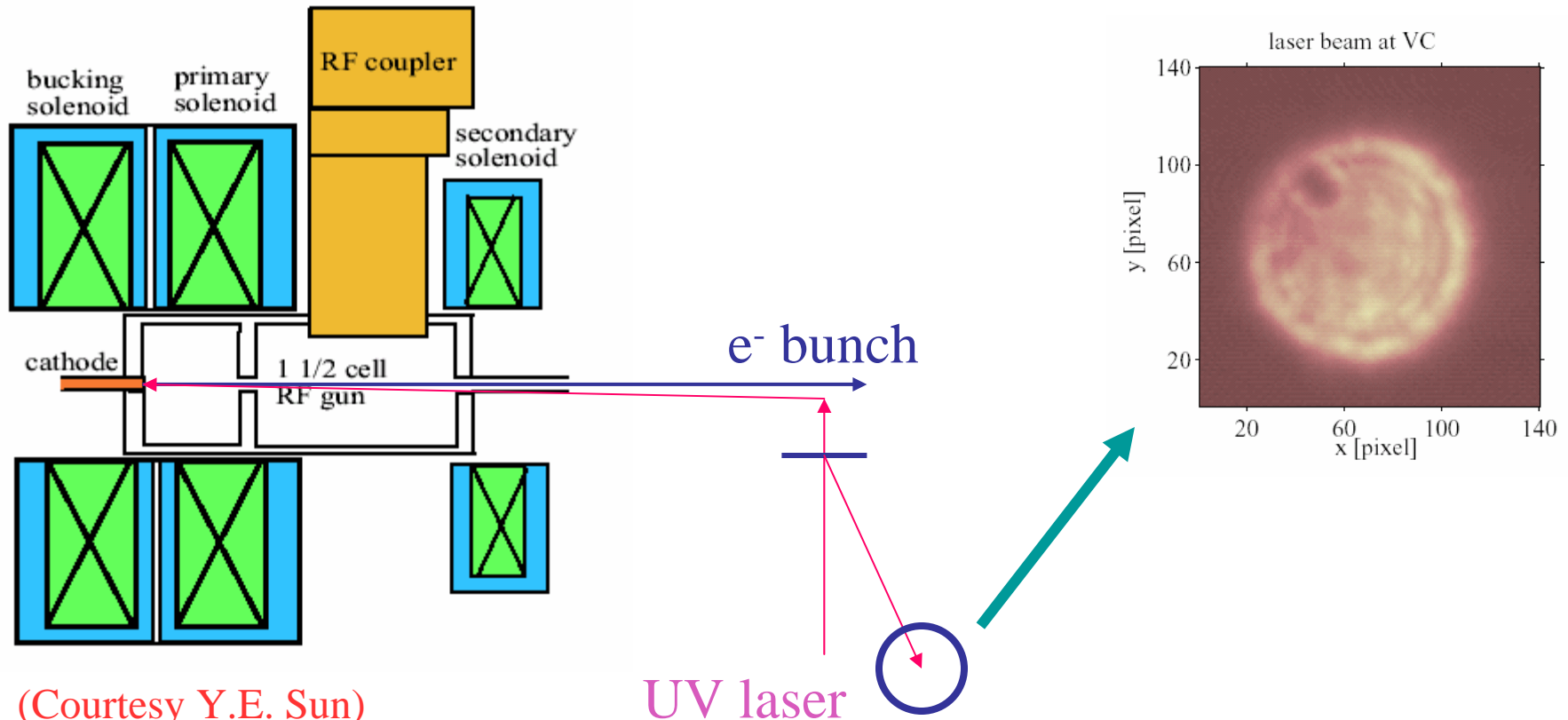
# Experiment at the Fermilab/NICADD photoinjector laboratory (FNPL)

- Photo-emission electron source
- A TESLA cavity operating at 12 MV/m
- Quads, correctors magnets, dipoles and extensive diagnostics (OTR and YaG-based screens, electromagnetic beam position monitors)
- Bunch compression possible with a magnetic chicane
- Soon to be decommissioned



# The FNPL 1+1/2 rf-gun

- High quantum efficiency photo-cathode (Cesium Telluride)
- A 1.3 Ghz rf-gun
- Three solenoids with independent power supplies



(Courtesy Y.E. Sun)

UV laser



# Scaling of angular momentum (1)

- Conversion of canonical angular momentum (CAM) into mechanical angular momentum is as predicted

- CAM calculated from:

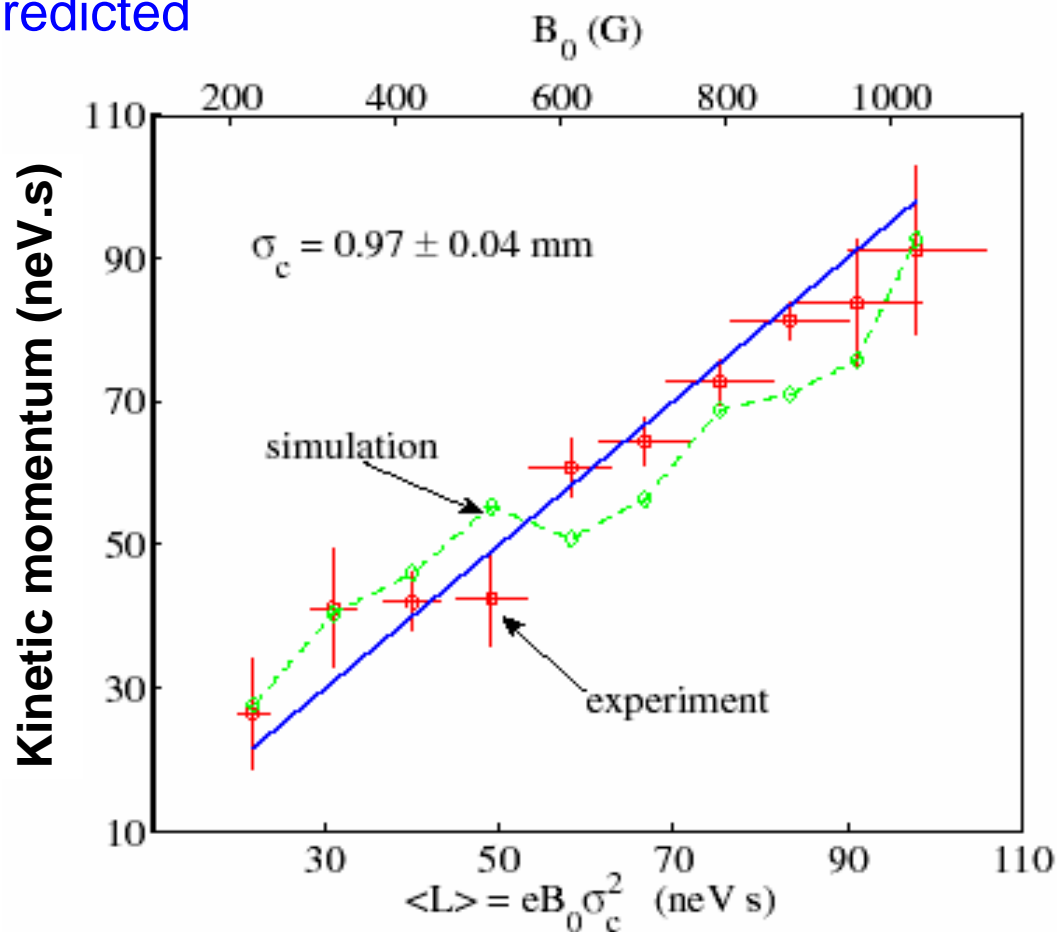
B-field on cathode  
( POISSON)

