



Synchrotron Light Interferometer

Project at Jefferson Lab

Pavel Chevtsov

February 21, 2003



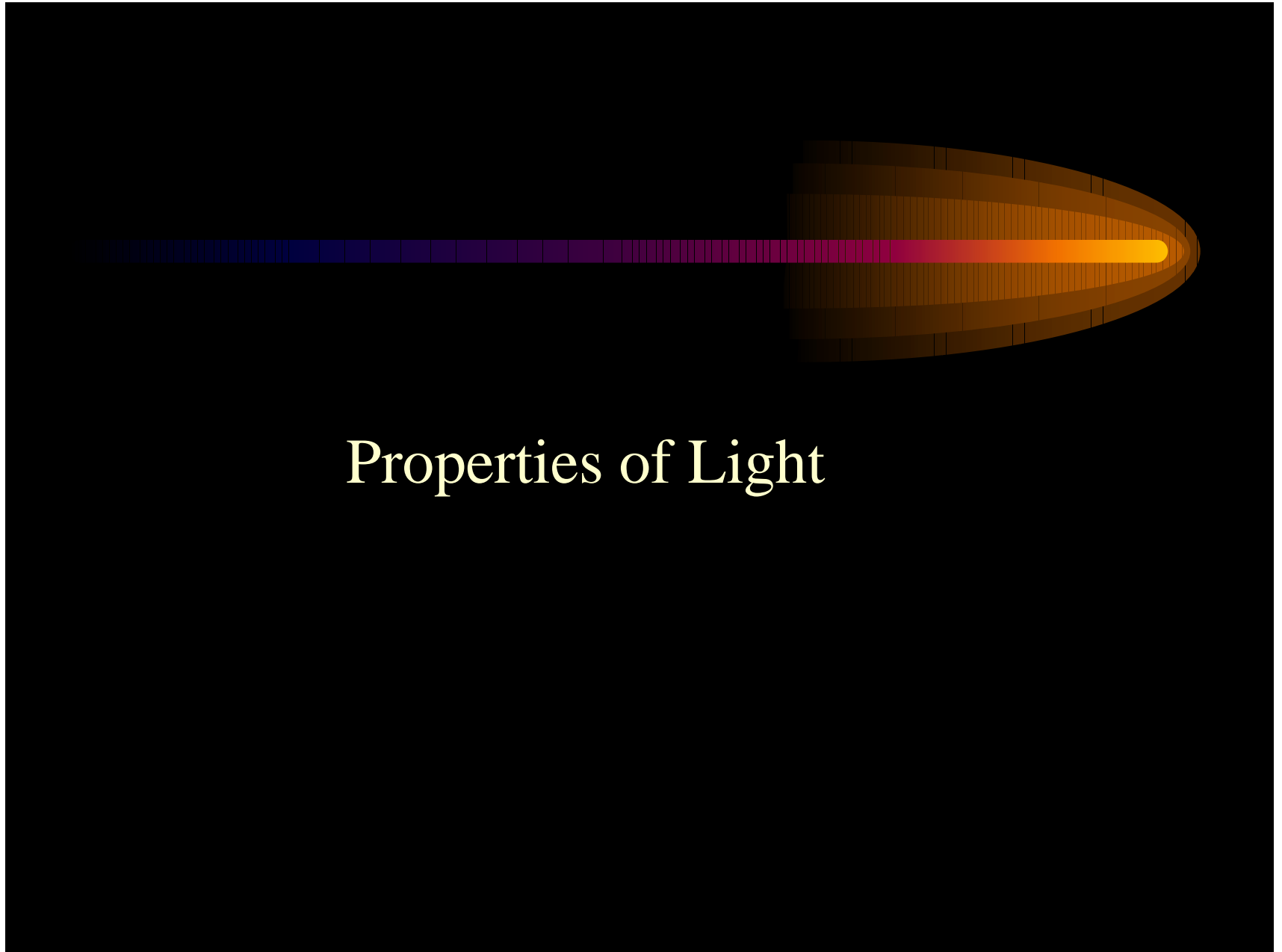
- Properties of Light

- Synchrotron Radiation

- Beam Diagnostics with Synchrotron Light

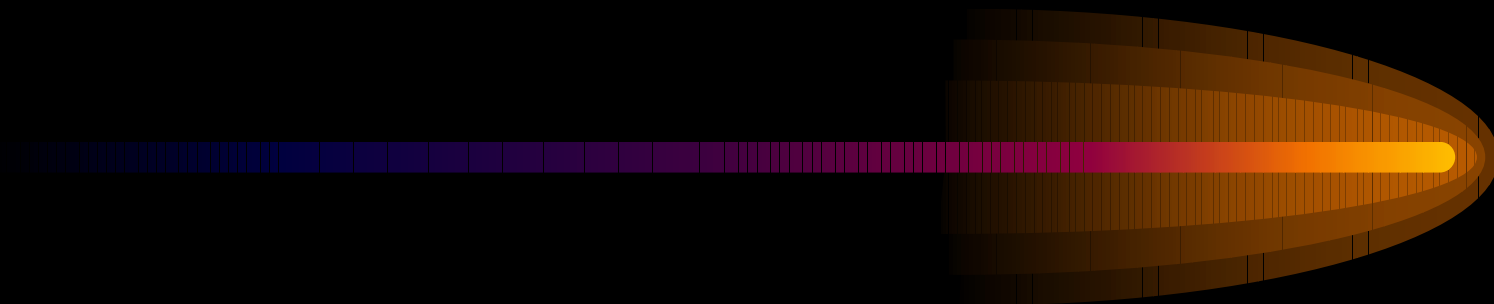
- Synchrotron Light Interferometer at Jefferson Lab
with some Experimental Results

- Conclusions

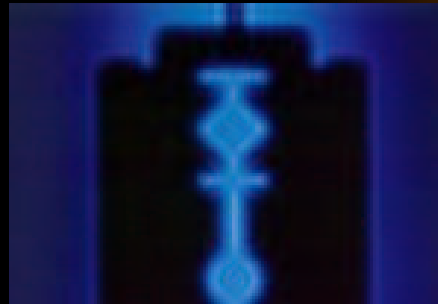


Properties of Light

Diffraction

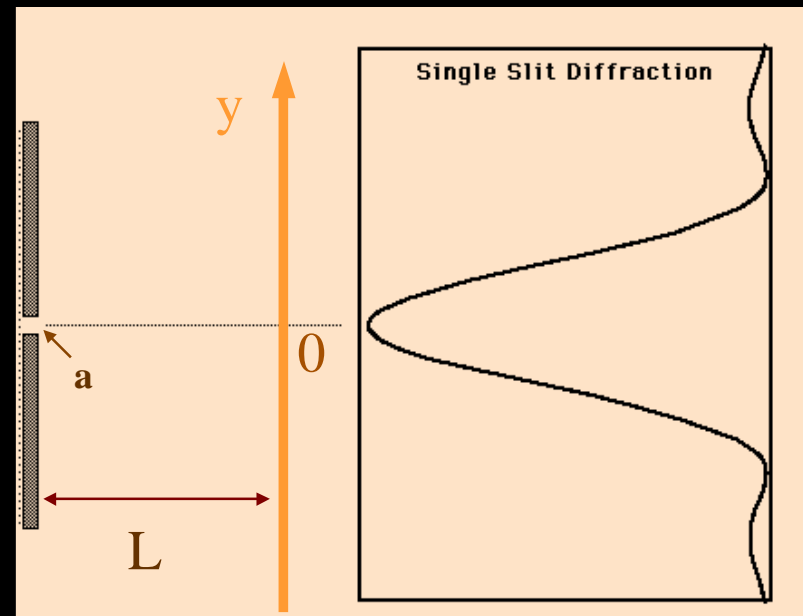


Diffraction is the spreading of waves around obstacles.



Diffraction describes how light
interacts with its physical environment.

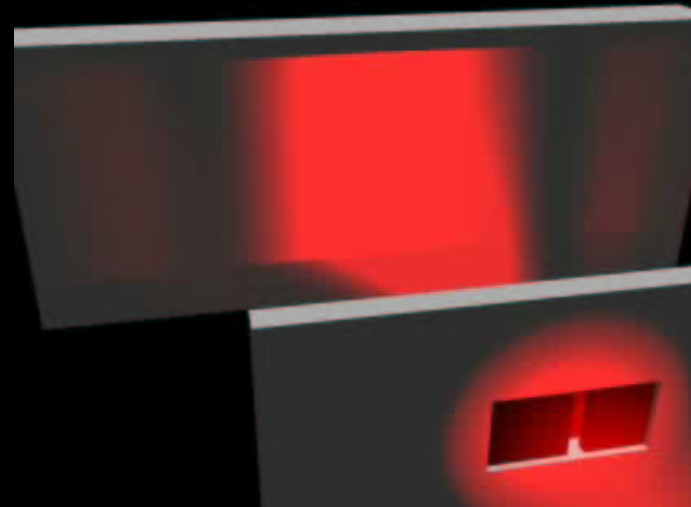
S



$$I(y) = I(0) \left[\frac{\sin(\alpha)}{\alpha} \right]^2$$

$$\alpha = k a y / (2L)$$

$$k = 2\pi / \lambda$$

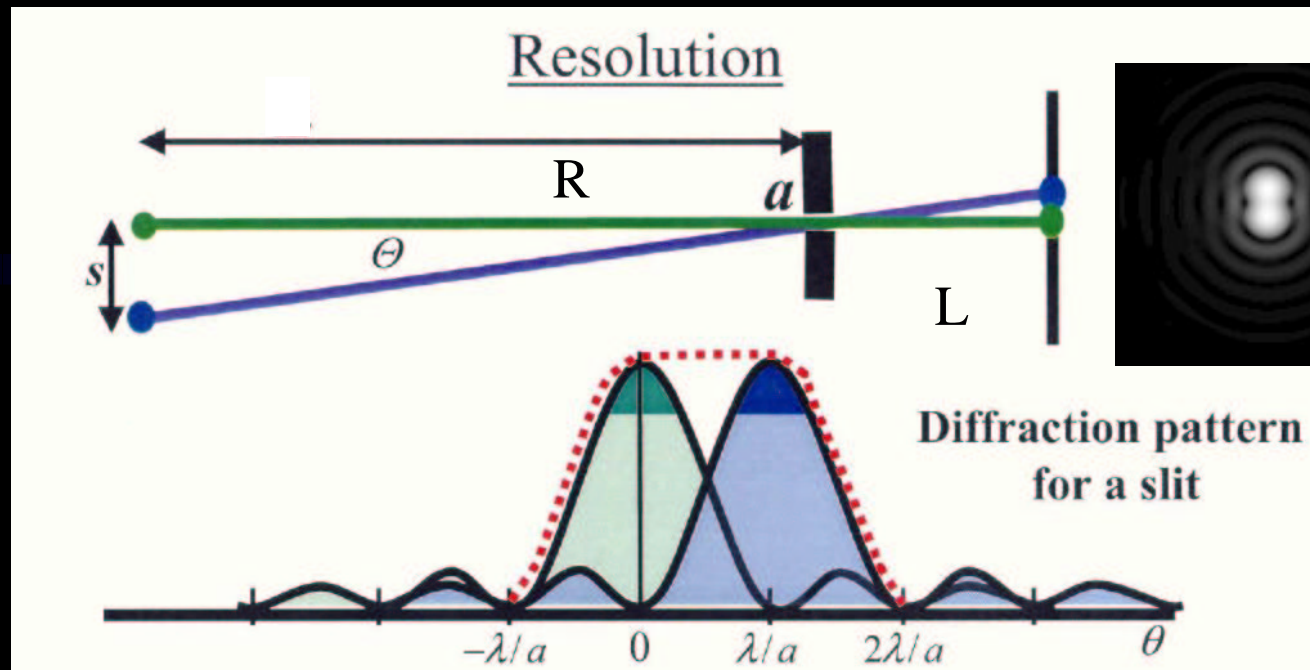


Resolving power of image-forming systems

Diffraction of light limits the resolution of optical systems.
The images of two objects, which are very close to each other, overlap.



How close two points can be brought together before they can no longer be distinguished as separate ?

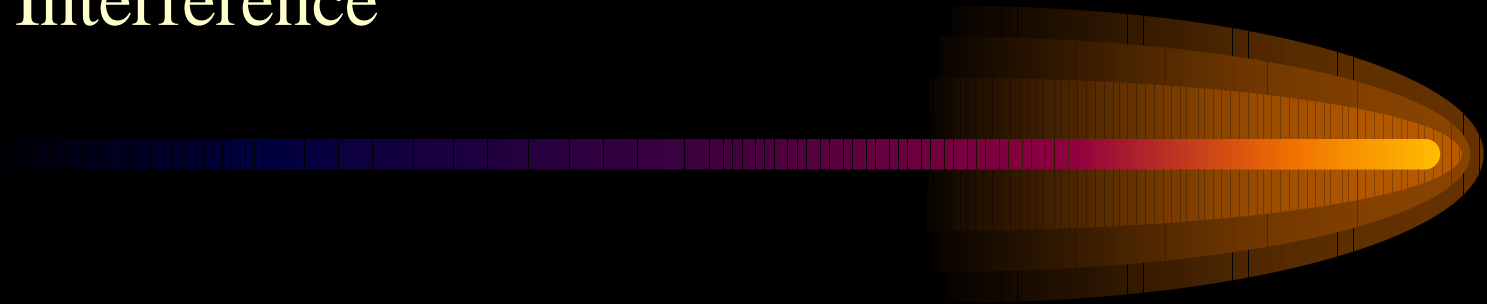


The **Rayleigh** criterion states that two similar diffraction patterns can just be resolved if the first zero of one pattern falls on the central peak of the other.



$$\left(\frac{s}{R}\right)_{\min} = \theta_{\min} = \frac{\lambda}{a}$$

Interference



Interference is the net effect of the combination of two or more wave trains.

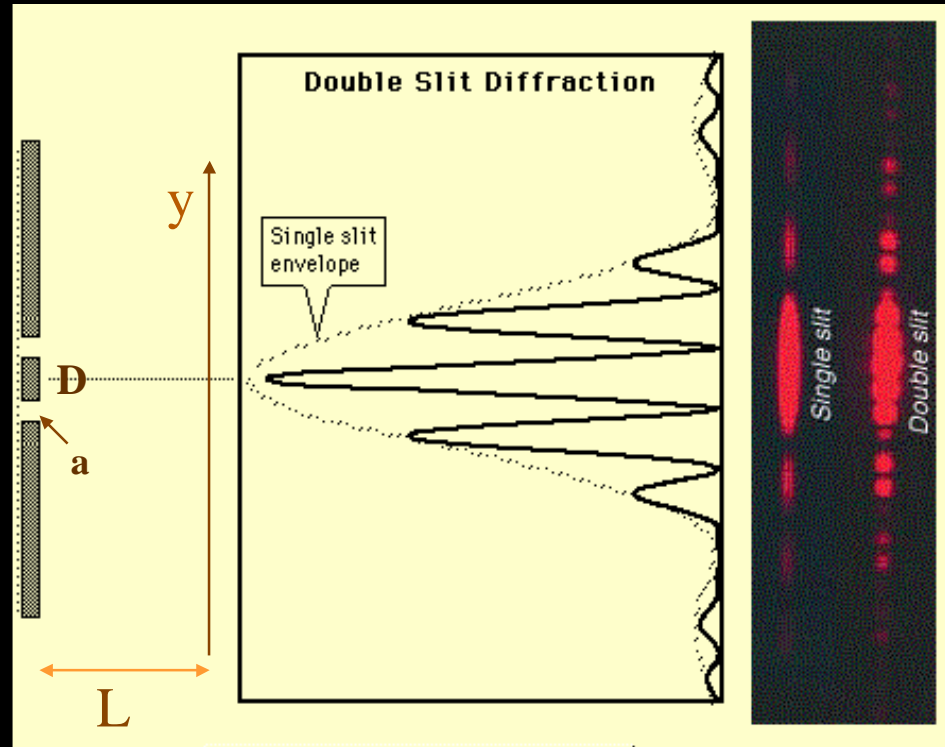


Interference results from the superposition of electromagnetic waves. It is the mechanism by which light interacts with light.