$$\langle L \rangle = e B_0 \sigma_c^2$$

averaged CAM

transverse rms size  
on photocathode

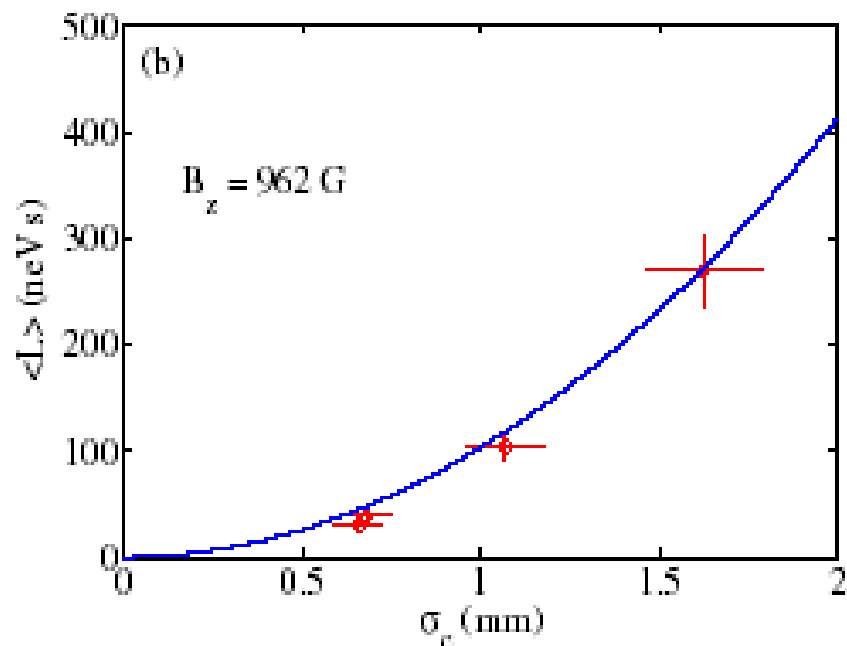
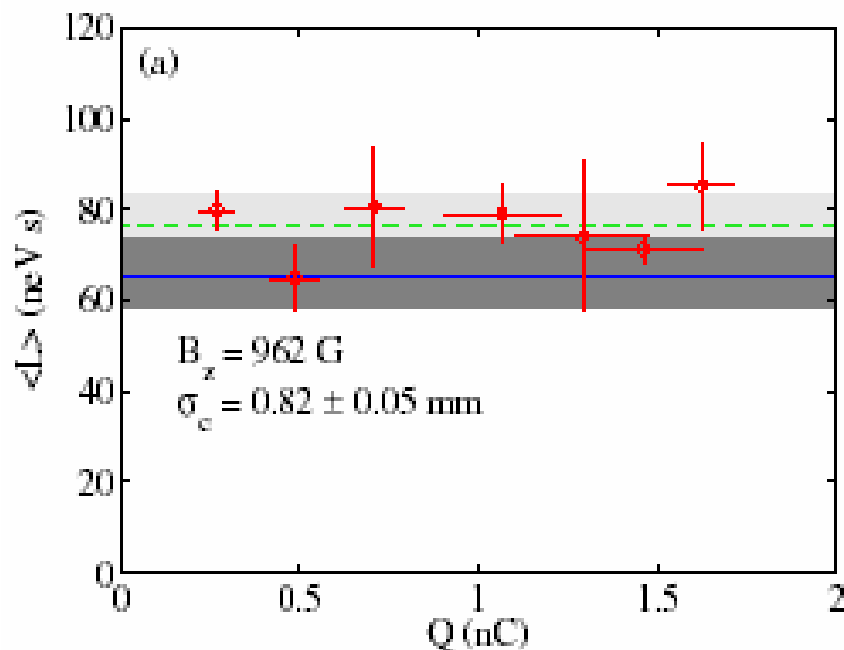
[Y.E. Sun et al. PRSTAB (2005)]





# Scaling of angular momentum (2)

- Other scaling law and MAM conservation rules were verified

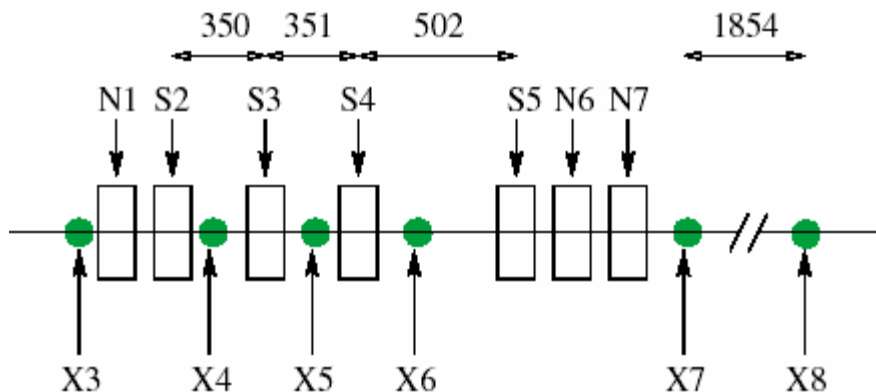


[Y.E. Sun et al. PRSTAB (2005)]

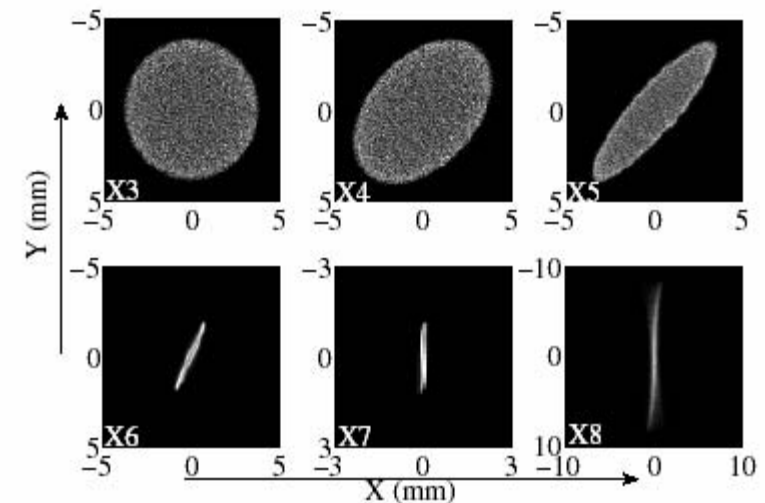
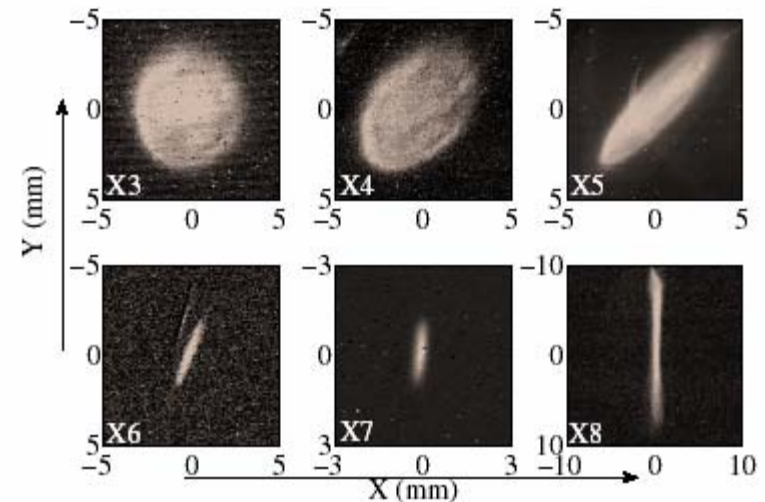


# Removal of angular momentum: flat beam generation

- From angular momentum measurement and beam size one can compute the correlation matrix  $\langle XY \rangle$
- The skew quadrupole settings can be computed to apply the proper torque



[Y.E. Sun et al. PRSTAB (2005)]



# Demonstration of emittance ratio of 100 (1)

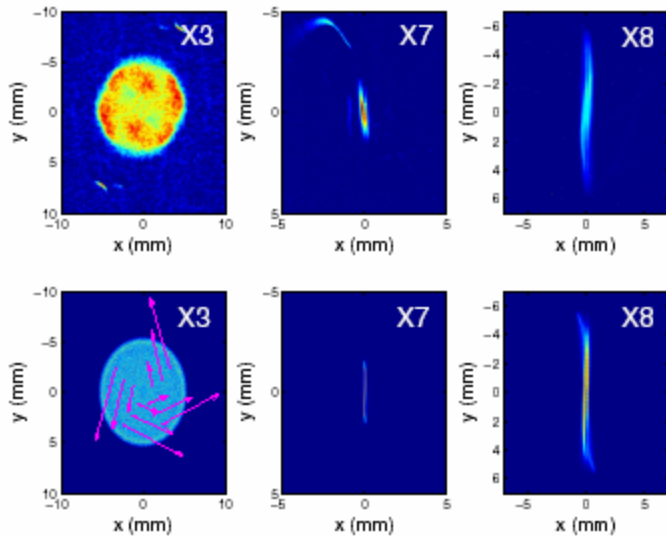
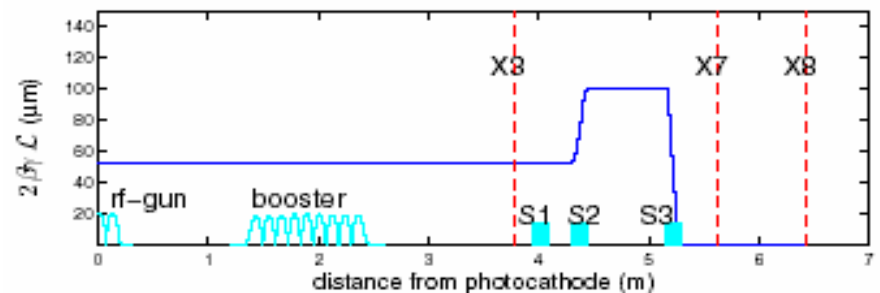
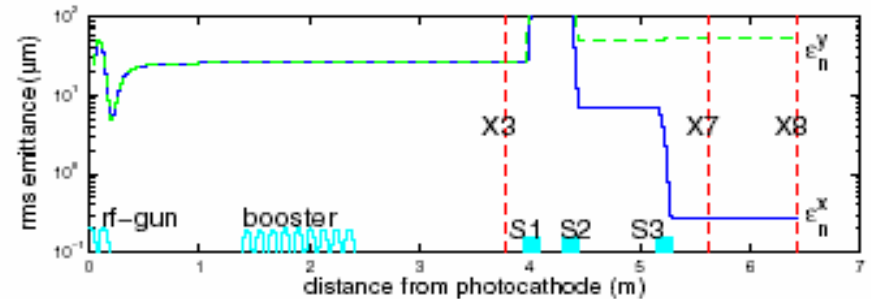
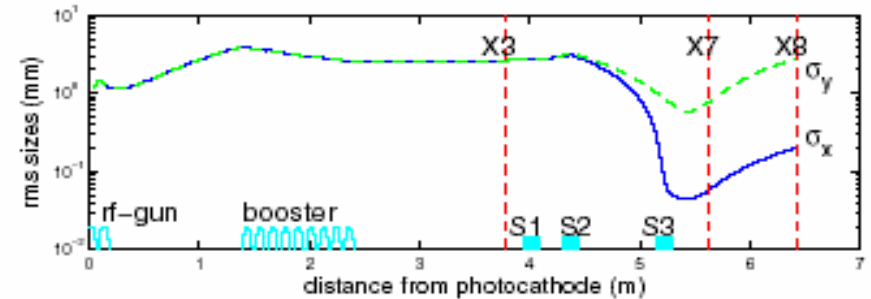


TABLE III. Measured and simulated flat-beam parameters for  $\sigma_c = 0.97$  mm. Both systematic and statistical (in brackets) error bars are included.

Parameter	Experiment	Simulation	Unit
$\sigma_x^{X7}$	$0.088 \pm 0.01$ ( $\pm 0.01$ )	0.058	mm
$\sigma_y^{X7}$	$0.63 \pm 0.01$ ( $\pm 0.01$ )	0.77	mm
$\sigma_x^{X8, v}$	$0.12 \pm 0.01$ ( $\pm 0.01$ )	0.11	mm
$\sigma_y^{X8, h}$	$1.68 \pm 0.09$ ( $\pm 0.01$ )	1.50	mm
$\epsilon_n^x$	$0.41 \pm 0.06$ ( $\pm 0.02$ )	0.27	$\mu\text{m}$
$\epsilon_n^y$	$41.1 \pm 2.5$ ( $\pm 0.54$ )	53	$\mu\text{m}$
$\epsilon_n^y / \epsilon_n^x$	$100.2 \pm 20.2$ ( $\pm 5.2$ )	196	

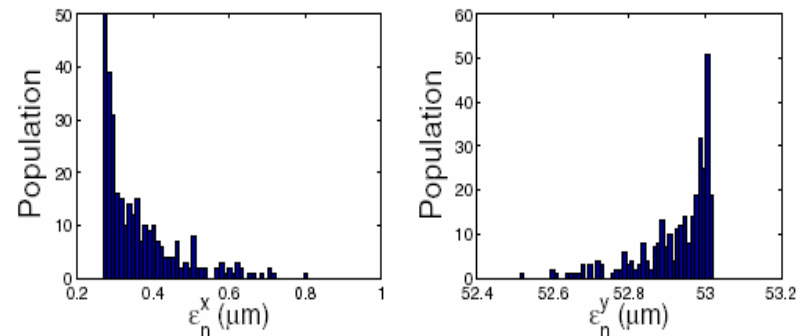
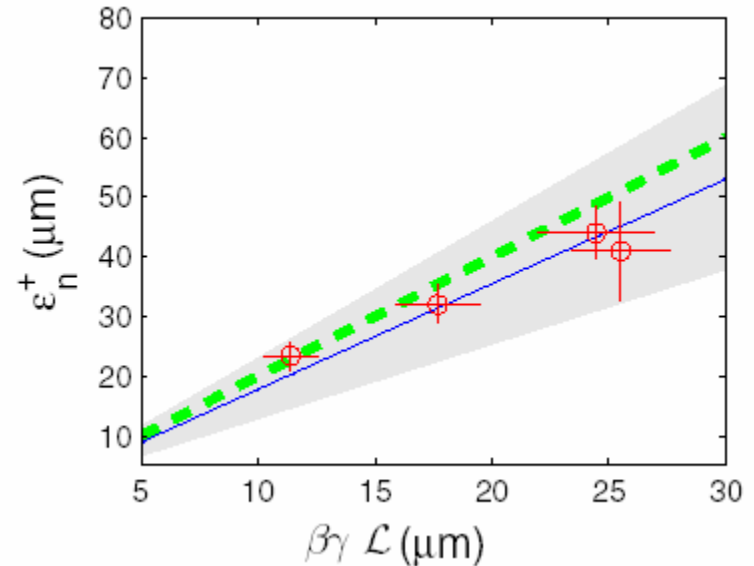
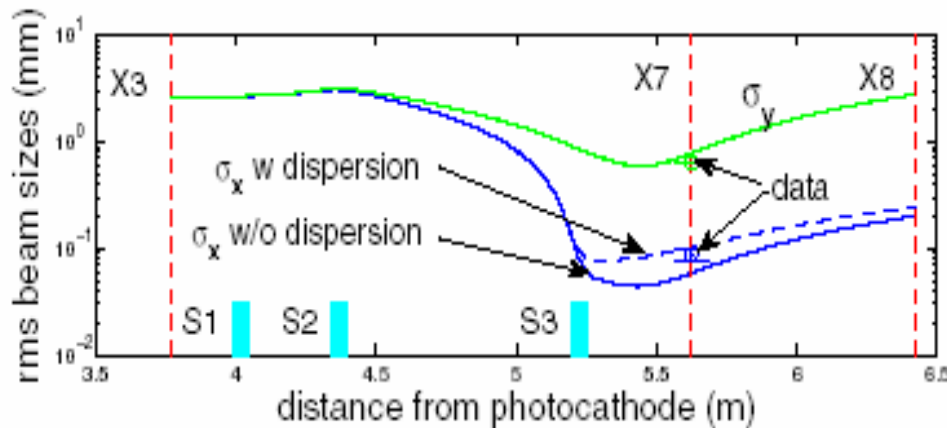