•

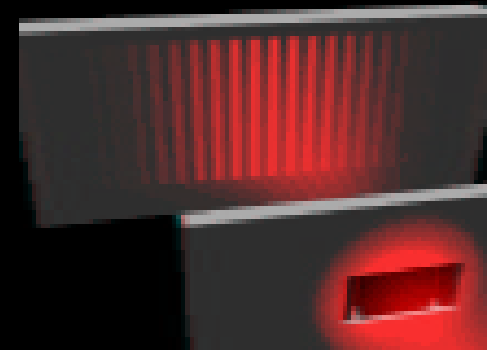
S



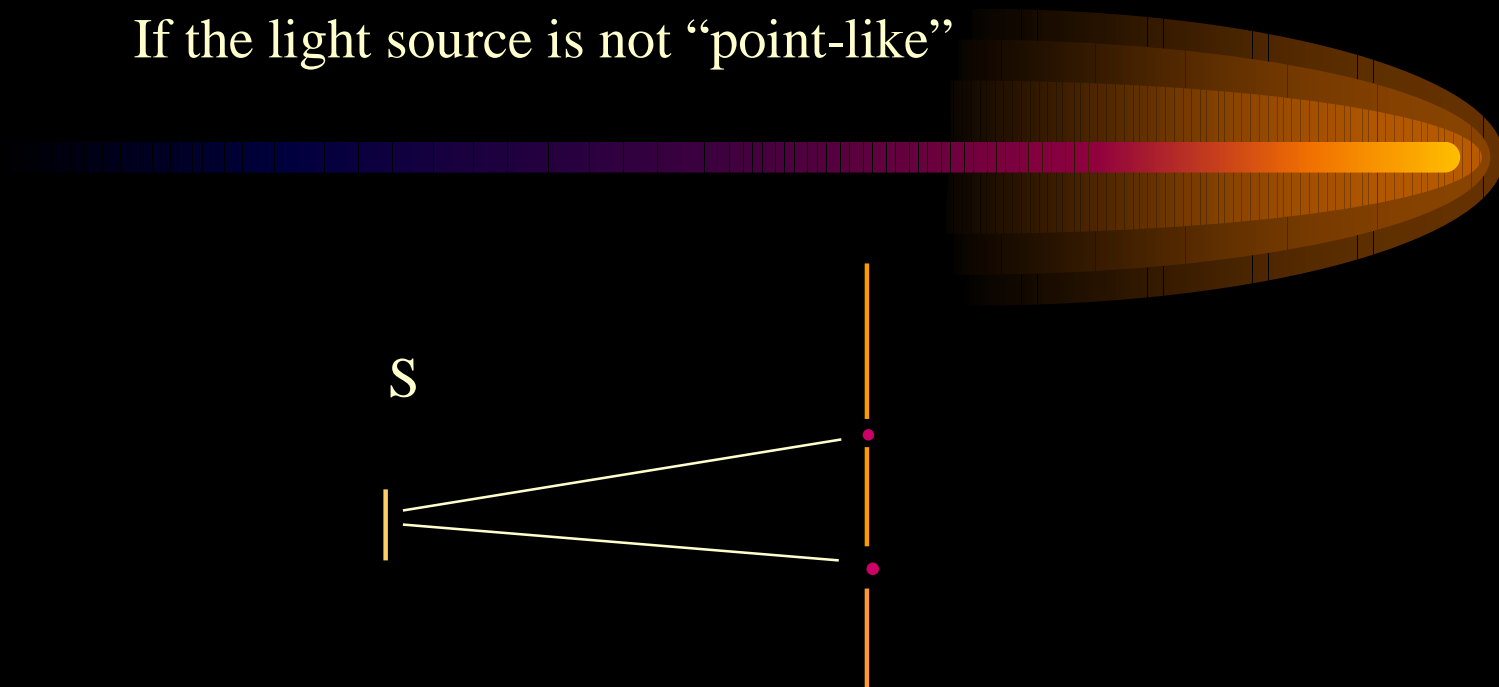
The intensity pattern is given by:

$$I(y) = I_0 \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + \cos(kDy/L)]$$

$$\alpha = kay/(2L)$$



If the light source is not “point-like”



$$I(y) = I_0 \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \phi)]$$

$$\alpha = kay/(2L)$$


$$V = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$$

visibility (fringe contrast)

And the visibility and the “phase shift” ϕ are connected with the degree of coherence Γ : $V = |\Gamma|$, $\phi = f(\arg \Gamma)$

Theorem of van Cittert – Zernike

The degree of coherence Γ is given by the Fourier transform of the intensity distribution of the source object.

$$\Gamma(\theta) = \int I(\xi) \exp\{-i 2\pi \theta \xi\} d\xi$$

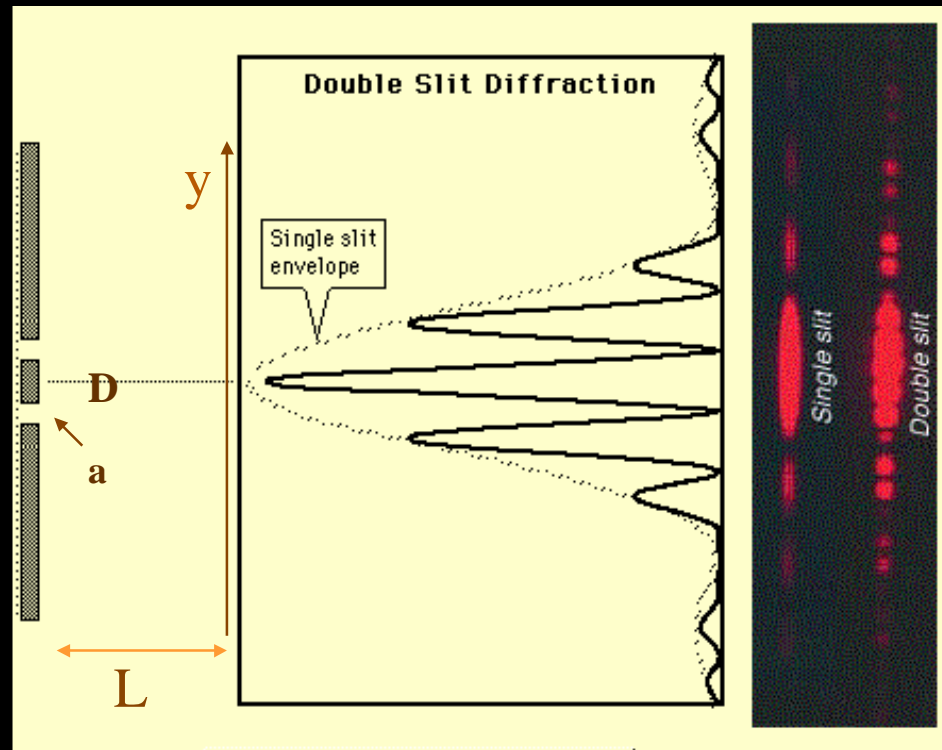
$$\Gamma = \frac{\Gamma(\theta)}{\Gamma(0)}$$

$$\theta = \frac{D}{\lambda R}$$



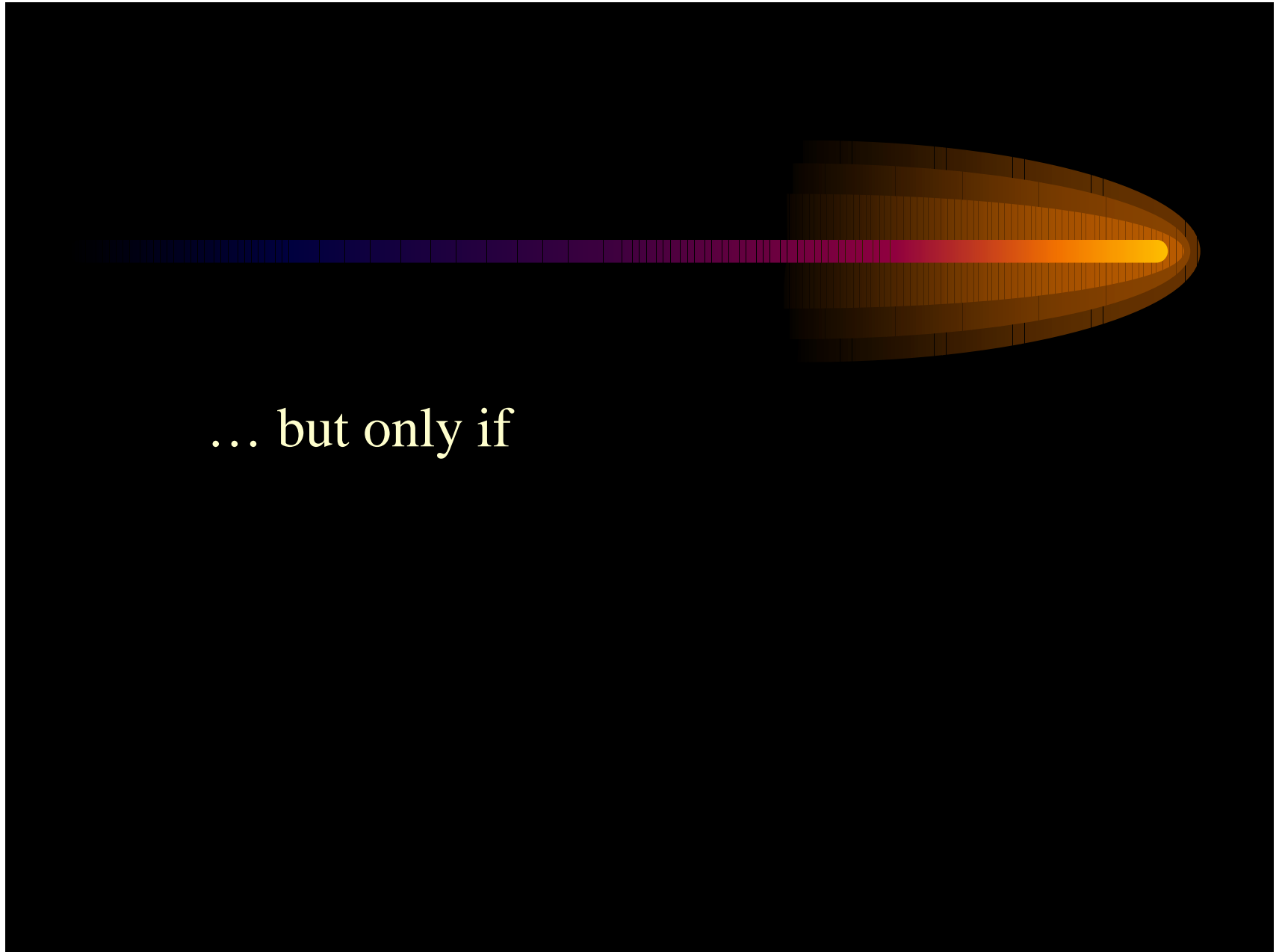
-
- the visibility of the interference fringe picture from a point source is equal to 1
 - a small source object gives a good visibility (fringe contrast)
 - a large source object gives a poor visibility (fringe contrast)

What is about the resolution of such a double slit assembly (interferometer) ?

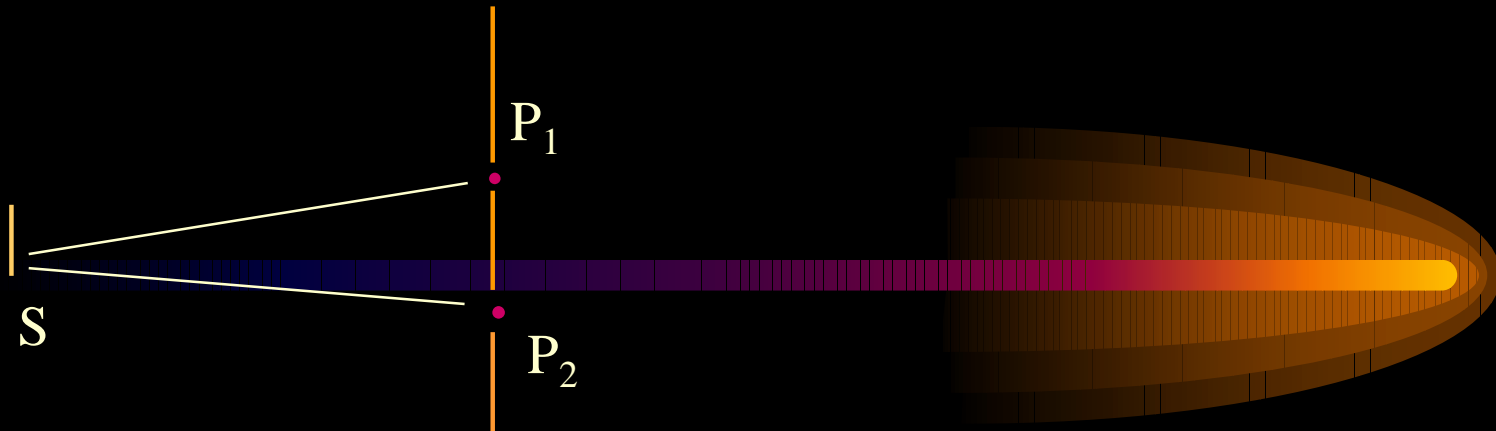


Following Rayleigh's criterion, $\left(\frac{s}{R}\right)_{\min} = \theta_{\min} = \frac{\lambda}{2D}$

The resolution can be made very high ...



... but only if



P_1 and P_2 remain correlated:

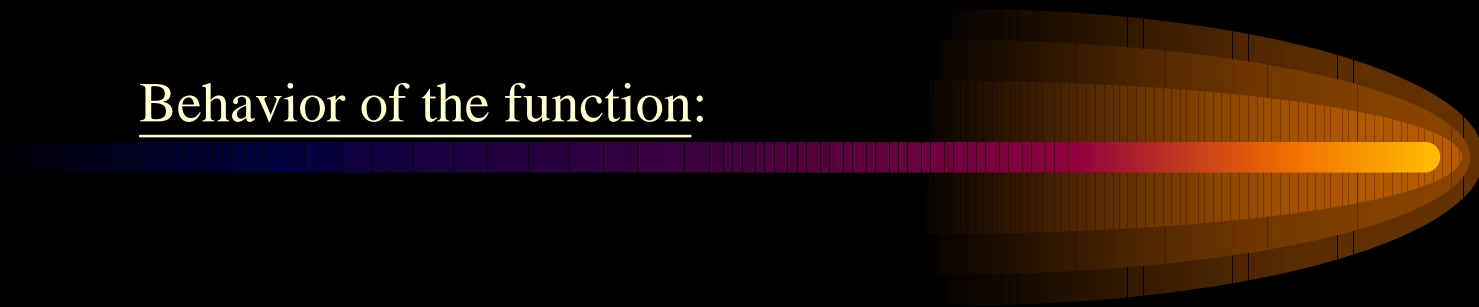
for all typical points S in the source

$$|SP_1 - SP_2| \ll \lambda_0^2 / \Delta\lambda$$

$\lambda_0^2 / \Delta\lambda$ is the coherence length for the
bandwidth $\Delta\lambda$



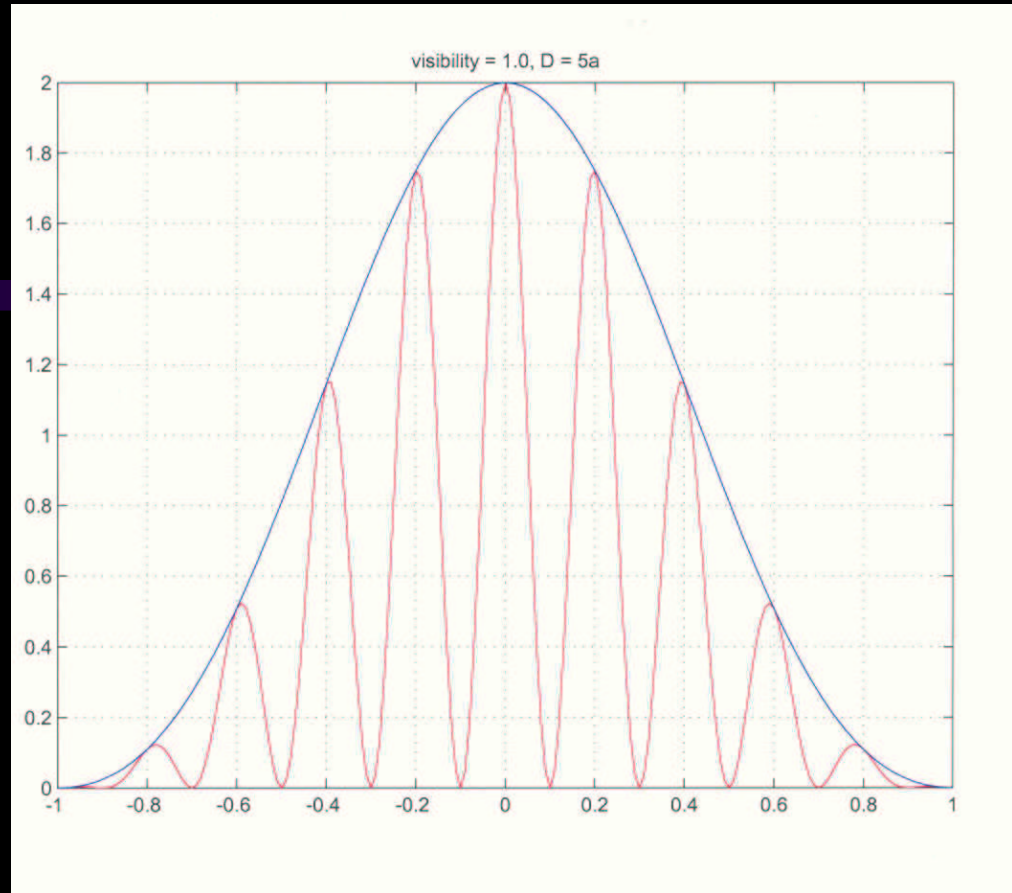
Behavior of the function:



$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \varphi)]$$

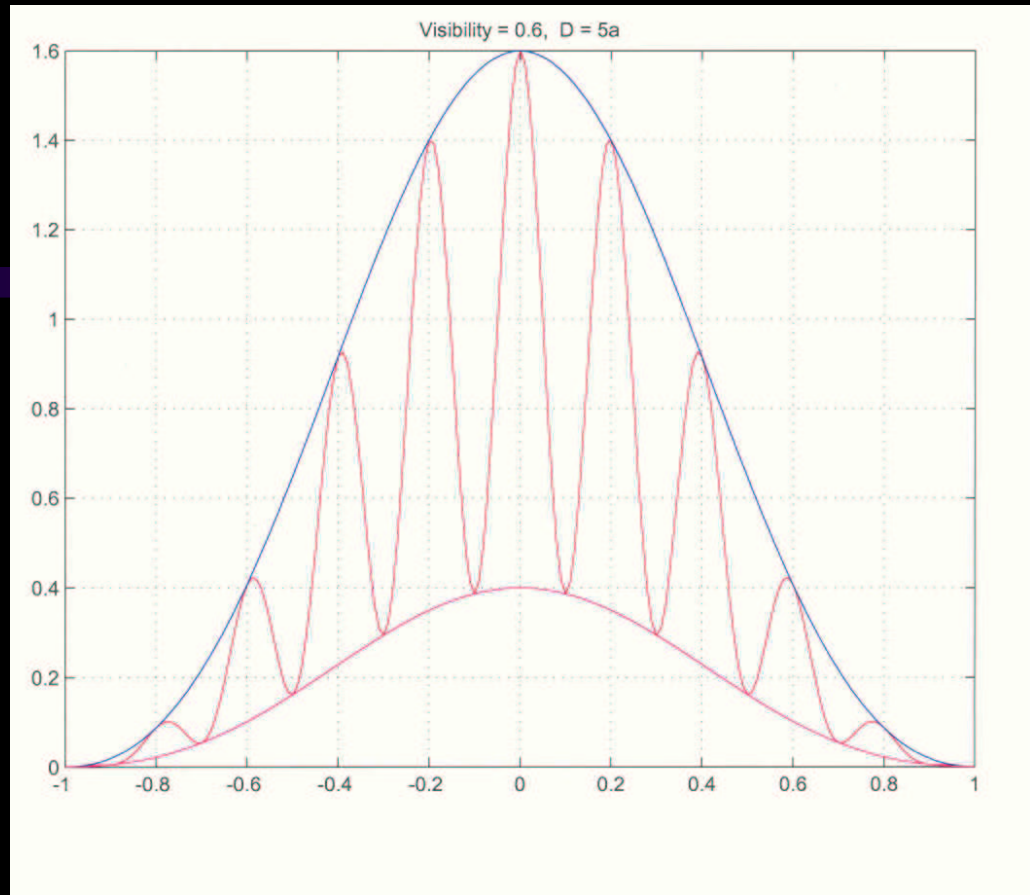
$$\alpha = kay/(2L)$$





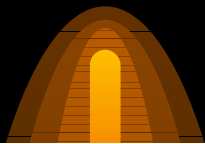
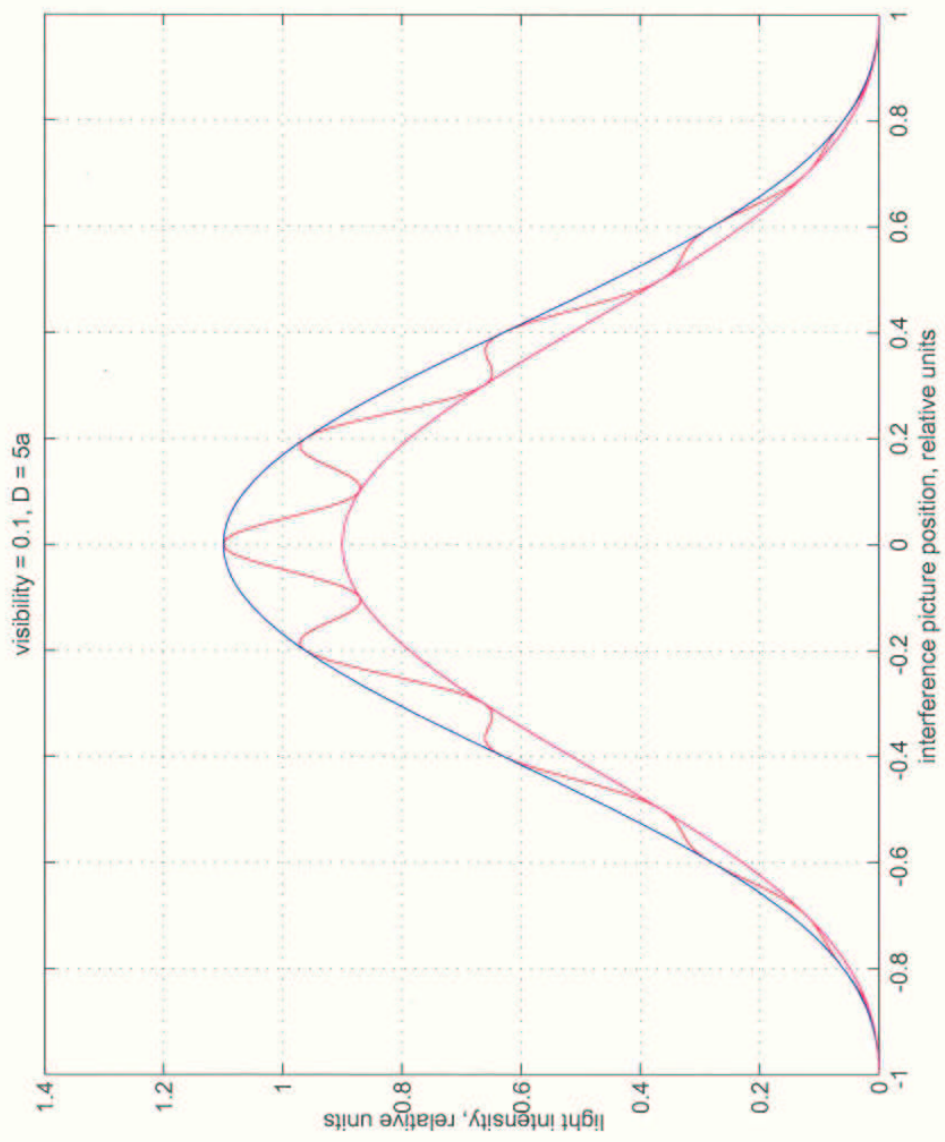
$$\alpha = kay/(2L)$$

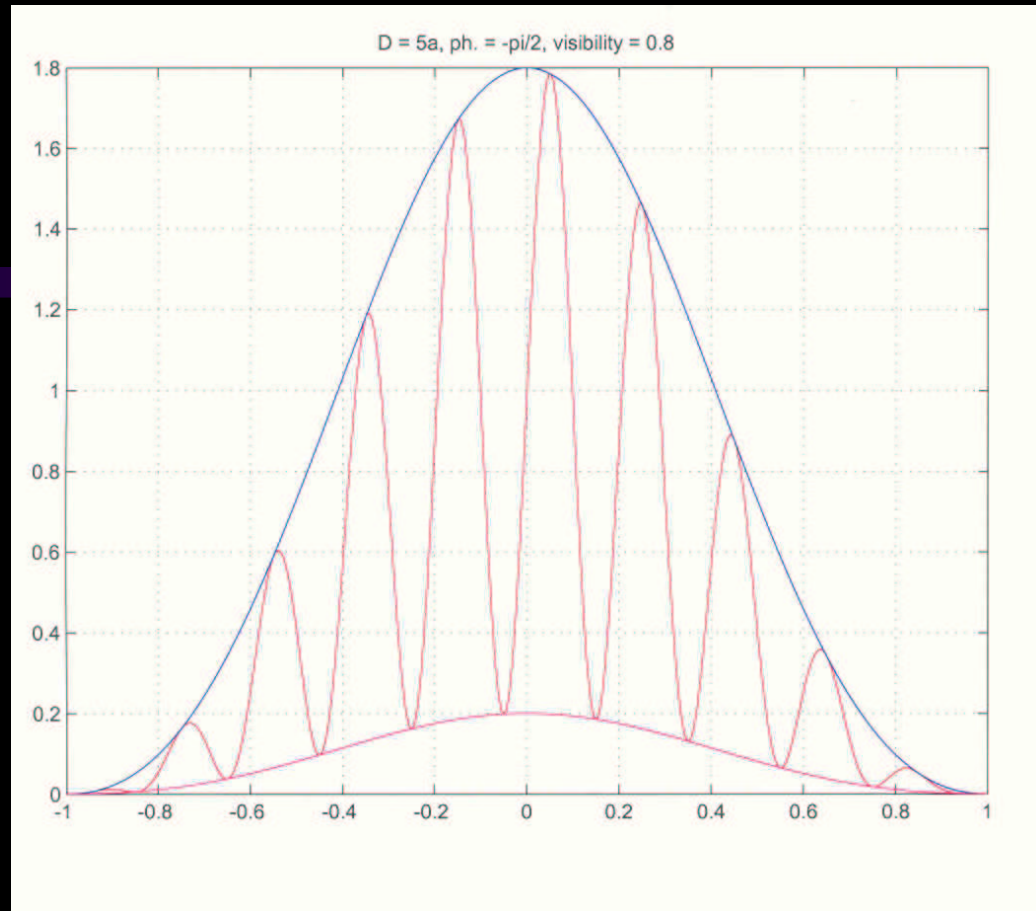
$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \phi)]$$



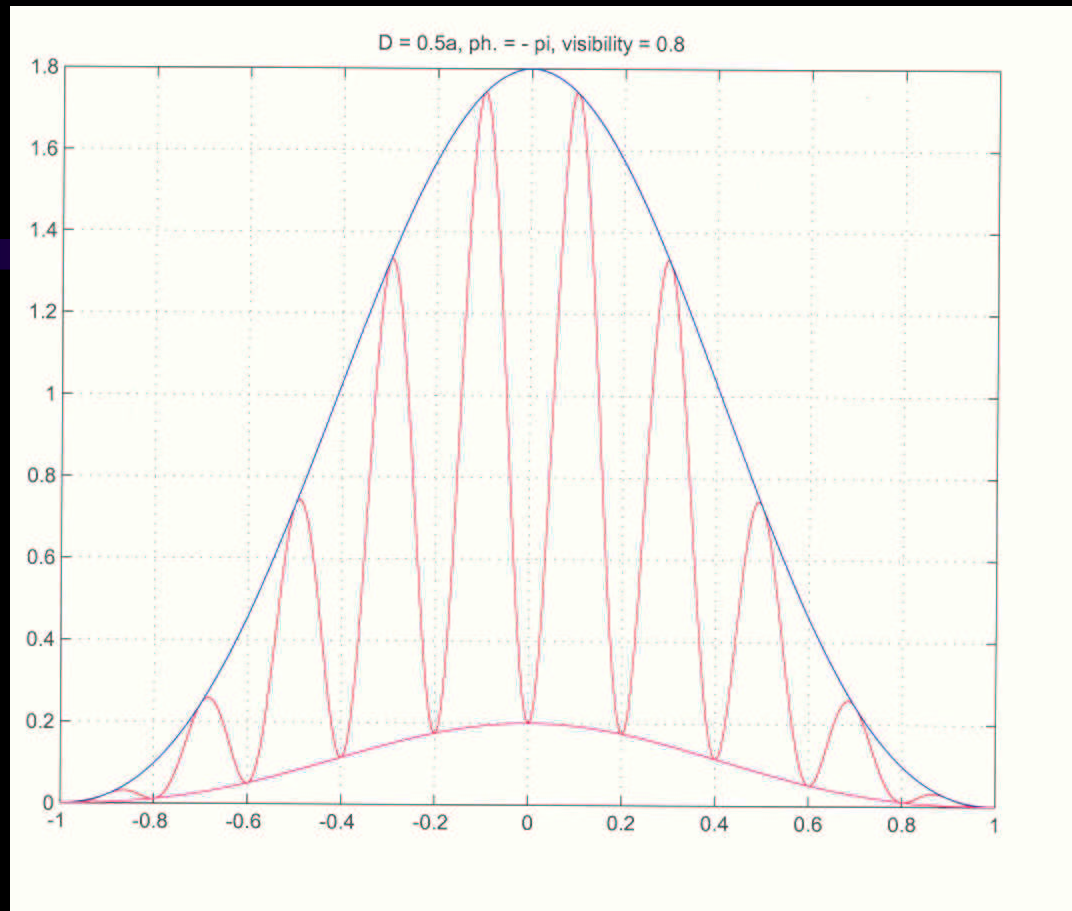
$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \phi)]$$

$$\text{Env}_{1,2}(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 \pm V]$$

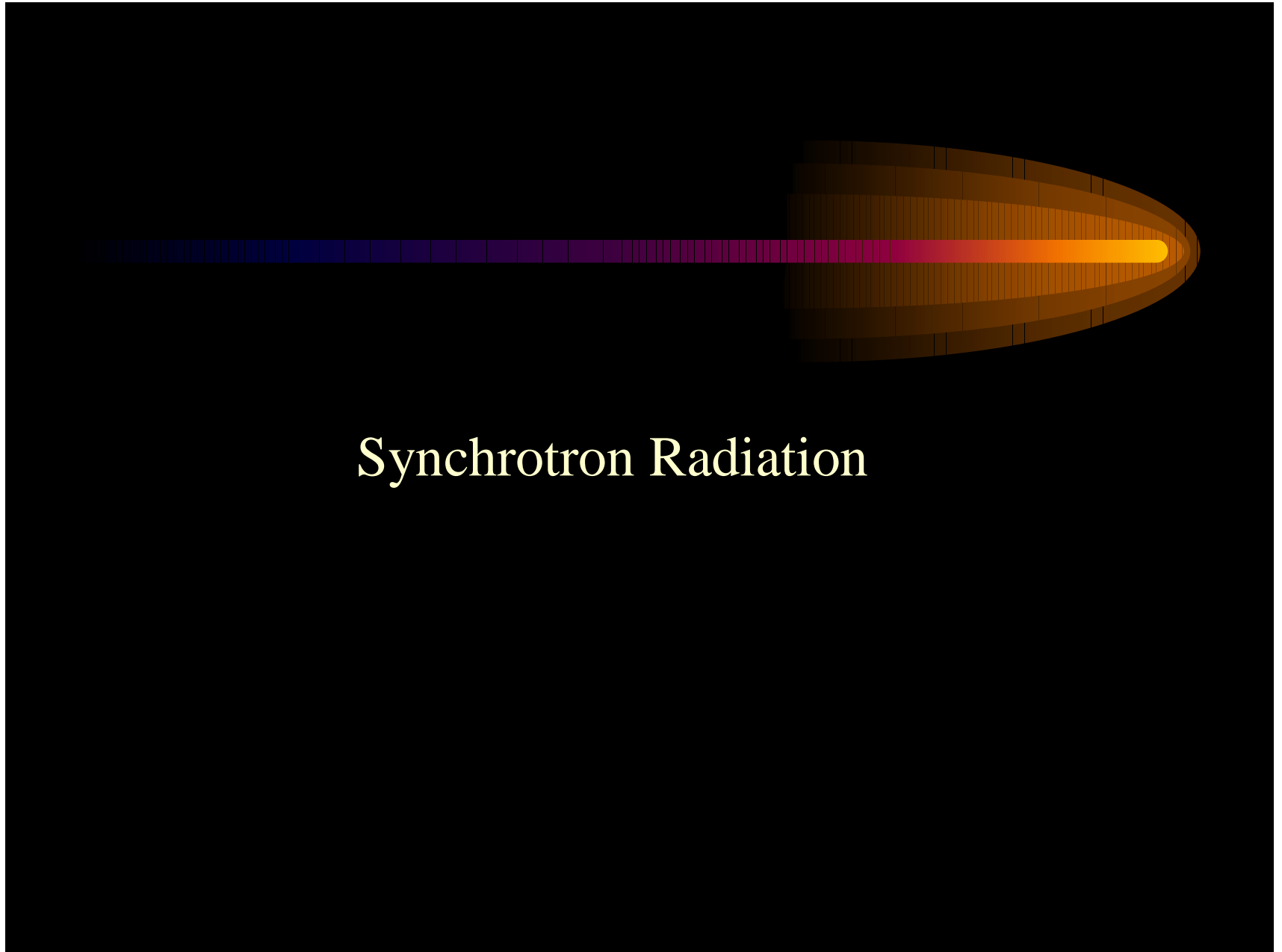




$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \varphi)]$$

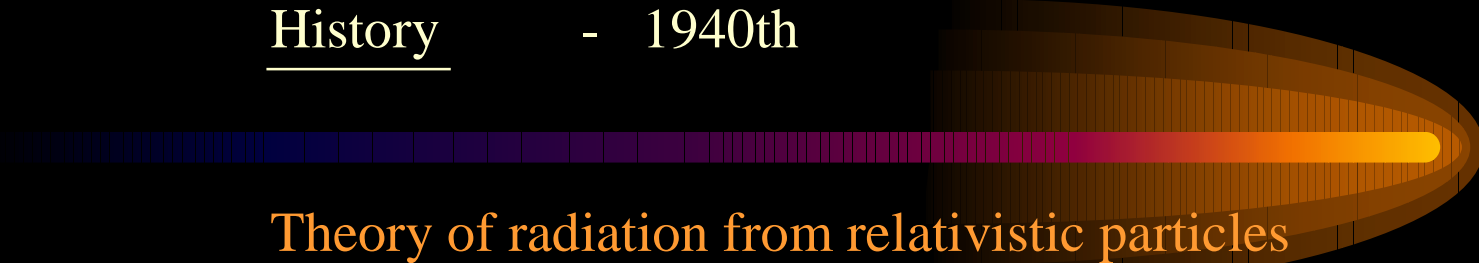


$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \varphi)]$$



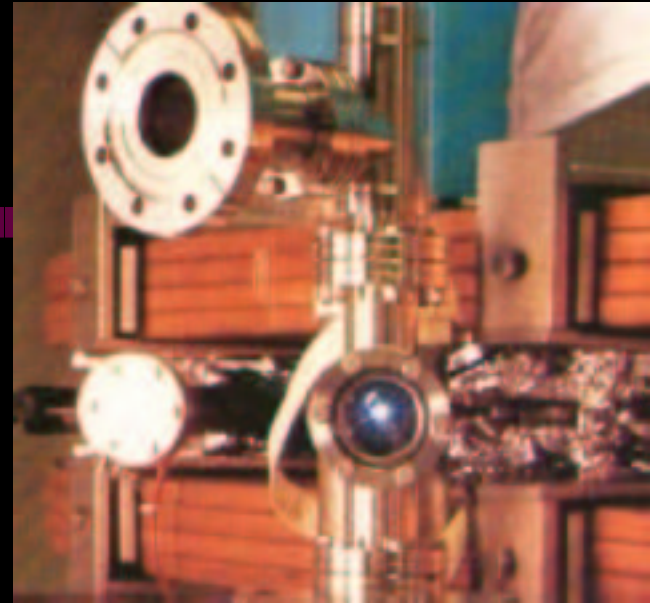
Synchrotron Radiation

History - 1940th



Theory of radiation from relativistic particles
Pomeranchuk, Ivanenko, Sokolov, Ternov (USSR)
Schwinger (USA)

Synchrotron ideas - 1945
Veksler (USSR), McMillan (USA)



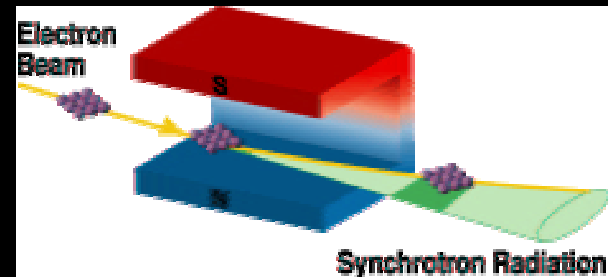
The first visual observation of synchrotron radiation was in 1947 from the General Electric synchrotron in the USA.

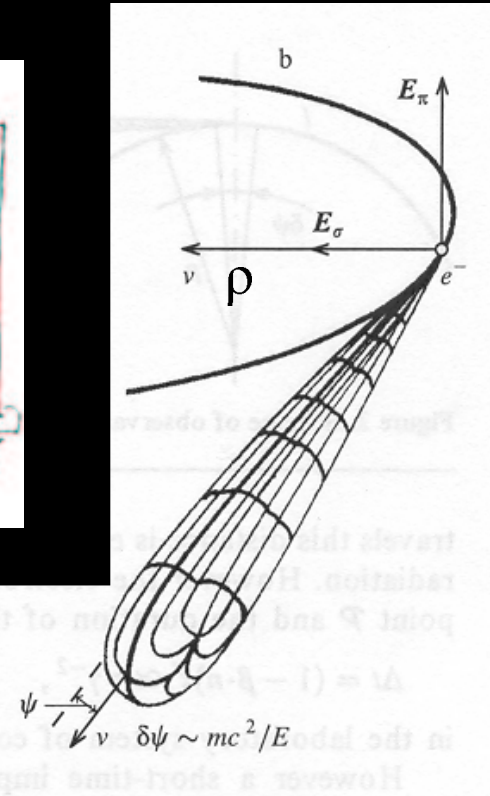
Synchrotron radiation (SR) is emitted from relativistic charged particles when their paths are changed.