[P. Piot et al. PRSTAB (2006)]



# Demonstration of emittance ratio of 100 (2)

- Linear scaling of larger emittance on angular momentum was verified
- Discrepancy between simulation & experiment attributed to emittance measurement.



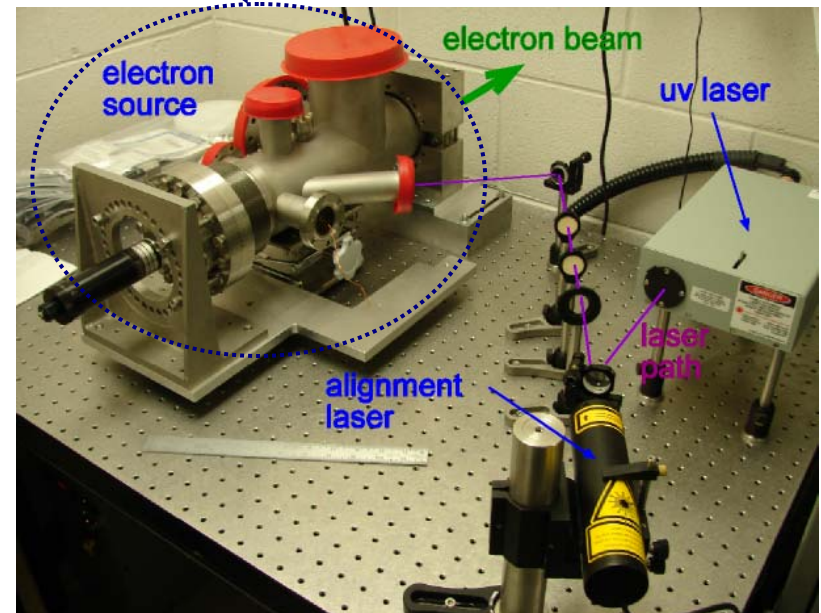
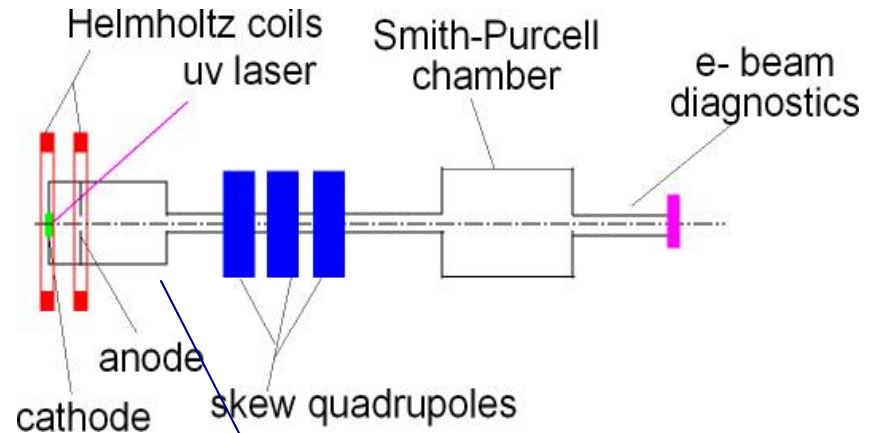
[P. Piot et al. PRSTAB (2006)]



# Applications: low energy Smith-Purcell free-electron laser

- A low energy electron source for time resolved electron microscopy was developed at NIU
- With minor upgrade (Helmoltz coils and skew quadrupoles), the source could generate sheet electron beam with suitable parameters to drive a low energy Smith-Purcell FEL (proposed in the late 80's by Walsh) Typical average power of 1 W is expected
- This could result in a table-top Terahertz light source with advantage compared to laser –based source making use of optical rectification

*[N. Vinogradov et al. PAC 2007]*



# Emittance exchange between one transverse and the longitudinal d.o.f

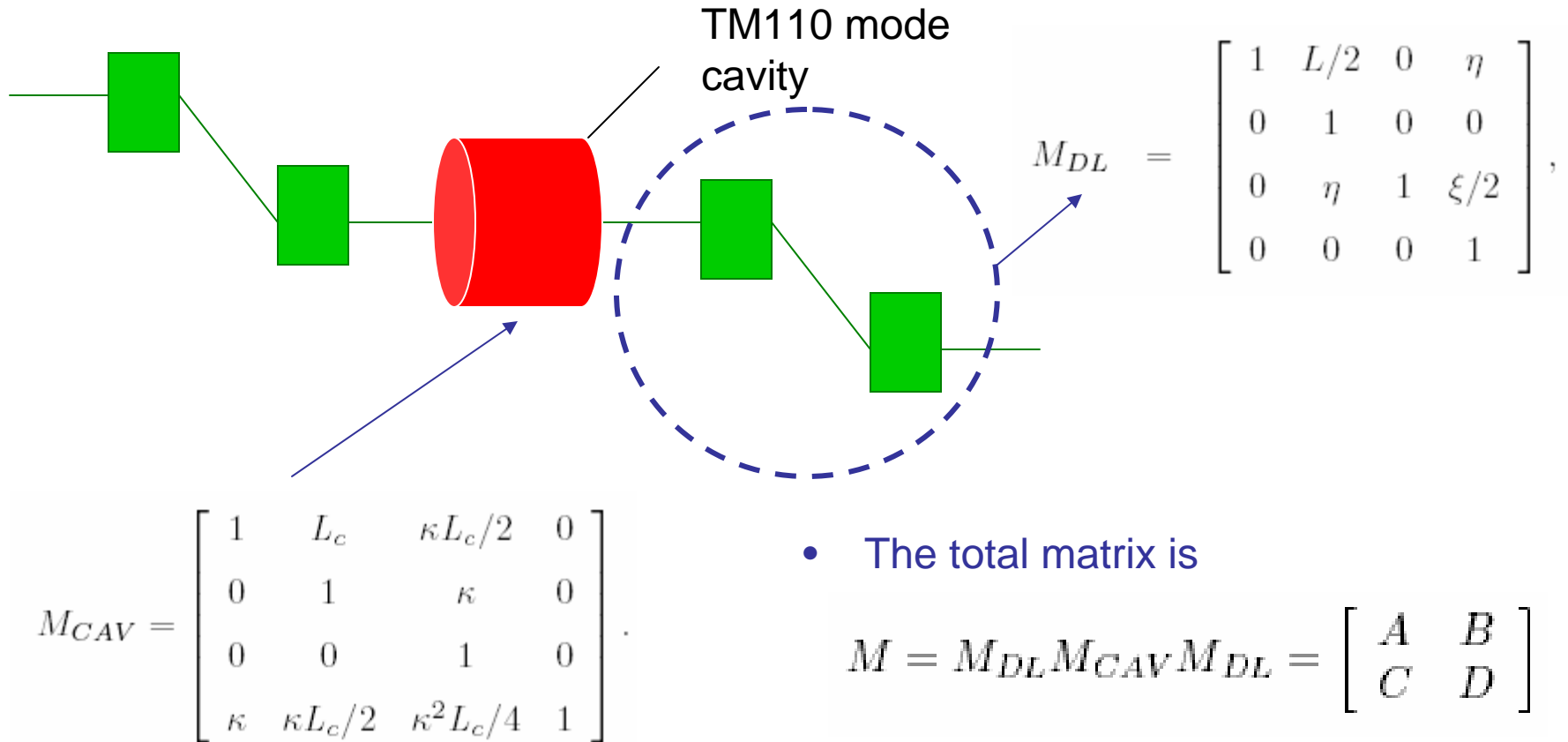
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- Basic idea suggested in the early days [Robinson]
- Proposed by Cornacchia and Emma (PRSTAB 2002) to increase the incoherent momentum spread in LCLS and thereby alleviate micro-bunching instabilities (due to CSR or LSC)
- When used with the round-to-flat beam transformation, can fully repartition emittances within the three degree-of-freedom and tailor the partition for specific applications
  - Greenfield FEL
  - MW power FEL ?
  - ILC (?)



# Emittance exchange principle

- Uses a deflecting mode cavity flanked by two dispersive sections (dogleg)





# Emittance exchange principle

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- When the condition  $\kappa = -1/\eta$  is satisfied

$$B = -\frac{1}{\eta} \begin{bmatrix} (L_c + 2L)/4 & (2\xi L - 8\eta^2 + \xi L_c)/8 \\ 1 & \xi/2 \end{bmatrix} = C$$

$$A_{1,2} = \frac{L_c}{4}$$

$$D = \frac{L_c}{4\eta^2} \begin{bmatrix} \xi/2 & \xi^2/4 \\ 1 & \xi/2 \end{bmatrix}$$

- For  $L_c=0$ , the total matrix is block diagonal And  $\varepsilon_x$  and  $\varepsilon_z$  are exchanged.
- Generally however we have (See Emma and Cornacchia PRSTAB)

$$\begin{bmatrix} \varepsilon_x^2 \\ \varepsilon_z^2 \end{bmatrix} = \begin{bmatrix} |A|^2 & |B|^2 \\ |C|^2 & |D|^2 \end{bmatrix} \begin{bmatrix} \varepsilon_{x,0}^2 \\ \varepsilon_{z,0}^2 \end{bmatrix} + \lambda^2 \varepsilon_{x,0} \varepsilon_{z,0} I,$$



# Emittance exchange principle

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- In our case the coupling term is given by

$$\lambda^2 = \frac{L_c^2(1 + \alpha_x^2)(\xi^2 + (\xi\alpha_z - 2\beta)^2)}{64\eta^2\beta_x\beta_z}.$$

- And can be minimized by a proper choice of incoming longitudinal Twiss parameters
- A possible choice for the optimum chirp ( $\alpha_z = -\frac{\langle z\delta \rangle}{\varepsilon_z}$ ) is

$$\alpha_{z,m} = \frac{2\beta_z}{\xi}$$

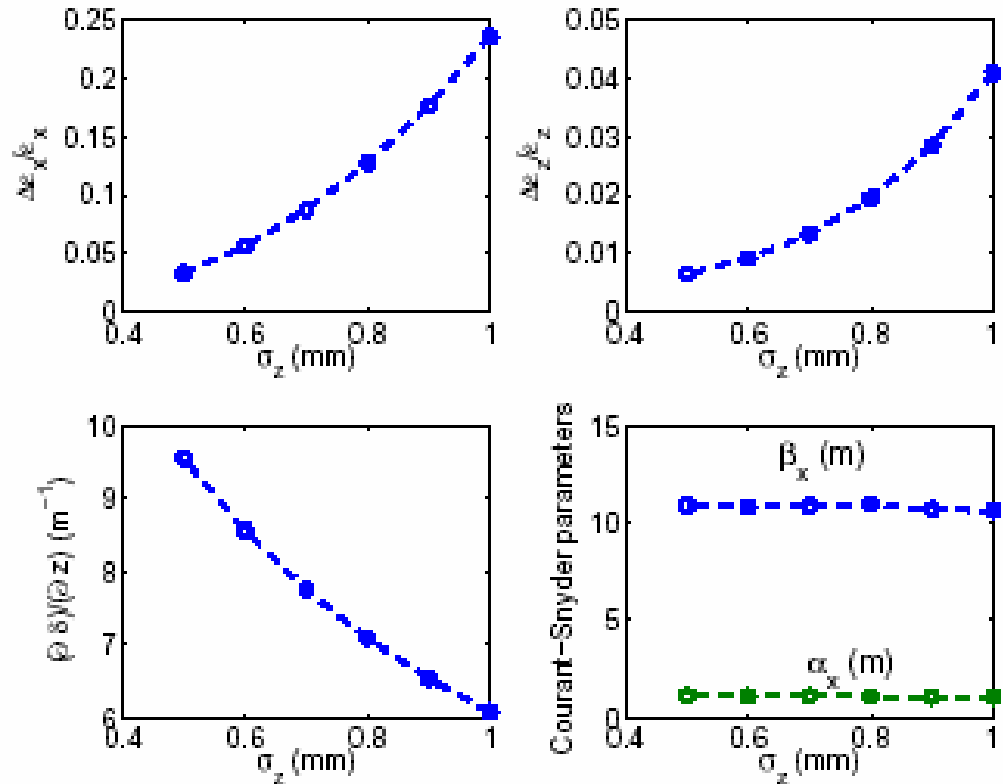
- And the residual coupling term is

$$\lambda_m^2 = \frac{1}{64} \frac{\xi^2 L_c^2 (1 + \alpha_x^2)}{\beta_x \eta^2 \beta_z} = \frac{1}{64} \frac{\xi^2 L_c^2}{\eta^2} \frac{\varepsilon_{z,0}}{\varepsilon_{x,0}} \left( \frac{\sigma_{x'}}{\sigma_z} \right)^2$$



# Optimizing the emittance exchange

- The scheme was tested with particle tracking
- The exchange aims at swapping  $\varepsilon_x$  and  $\varepsilon_z$
- Here initial emittance values are  $\varepsilon_x = 3 \mu\text{m}$ , and  $\varepsilon_z = 10 \mu\text{m}$ .