By the magnetic field, for example.



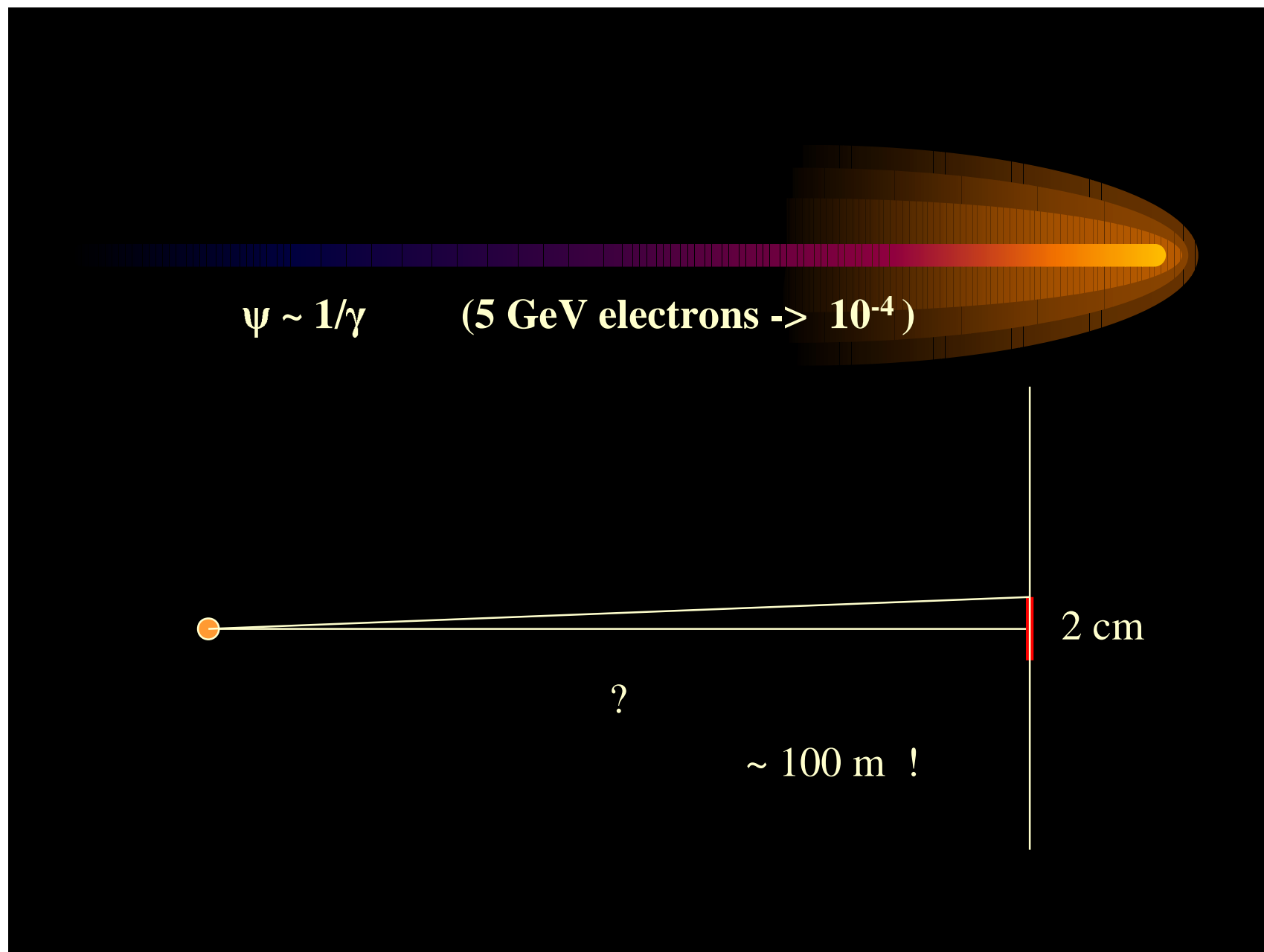
Everywhere further we will consider only the synchrotron radiation from electrons generated in the bending magnets.





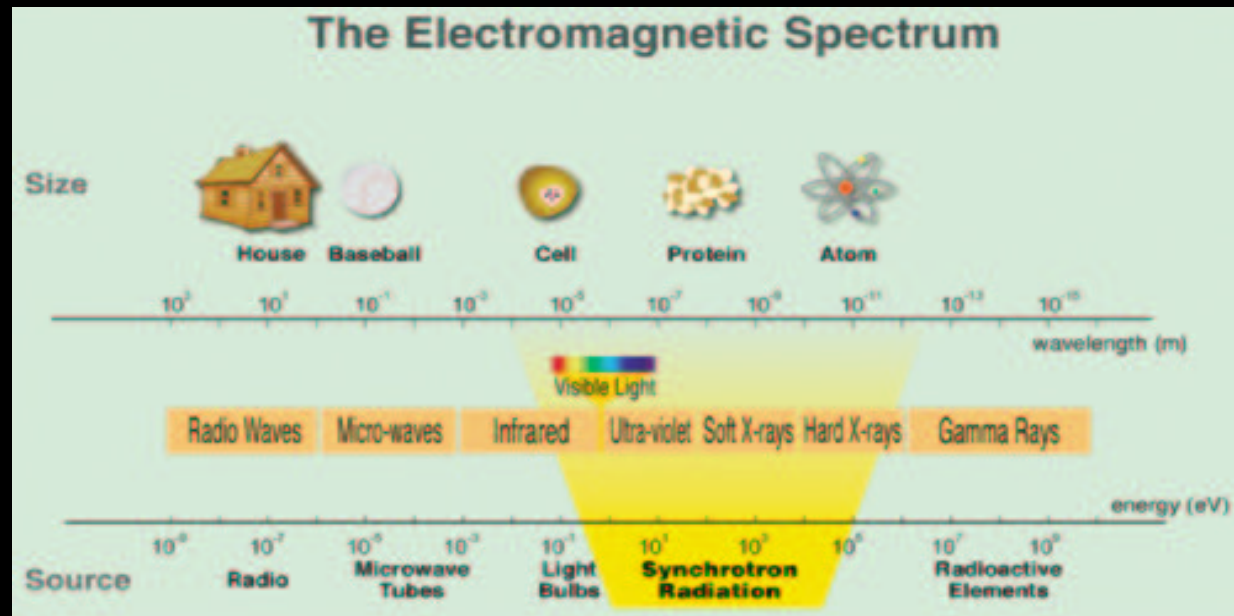
Because of the relativistic effect, the synchrotron radiation is emitted in a narrow cone in the forward direction, at a tangent to the orbit

$$\psi \sim 1/\gamma \quad (5 \text{ GeV electrons} \rightarrow 10^{-4})$$

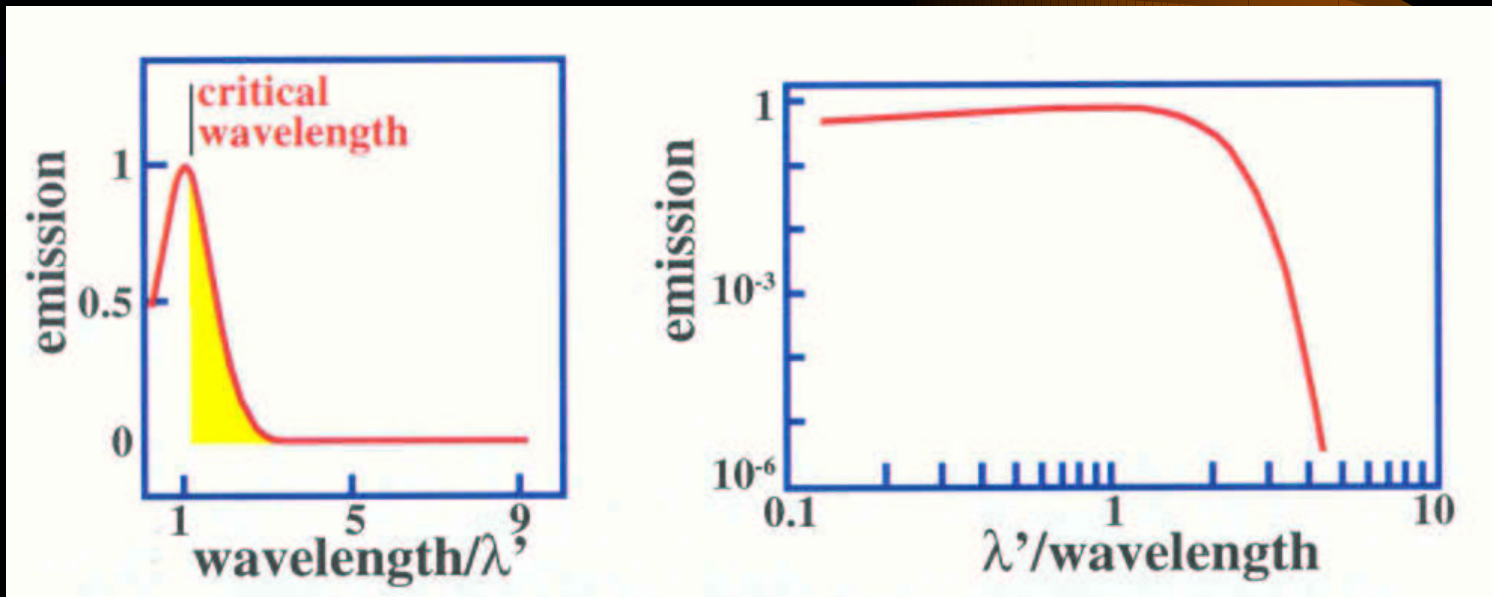


Synchrotron radiation

- extremely intense and highly collimated
- highly polarized (E_σ and E_π)
- has a wide energy spectrum (from infrared to γ -rays)

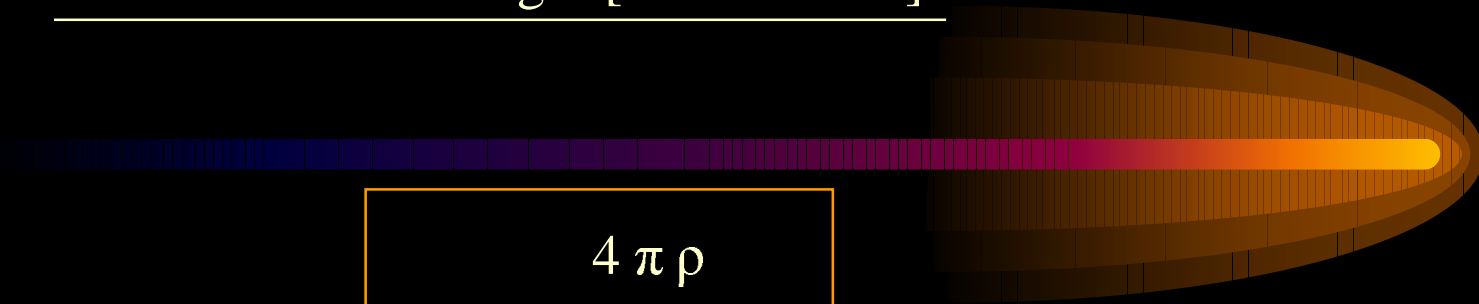


A typical energy spectrum of synchrotron radiation



The critical wavelength λ' (or λ_c) divides the radiated power into two equal parts: one-half of the power is radiated above this wavelength and one-half below.

The critical wavelength [A. Hofmann]



$$\lambda_c = \frac{4 \pi \rho}{3 \gamma^3}$$

Example: 5 GeV electrons, $\rho = 40$ m

$$\lambda_c = 0.16 \text{ nm}$$

At low frequencies the properties of synchrotron radiation are independent of the particle energy and depend only on the radius ρ of the curvature.

The rms opening angle for $\lambda \gg \lambda_c$

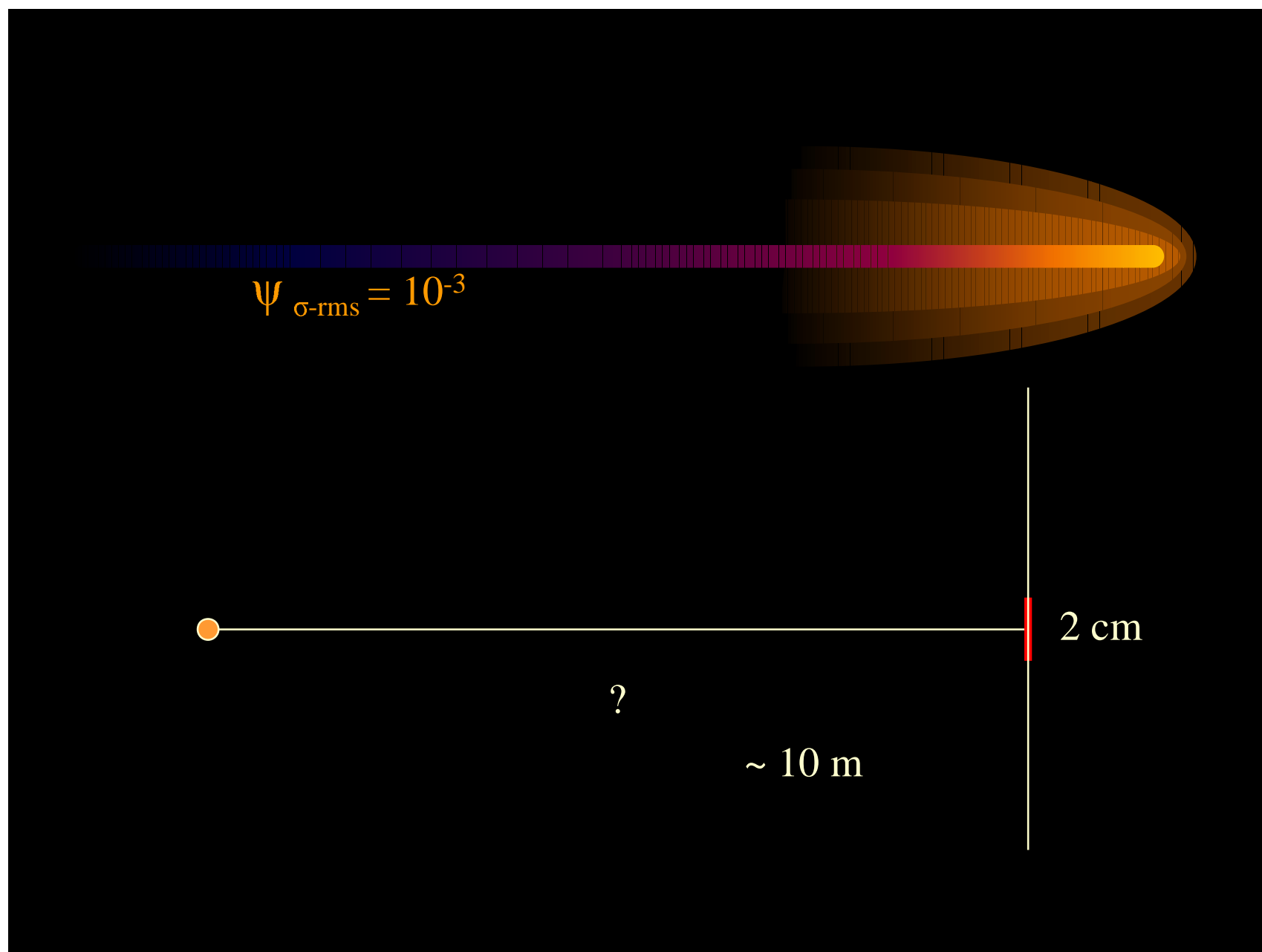
$$\psi_{\sigma\text{-rms}} = 0.41 (\lambda / \rho)^{1/3}$$

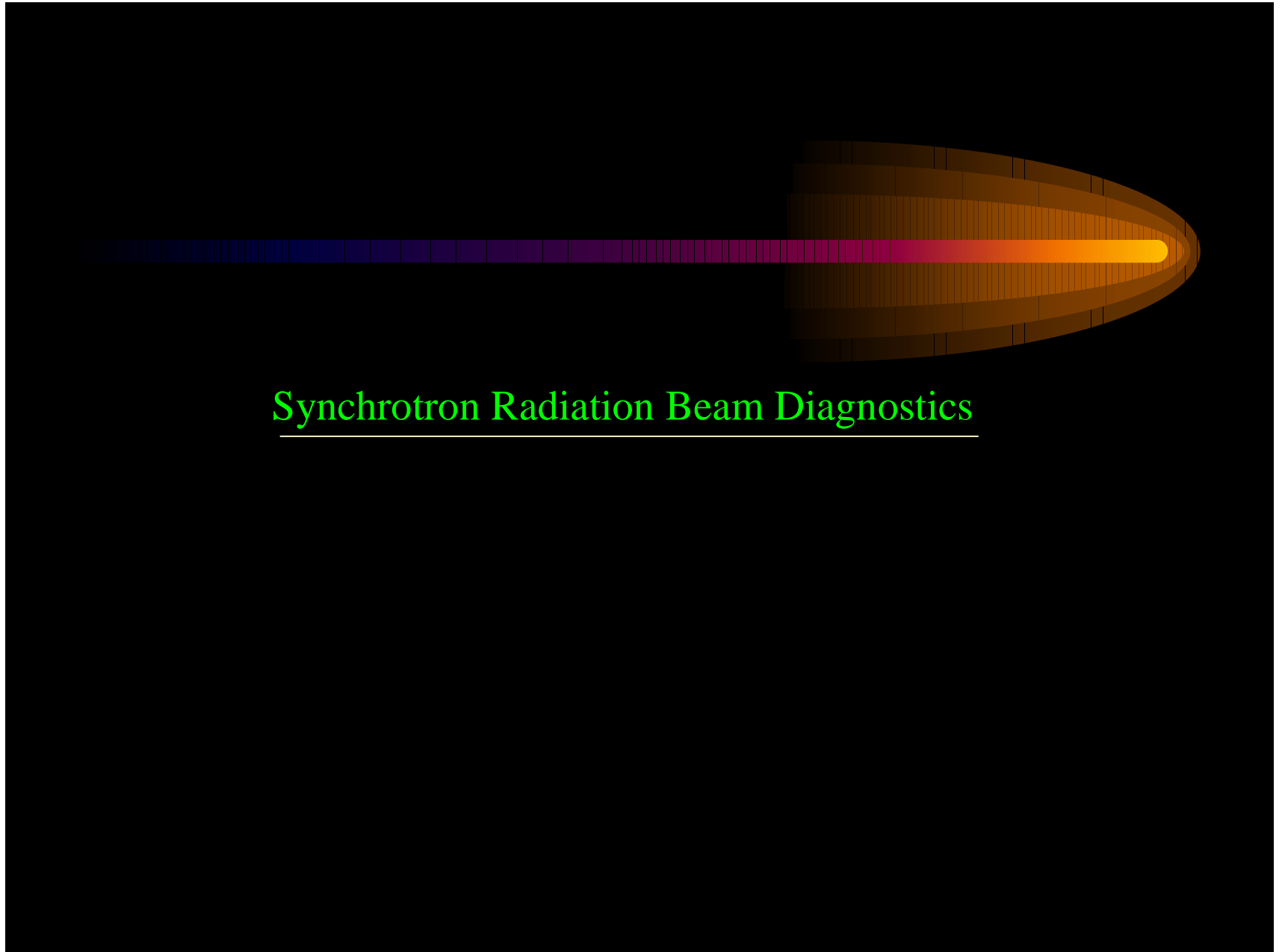
$$\psi_{\pi\text{-rms}} = 0.55 (\lambda / \rho)^{1/3}$$



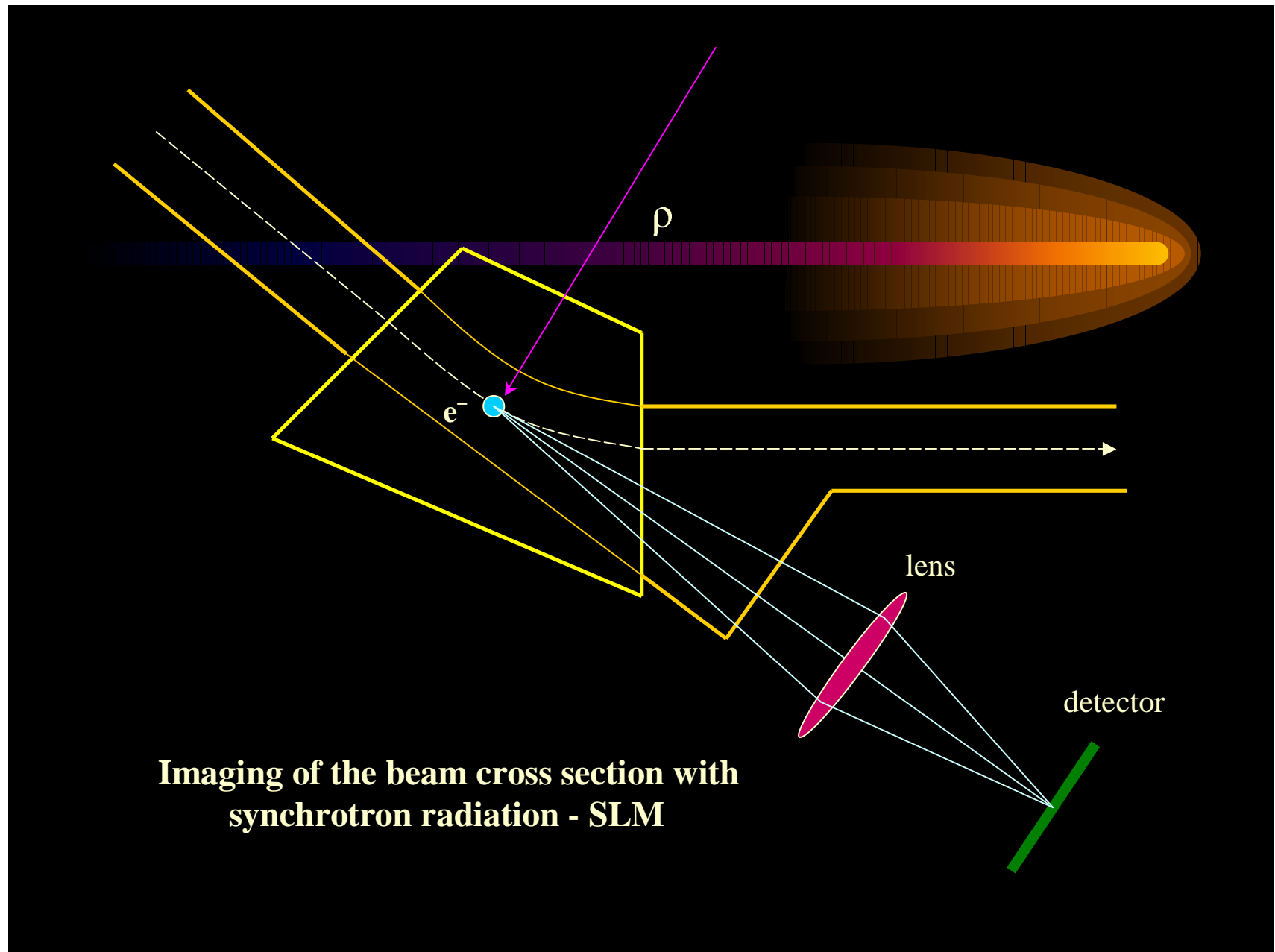
Example: $\lambda = 630 \text{ nm}$, $\rho = 40 \text{ m}$

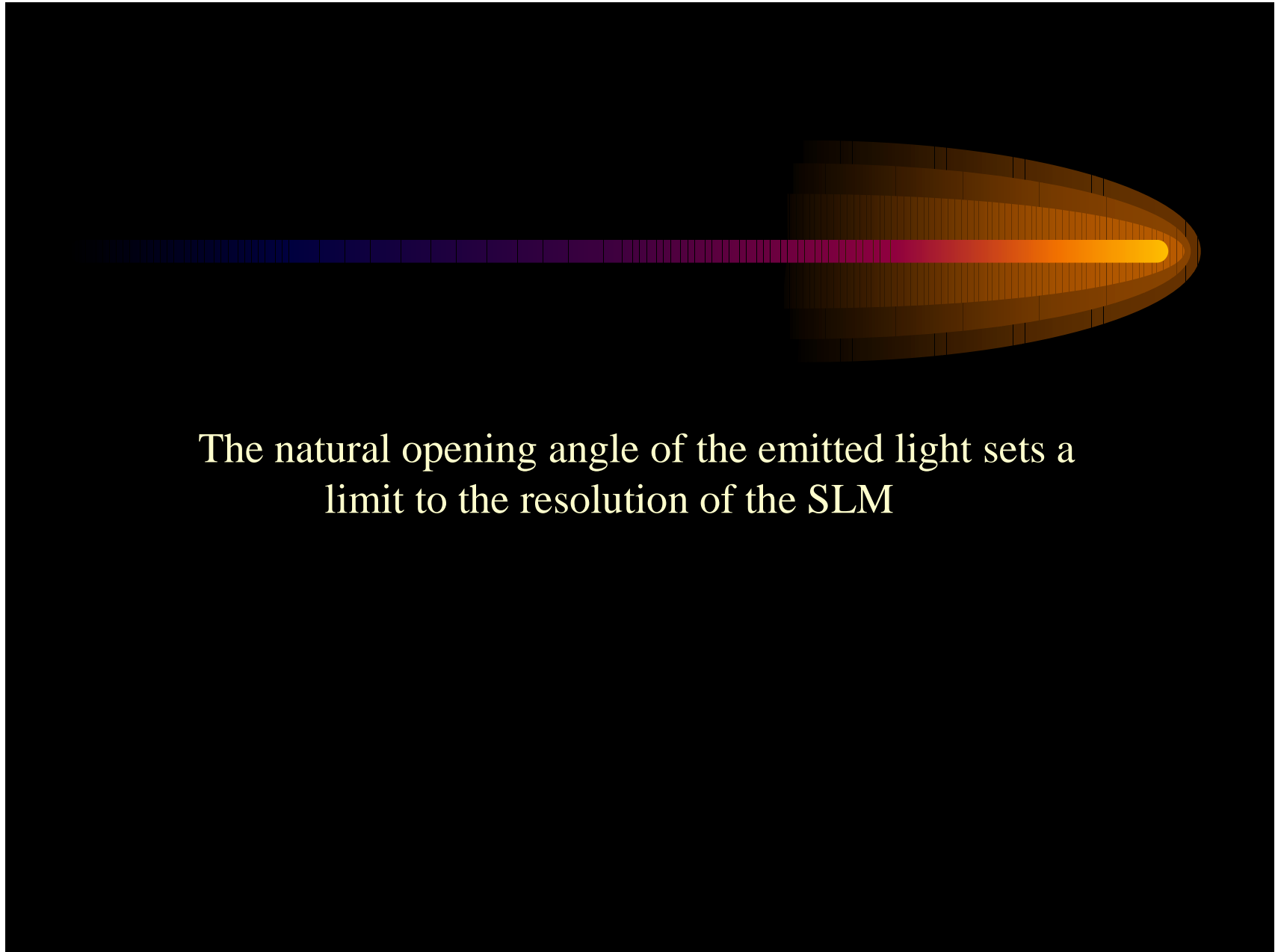
$$\psi_{\sigma\text{-rms}} = 10^{-3}$$





Synchrotron Radiation Beam Diagnostics





The natural opening angle of the emitted light sets a
limit to the resolution of the SLM

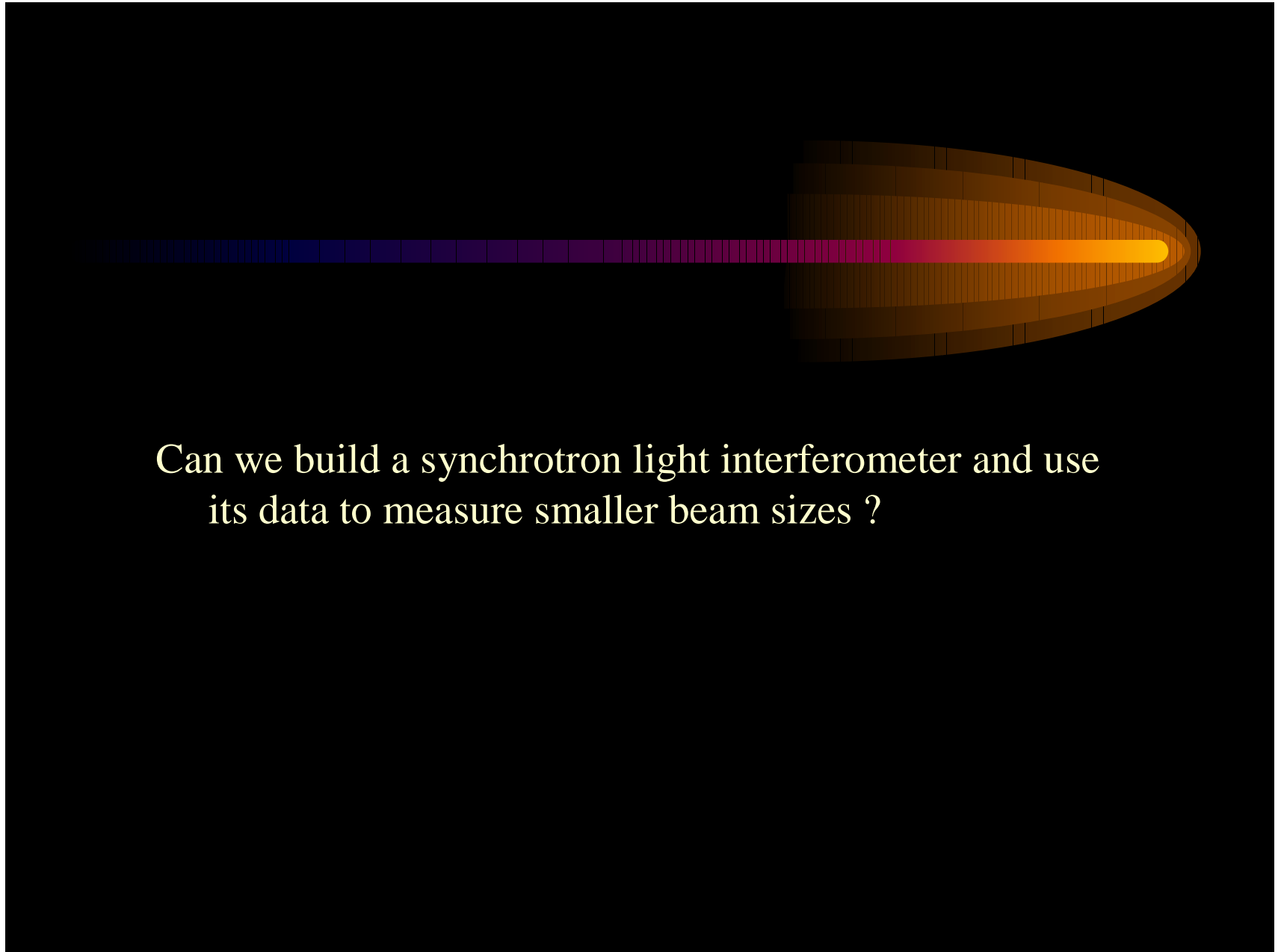
The diffraction limited resolution of synchrotron light imaging systems in the visible part of the spectrum [A.Hofmann]:

$$\sigma_s \approx 0.3 (\lambda^2 \rho)^{1/3}$$

Example:

$$\lambda = 630 \text{ nm}, \quad \rho = 40 \text{ m}$$

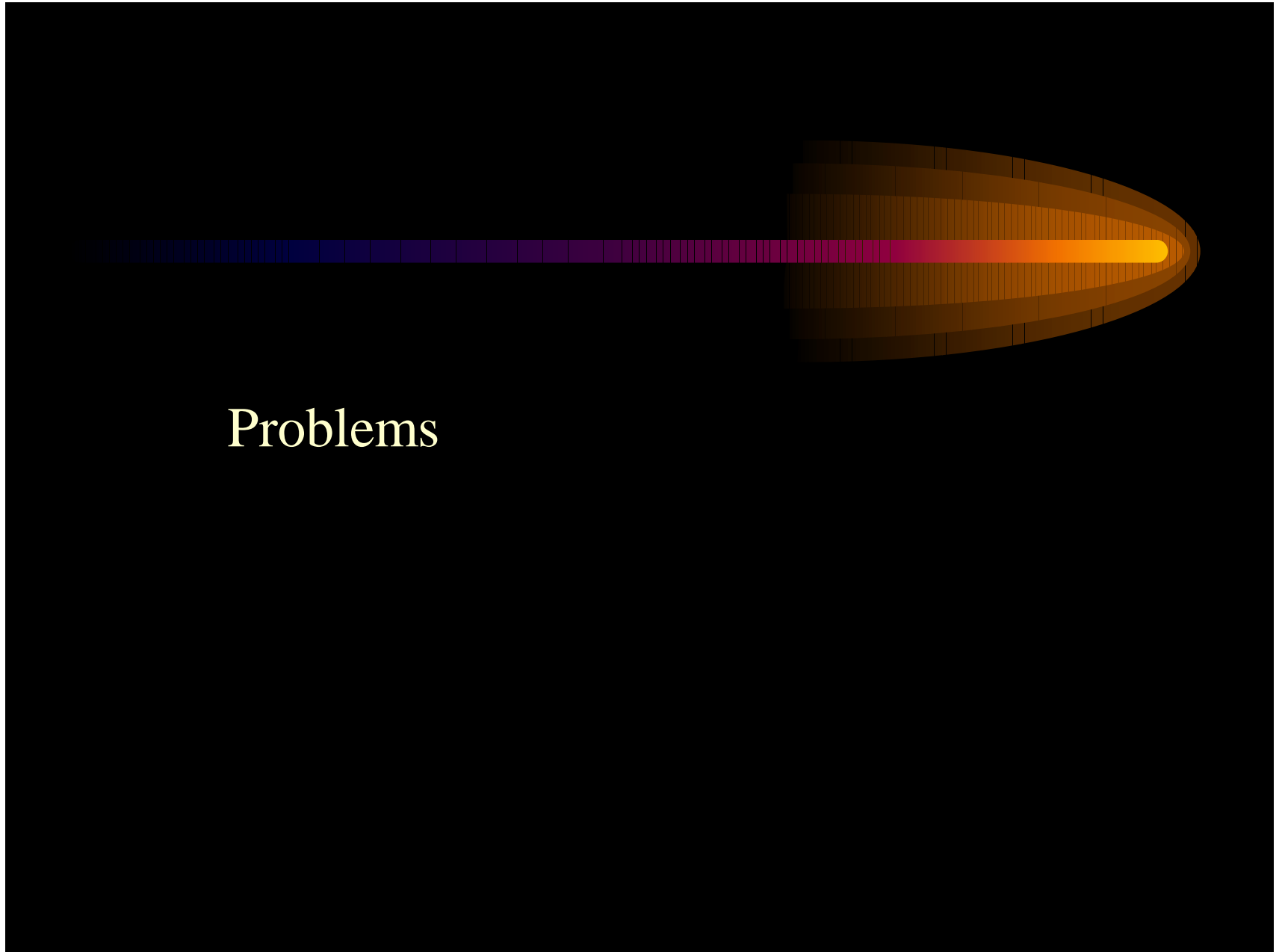
$$\sigma_s \approx 0.1 \text{ mm}$$



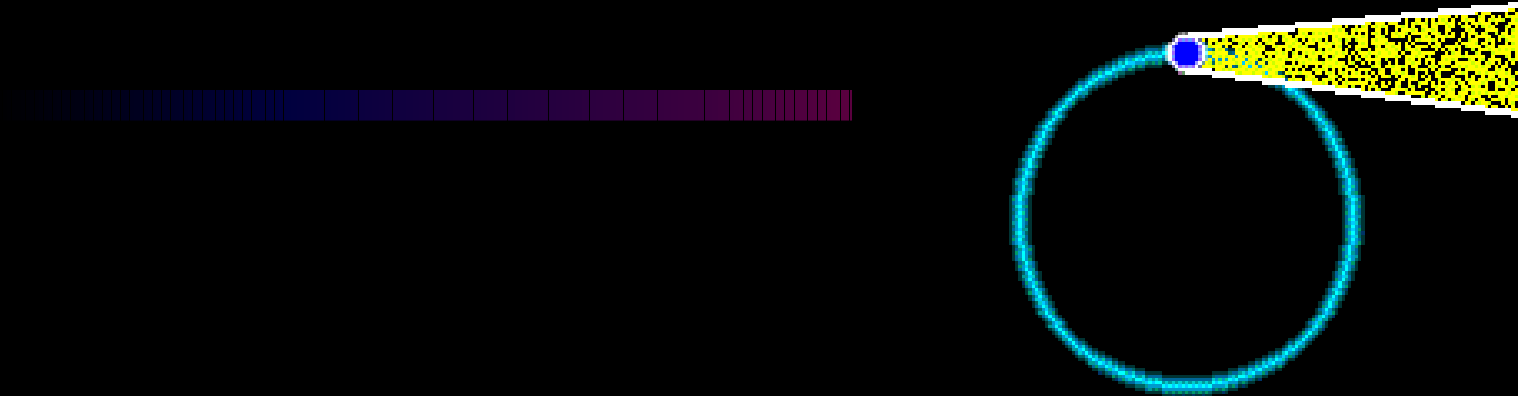
Can we build a synchrotron light interferometer and use
its data to measure smaller beam sizes ?