# Applications: Greenfield FEL

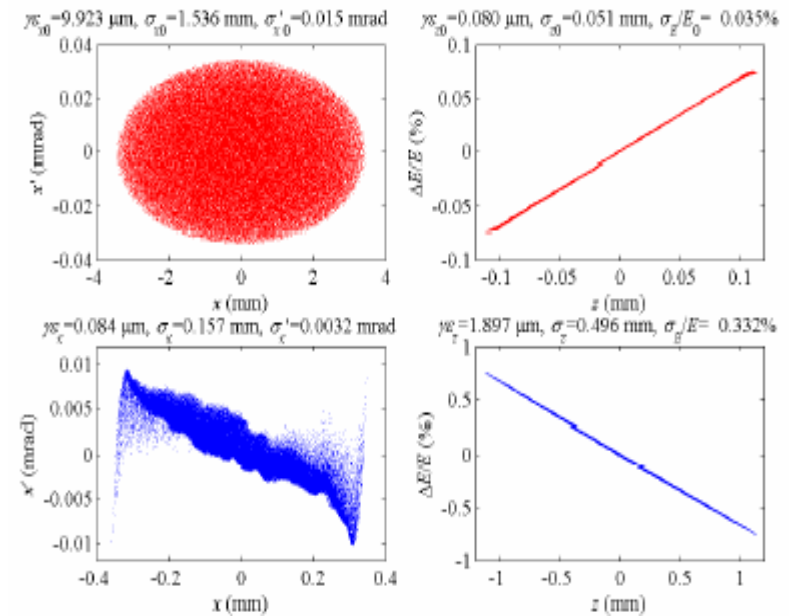
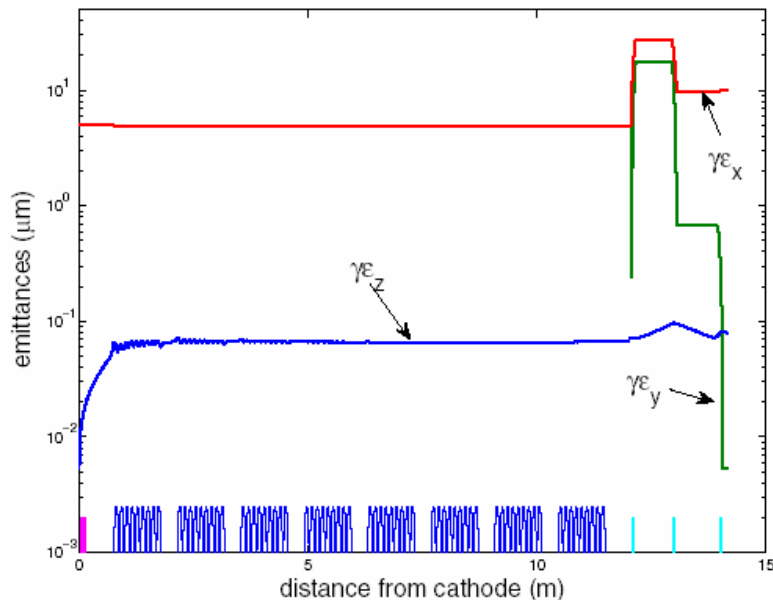
- Greenfield FEL ( $\lambda=1$  A) require tranverse emittance of 0.1 mm
- This can be achieved with an the two transformations discussed

- Flat beam

$$\gamma\epsilon_x \otimes \gamma\epsilon_y : (10^{-6})^2 \rightarrow 10^{-5} \otimes 10^{-7}$$

- $\epsilon_x$ - $\epsilon_z$  exchange

$$\gamma\epsilon_x \otimes \gamma\epsilon_y \otimes \gamma\epsilon_z : (10^{-6}, 10^{-6}, 10^{-7}) \rightarrow (10^{-5}, 10^{-7}, 10^{-7}) \rightarrow (10^{-7}, 10^{-7}, 10^{-5})$$

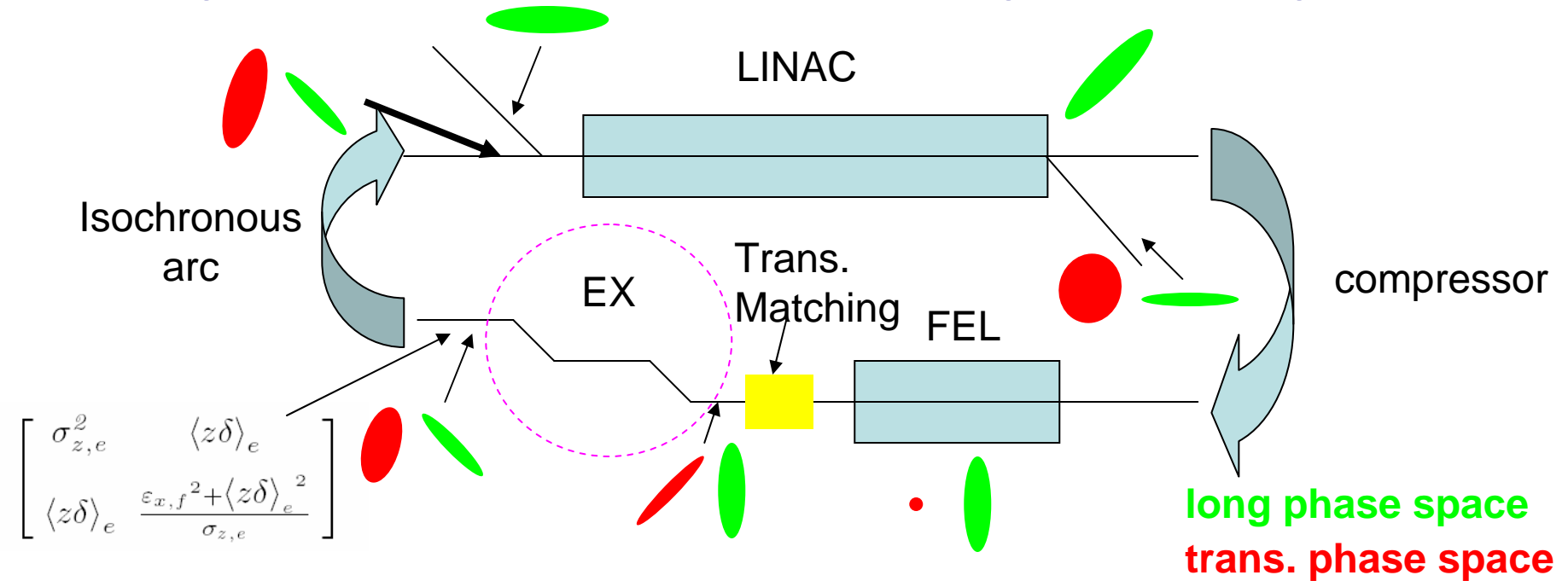


[Emma, Huan Kim and Piot. PRSTAB (2006)]



# Applications: MW ERL (1)

- Might have application in ERL to enable higher final energy spread



- After the FEL, the transverse beam parameters are matched such that they provide the desired bunch length and correlated energy spread after the emittance exchanger
- The beam is then decelerated



# Applications: MW ERL (2)

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- The final transverse matrix is

$$\begin{bmatrix} \frac{1}{4} \frac{\varepsilon_{z,f} (\beta_{z,f}^2 L^2 + \eta^4)}{\beta_{z,f} \eta^2} & \frac{1}{2} \frac{\varepsilon_{z,f} (\beta_{z,f}^2 L^2 - \eta^4)}{\beta_{z,f} \eta^2 L} \\ \frac{1}{2} \frac{\varepsilon_{z,f} (\beta_{z,f}^2 L^2 - \eta^4)}{\beta_{z,f} \eta^2 L} & \frac{\varepsilon_{z,f} (\beta_{z,f}^2 L^2 + \eta^4)}{\beta_{z,f} \eta^2 L^2} \end{bmatrix}$$

- Issues:
  - After the exchanger transverse emittance is huge and so is the transverse beta function (but this can be controlled)
  - No clear advantage compared to usual longitudinal phase space manipulation (at least not obvious from this first look)
  - Real question is does one prefer a large longitudinal or transverse emittance?
  - One advantages might be BBU mitigation?