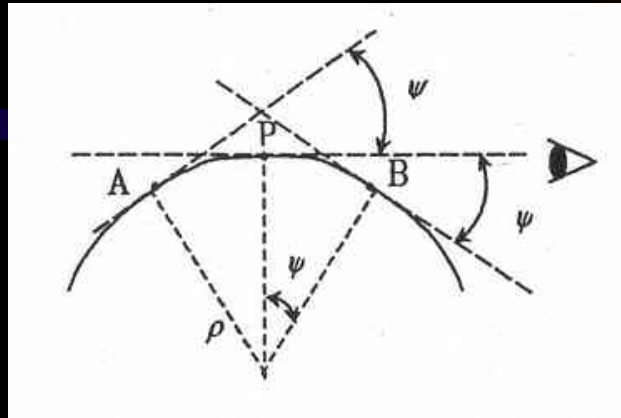
T. Mitsuhashi, Photon Factory, KEK, Japan



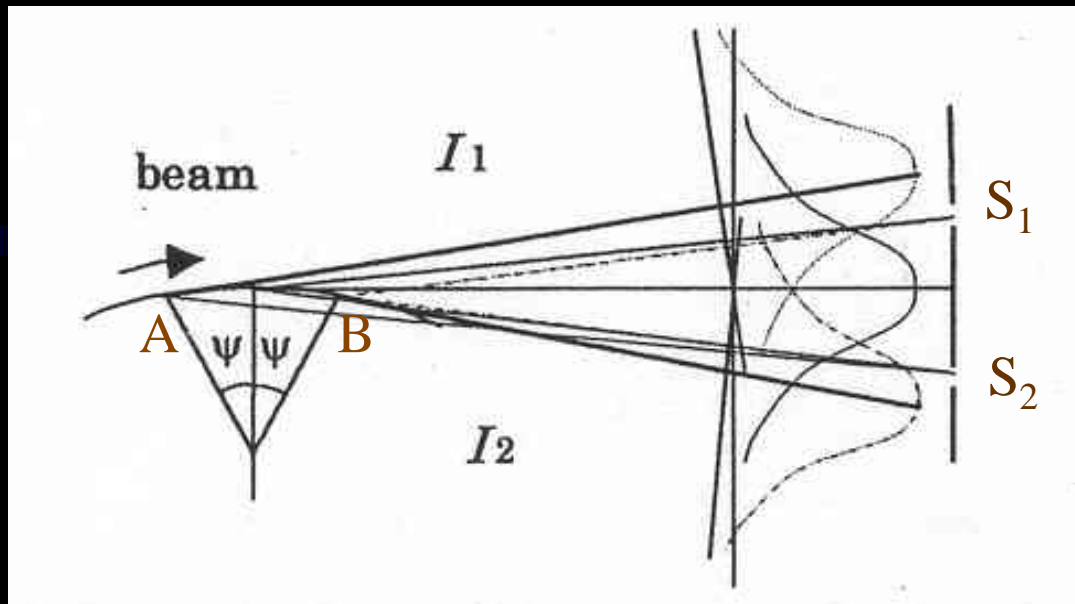
Problems



Synchrotron radiation is like a moving narrow searchlight in horizontal direction.

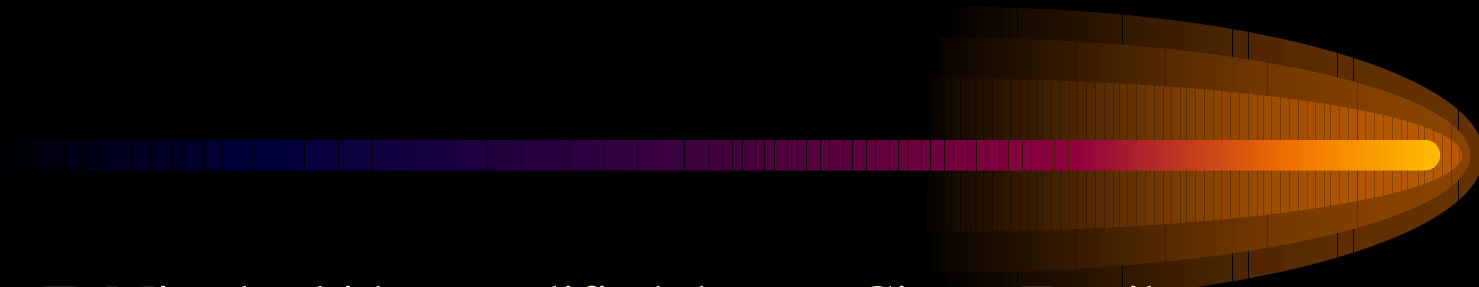


We observe photons coming from different positions when the electron moves from point A to point B. We must sum these photons.



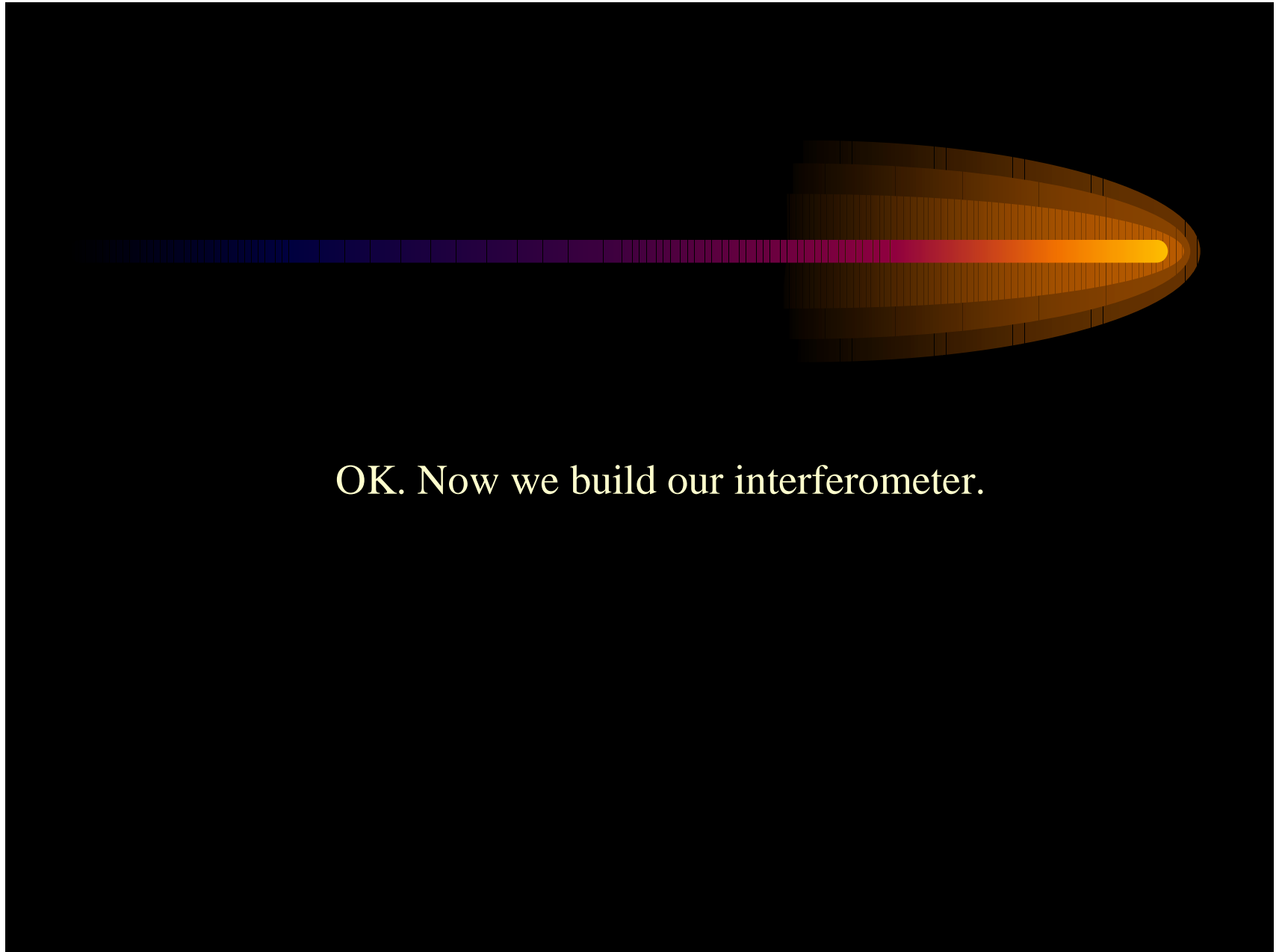
When an electron is moving from point A to point B, the light is sweeping from slit S_1 to slit S_2 .

- The intensities of two modes of light illuminating the slits are different.



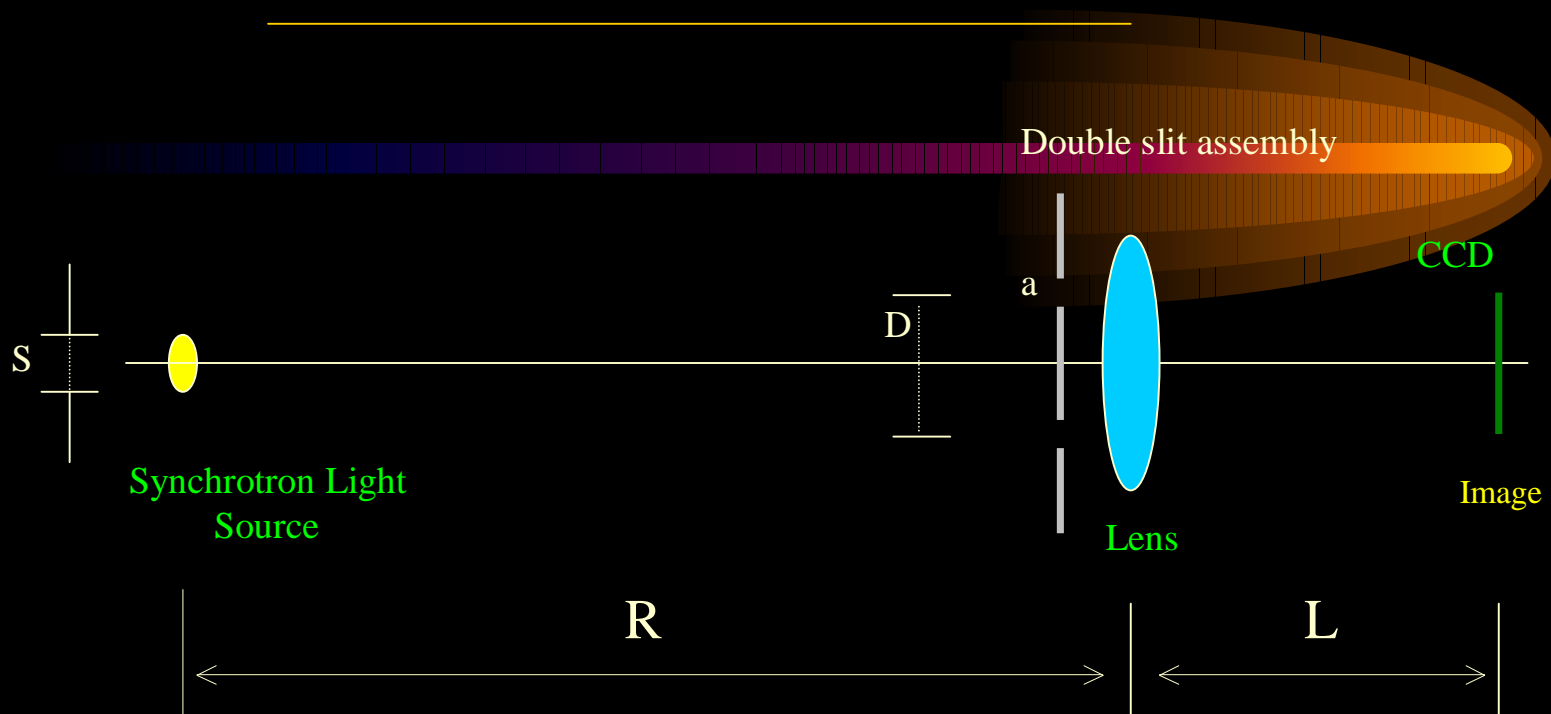
T. Mitsuhashi has modified the van Cittert-Zernike theorem and developed the method to calculate the beam size on the basis of the interference picture for the synchrotron light emitted by the beam.

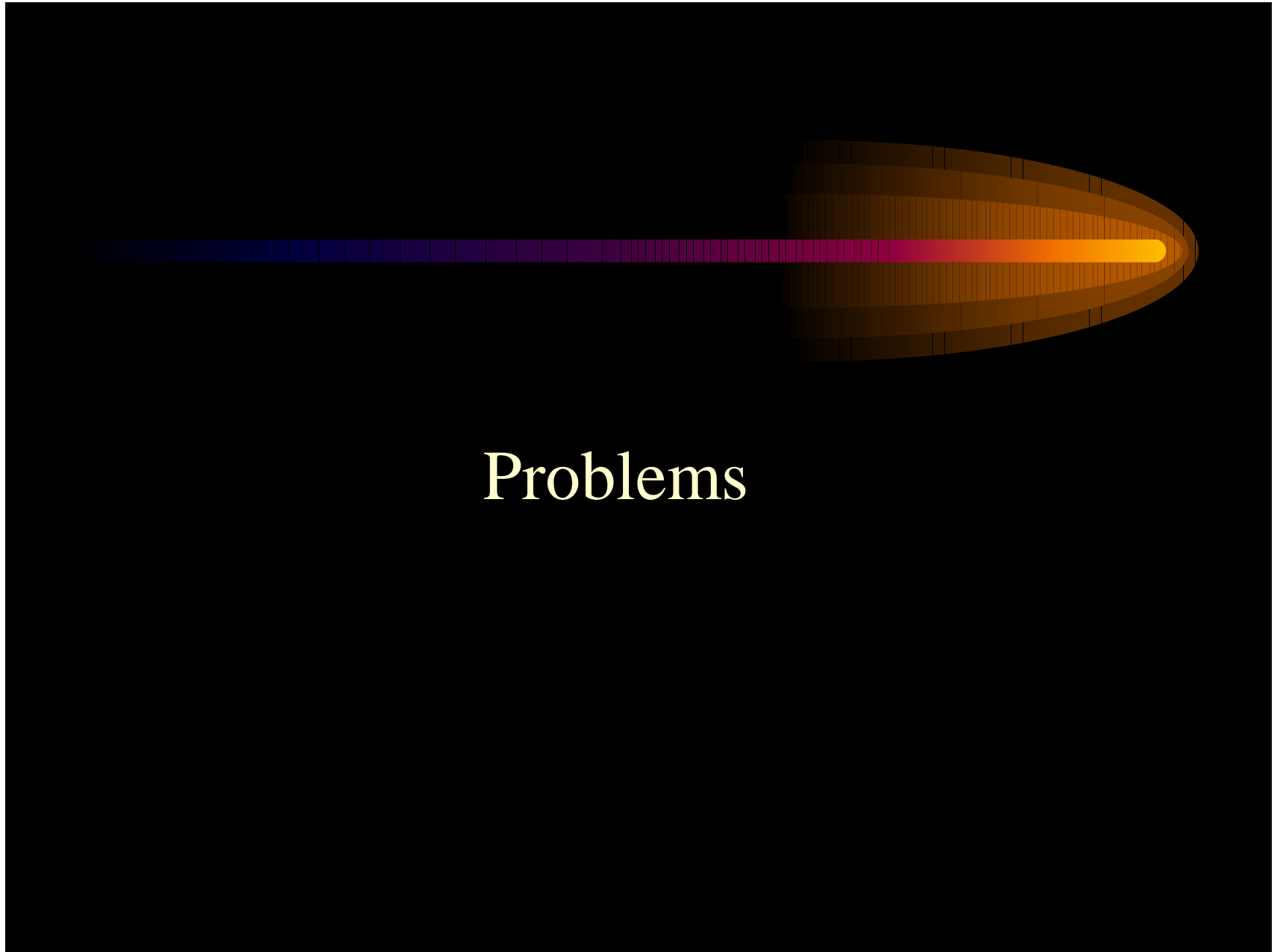
“Beam Profile and Size Measurement by the Use of the Synchrotron Light Interferometer”



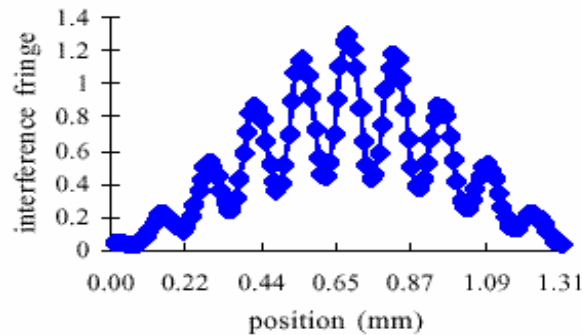
OK. Now we build our interferometer.