# ILC revisited (work in progress)

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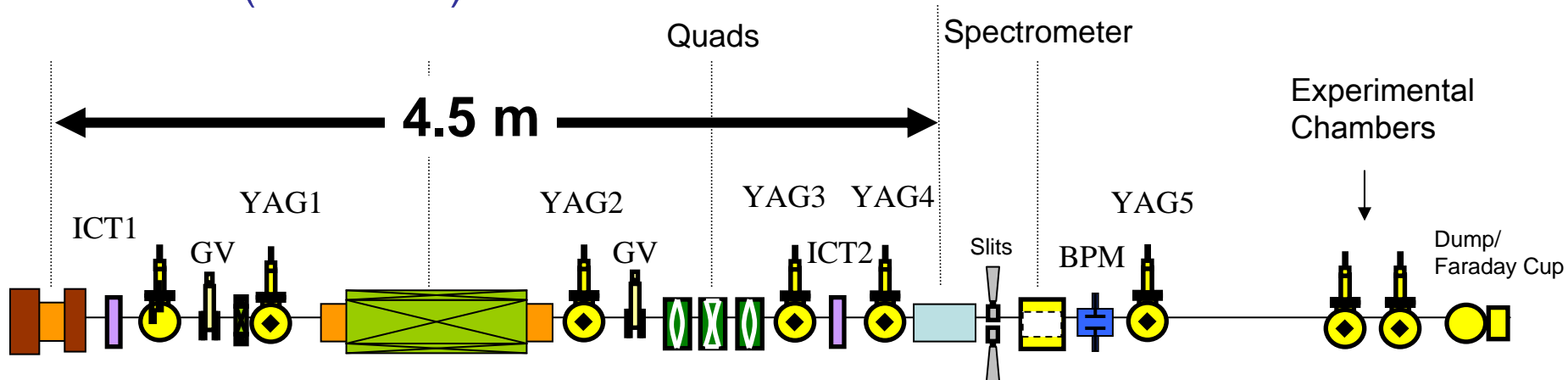
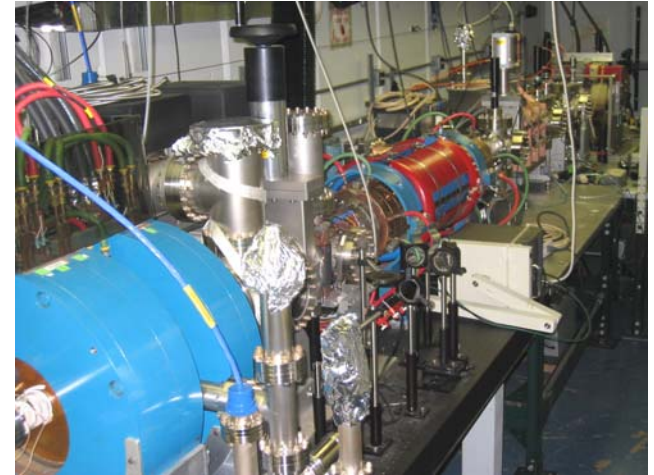
- Flat beam (see before) seems not able to provide the proper emittance values for ILC  $(\varepsilon_x, \varepsilon_z) \rightarrow (0.02, 8) \mu\text{m}$
- ILC target  $(0.02 \times 8)^{1/2} \sim 0.4 \mu\text{m}$  for 3.2 nC is not reachable a conventional electron source
- These bunches are produced by a 5 GeV, 6 km damping ring  
Considering the 6-D emittance after the damping ring we have  $(\varepsilon_x, \varepsilon_y, \varepsilon_z) = (8, 0.02, 3000) \mu\text{m}$
- A possibility:  $(5, 5, 8) \rightarrow (1250, 0.02, 8) \rightarrow (8, 0.02, 1250) \mu\text{m}$
- The problem is to produce the “low” initial **longitudinal emittance** (self generating scheme are hopeless with GaAs cathode)





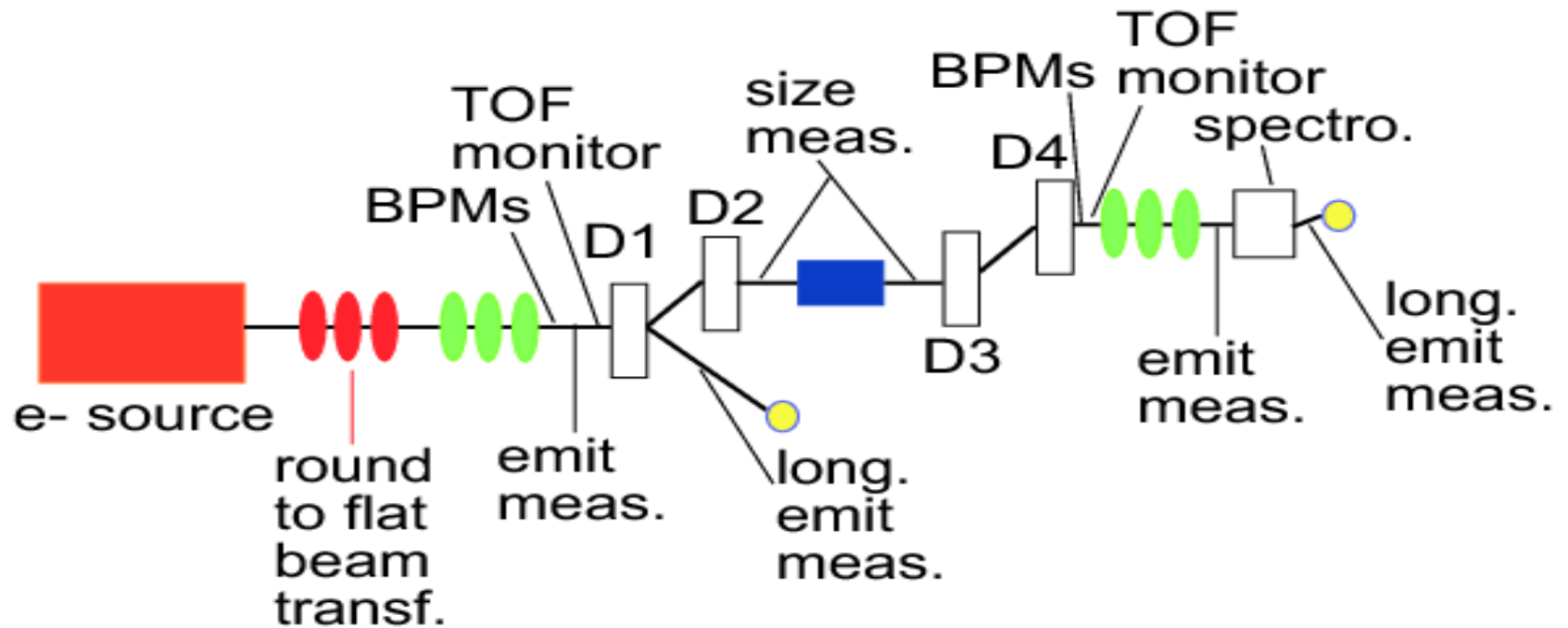
# Plans for POF experiment at AWA (1)

- Argonne wakefield accelerator
  - 15 MeV maximum energy
  - Few pC to 100 nC bunches
  - Many diagnostics
- Managed/Operated by Wei Gai and John Power (HEP/ANL)