Synchrotron Radiation Interferometer

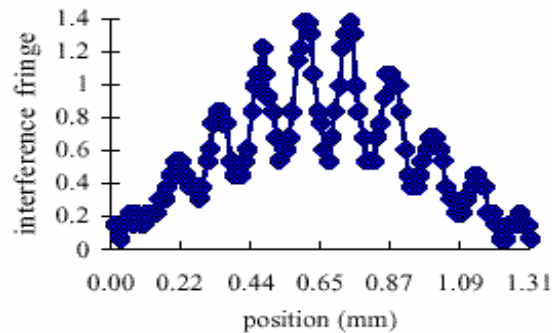




Problems

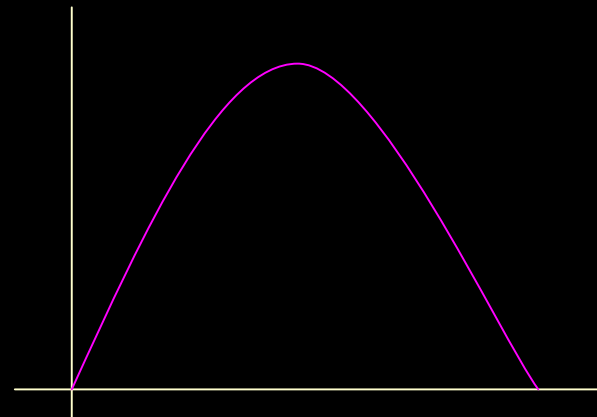


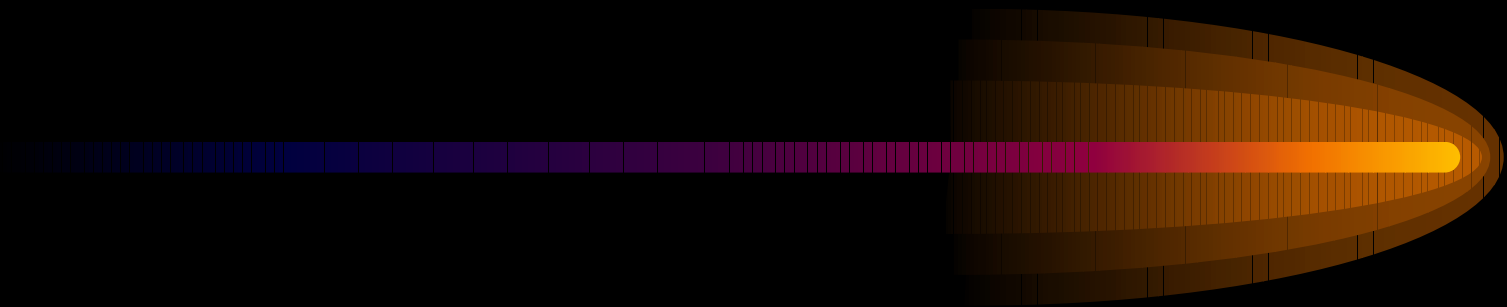
a) interferogram by s-polarized components.



b) interferogram by p-polarized components.

Two polarized components of the synchrotron light (p and s) are “in anti-phase”. Their superposition will not give us the interference fringes at all.
 -> We get just a sort of a “SLM”.

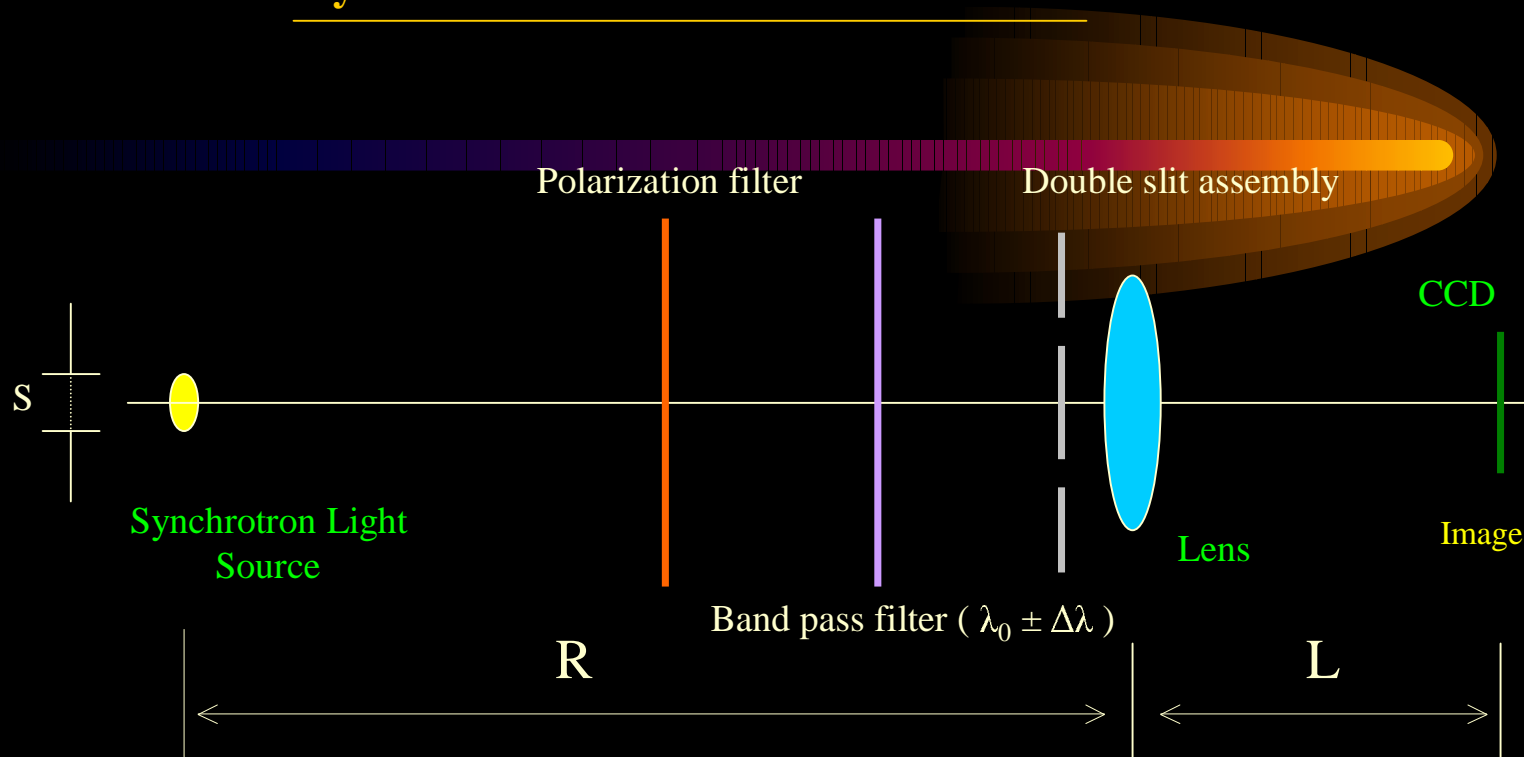




The synchrotron light is not monochromatic.

λ range is the whole visible spectrum !

Synchrotron Radiation Interferometer



DataCube Setup for Hall A 1C12 SLM – Multiplex

(2002-04-15, Chevtsov)

video ☐ disabled ☒ enabled

Video camera ☐ Control ☒

☐ Diffraction ☒ slit control

Current **99.117** microAmp

Units Pixels mm

X Position 324.8

X Width (rms) 29.8

Y Position 45.8

Y Width (rms) 8.9

X Position 1.356

X Width (rms) 0.583

Y Position 4.052

Y Width (rms) 0.185

Advanced ☐

Display ☐

Trouble

Calibration screen HA Target ☐

Acquire Gain **1000**

LUT1 Mode Subtract ☐

LUT1 Threshold 40

Setup Scripts

Masks ☐ enable mask ☐ enable disp mask

MASK OUTSIDE

X1: 117

Y1: 1

X2: 470

Y2: 65

Saturated 3

Max Pixel 255

-255

-150

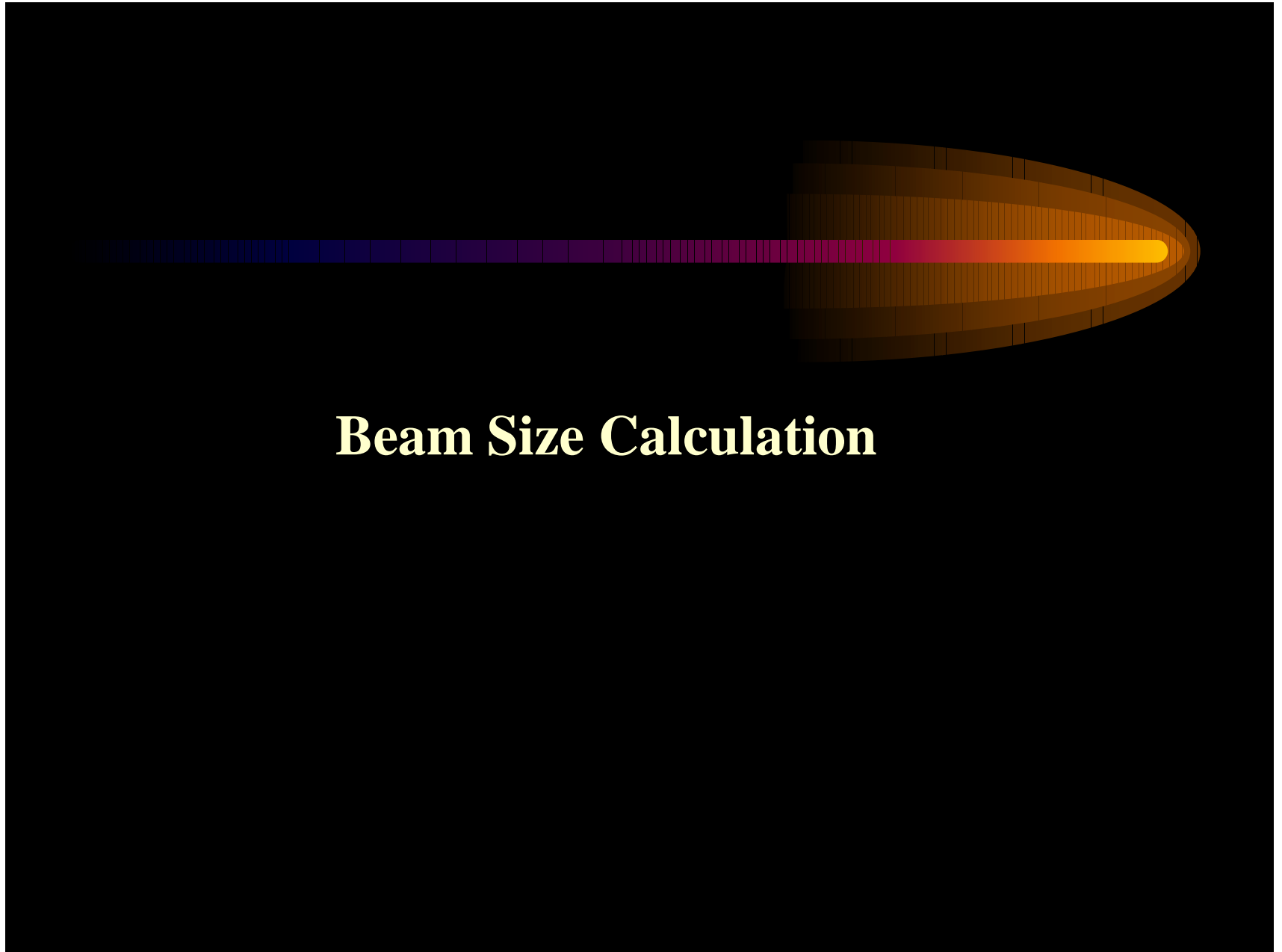
-100

-50

0

X profile

Y profile



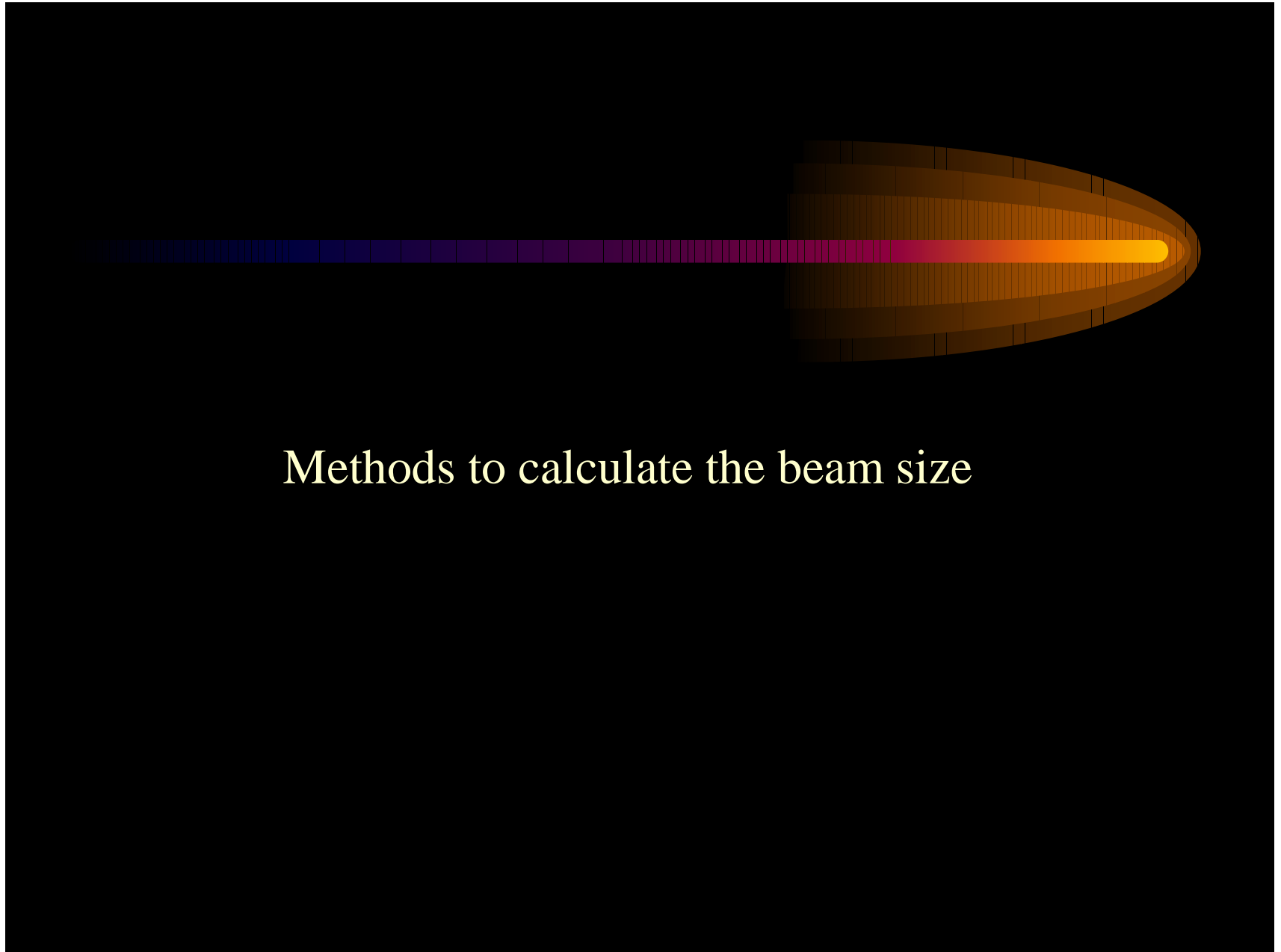
Beam Size Calculation

In case of a gaussian beam shape it is easy:

$$\Gamma(\theta) = \int I(\xi) \exp\{ -i 2\pi \theta \xi \} d \xi \qquad \Gamma = \frac{\Gamma(\theta)}{\Gamma(0)}$$

$$I(y) = I_0 \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \varphi)] \quad \alpha = kay/2L$$

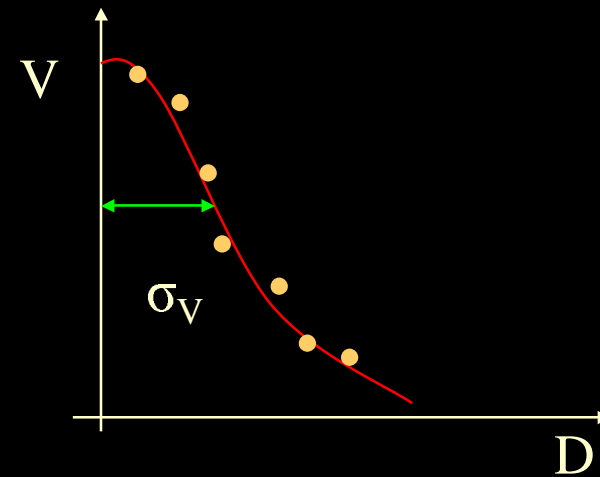
$$V = \exp\left(- \frac{2\pi^2 D^2 \sigma_{\text{beam}}^2}{\lambda^2 R^2} \right) = V(D)$$

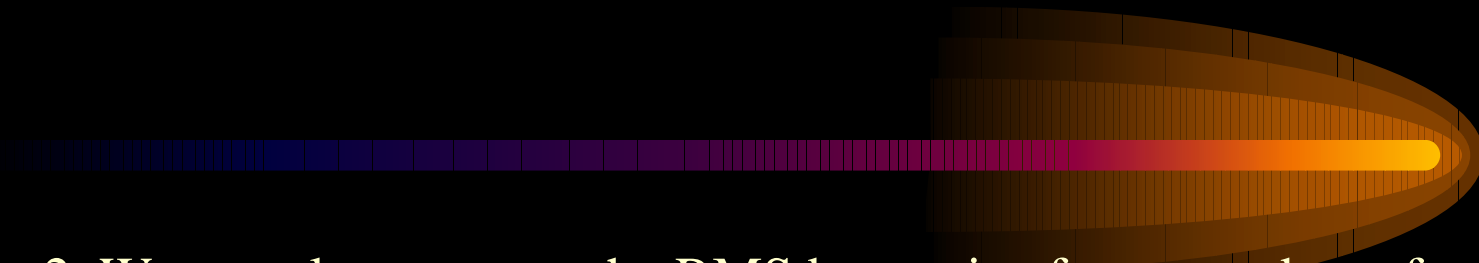


Methods to calculate the beam size

1. We measure (experimentally) the contrast of the interferogram as a function of the slit separation D . Then we define the RMS of the visibility curve σ_V .