# Plans for POF experiment at AWA (2)

- Emittance exchange include extensive diagnostics currently being developed
- We included both the flat beam transform and transverse-to-longitudinal exchanger

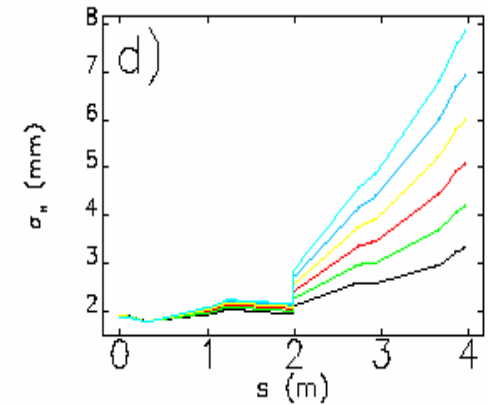
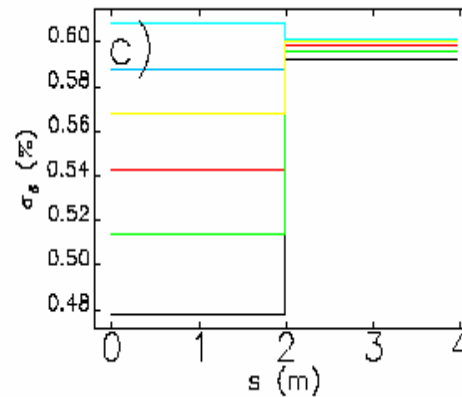
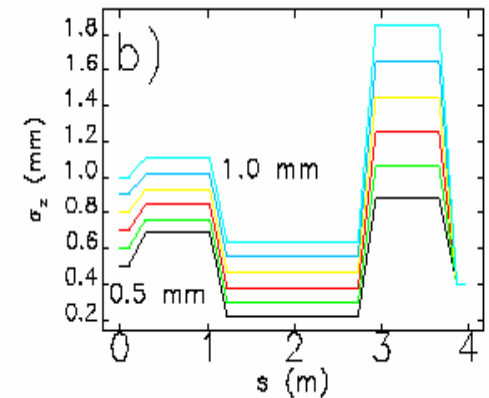
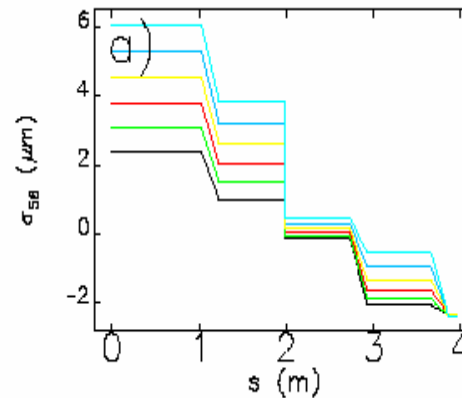


# Second order effects problems...

- Bunch length at AWA larger than cases studied in literature
- Second order effects spoil the final emittance

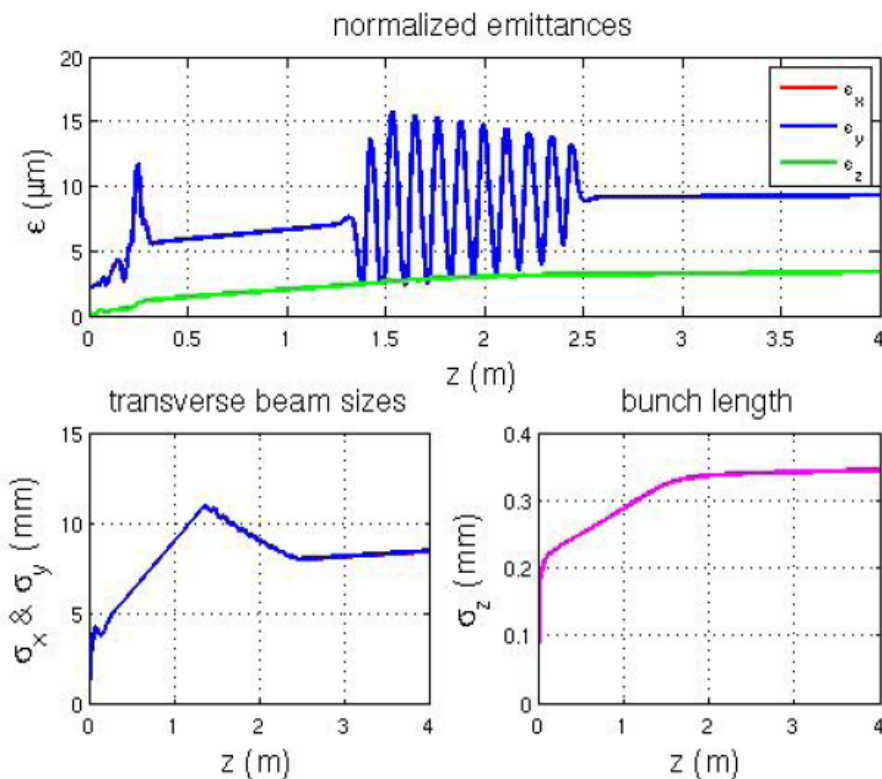
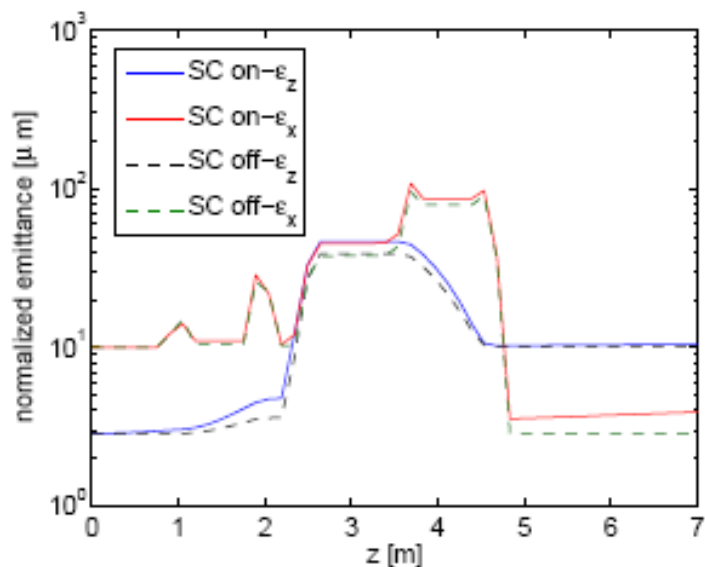
$$\varepsilon_x \simeq \left| M \Sigma_0 \widetilde{M} + \sum_j \begin{bmatrix} T_{1jj} \\ T_{2jj} \end{bmatrix} [T_{1jj}, T_{2jj}] \langle x_j^4 \rangle \right|^{1/2}$$

- Photocathode drive laser will need to be shortened



# Start-to-end simulation of the POP at AWA

- Round beam simulation  
(M. Rihaoui, NIU)
- Simulation of exchanger including space charge  
(Yin-e Sun et al., PAC 07)



- Flat beam optimization

$(17, 17, 5) \rightarrow (34, 0.2, 5)$  with a ratio  $\bar{e}_x/\bar{e}_y = 210$ .



# Summary

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- Phase space tailoring are emerging techniques
- Flat beam generation has been demonstrated and is now implement in the standard design of ILCTA. It will open opportunities to test concept such as image-charge undulator and dielectric wakefield
- Emittance exchange between the transverse and longitudinal phase spaces together with the flat beam technique provides control of emittance partitioning within the three degree-of-freedoms.
- Possible application might include longitudinal phase space management in FEL-driver ERL's