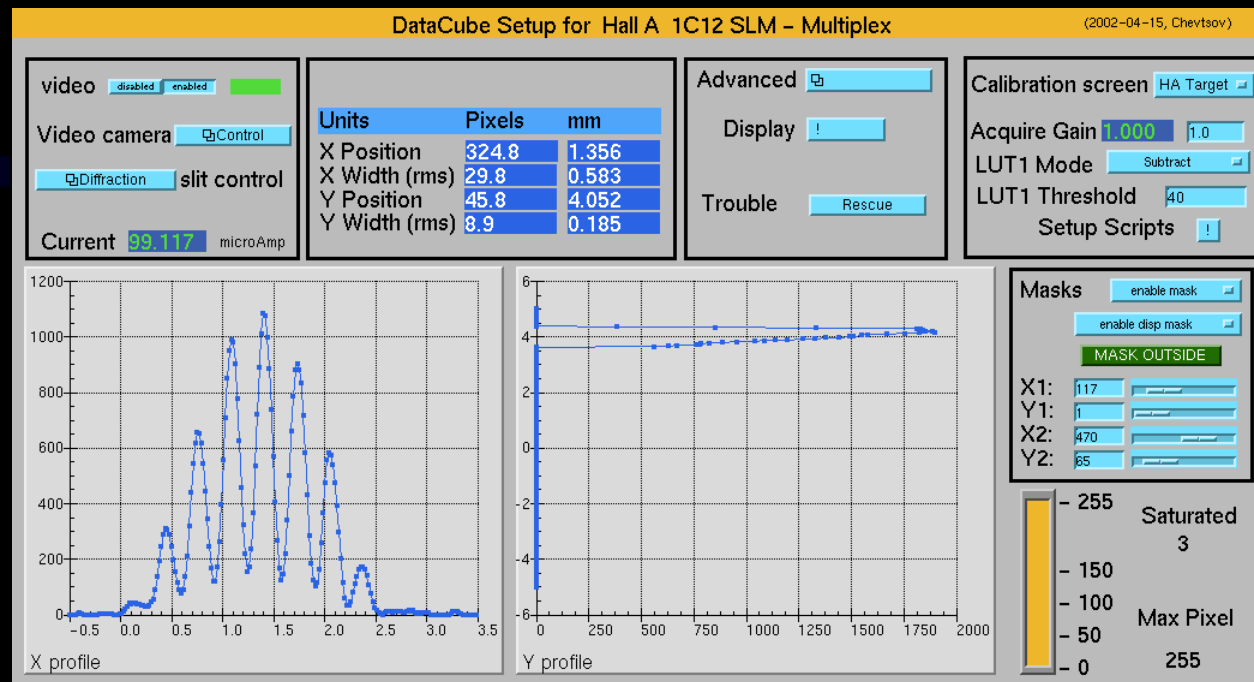
$$\sigma_{\text{beam}} = \frac{\lambda R}{2 \pi \sigma_V}$$





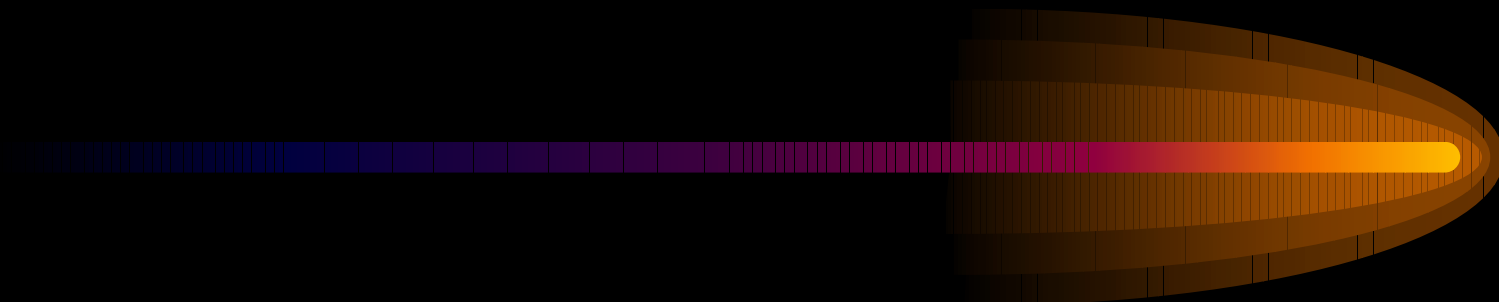
2. We can also measure the RMS beam size from one data of visibility which is measured at a fixed separation of a double slit assembly

$$\sigma_{\text{beam}} = \frac{\lambda R}{\pi D} \sqrt{0.5 \ln(1/V)}$$



$$V = 0.8$$

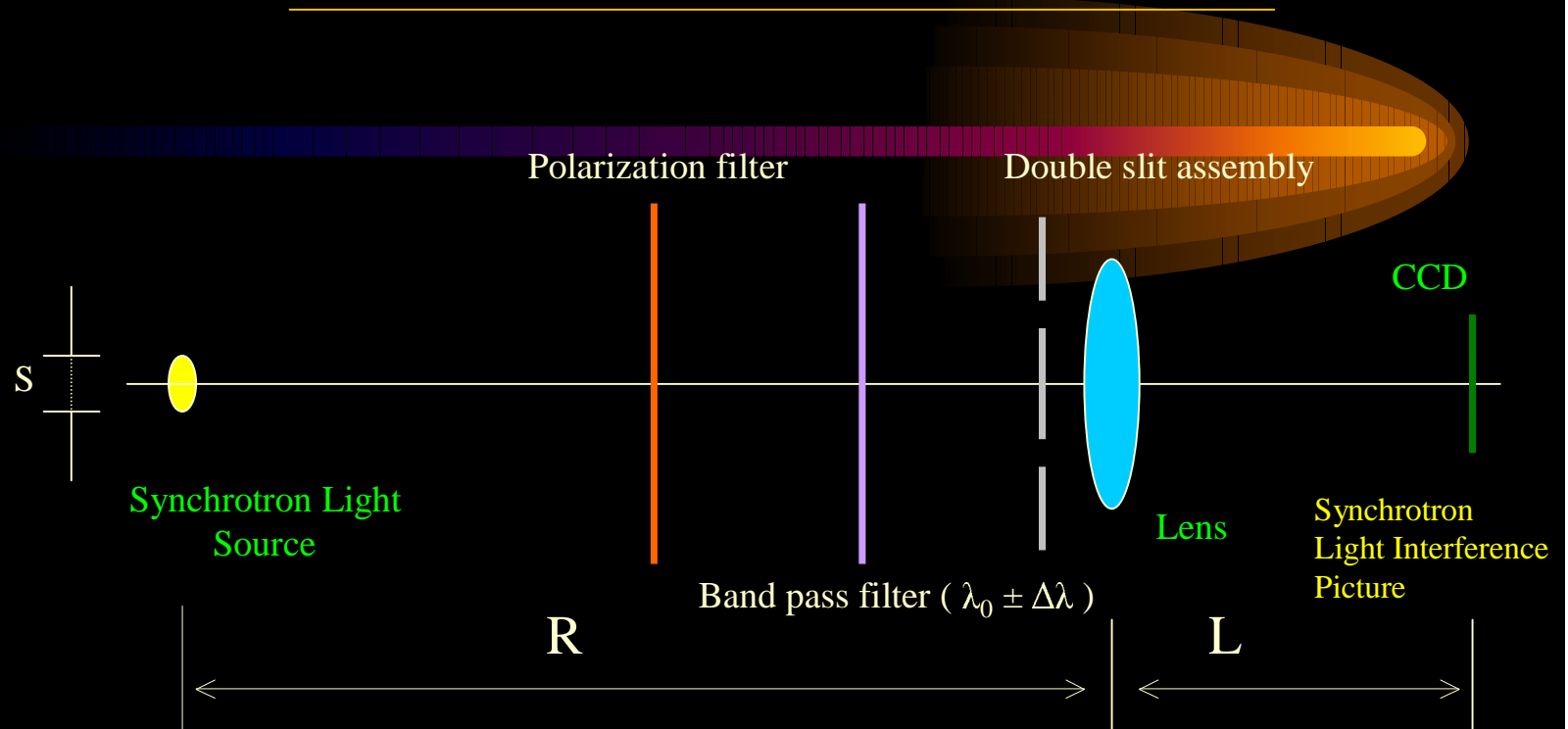
$$\sigma_s = 0.12 \text{ mm}$$



Synchrotron Light Interferometer at Jefferson Lab

Main Components

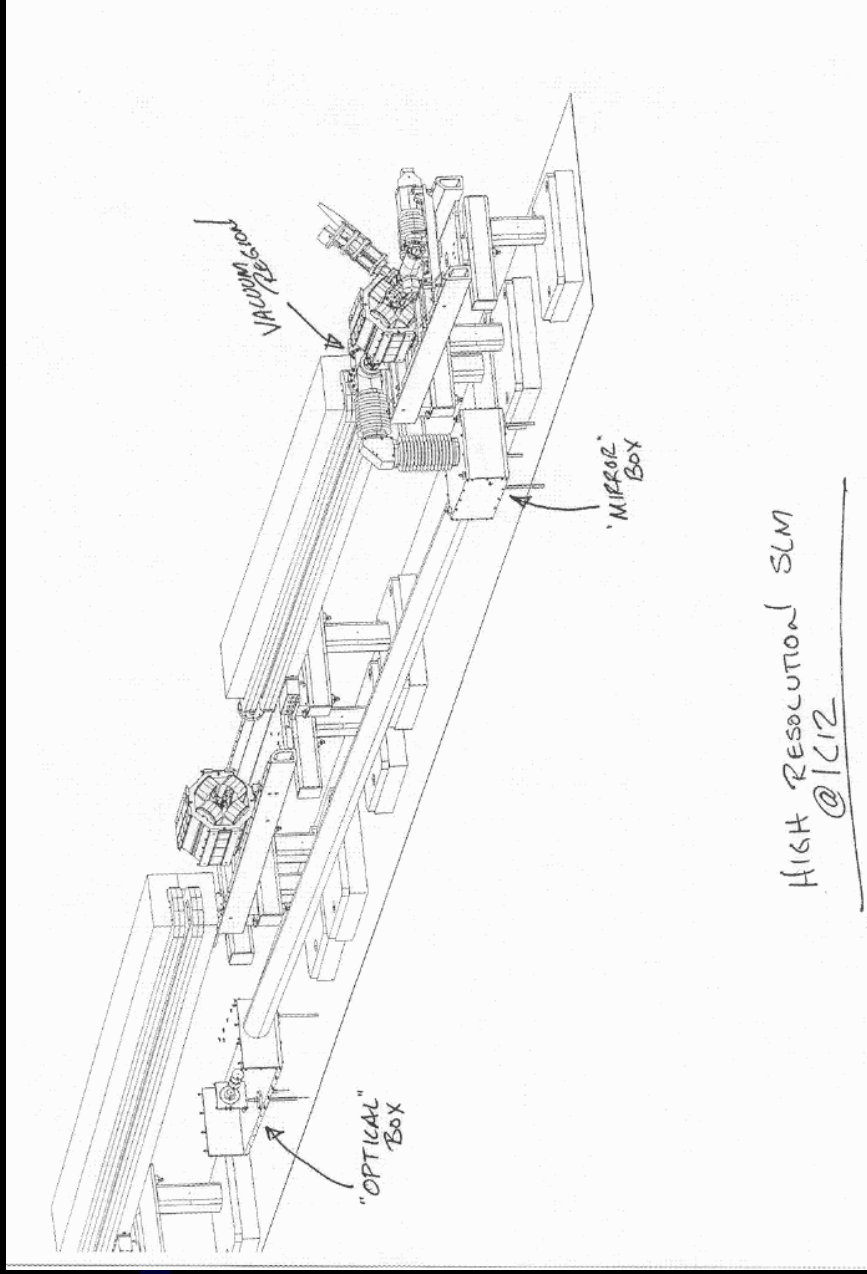
Synchrotron Radiation Interferometer at Jefferson Lab



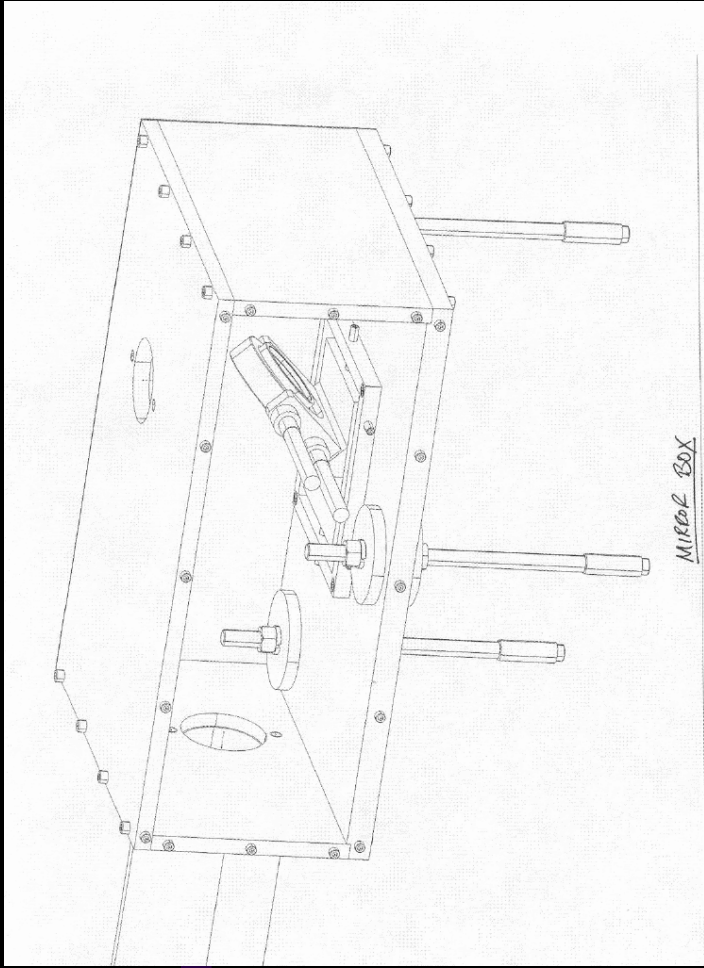
$$R = 9.18 \text{ m} \quad L = 1.12 \text{ m} \quad \lambda_0 = 630 \text{ nm} \quad \rho = 40 \text{ m}$$

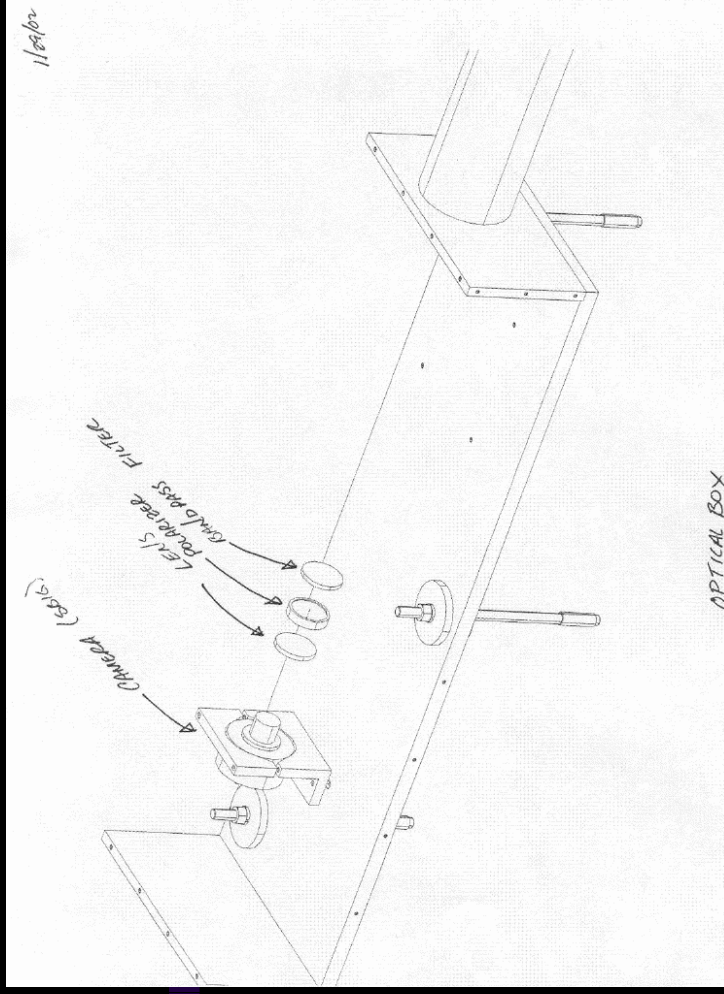


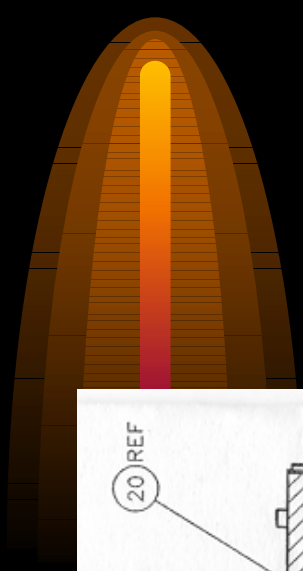
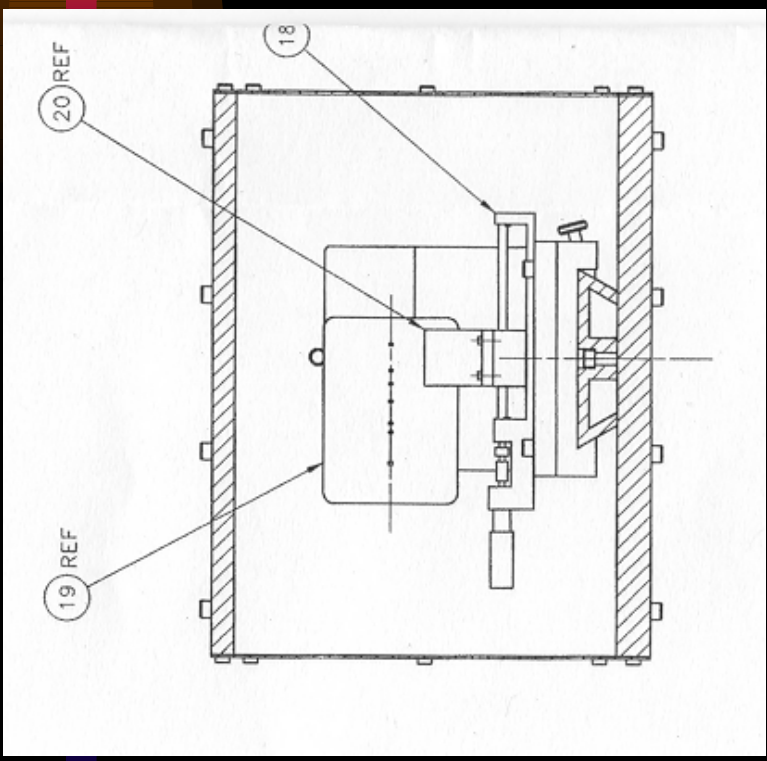
1C12

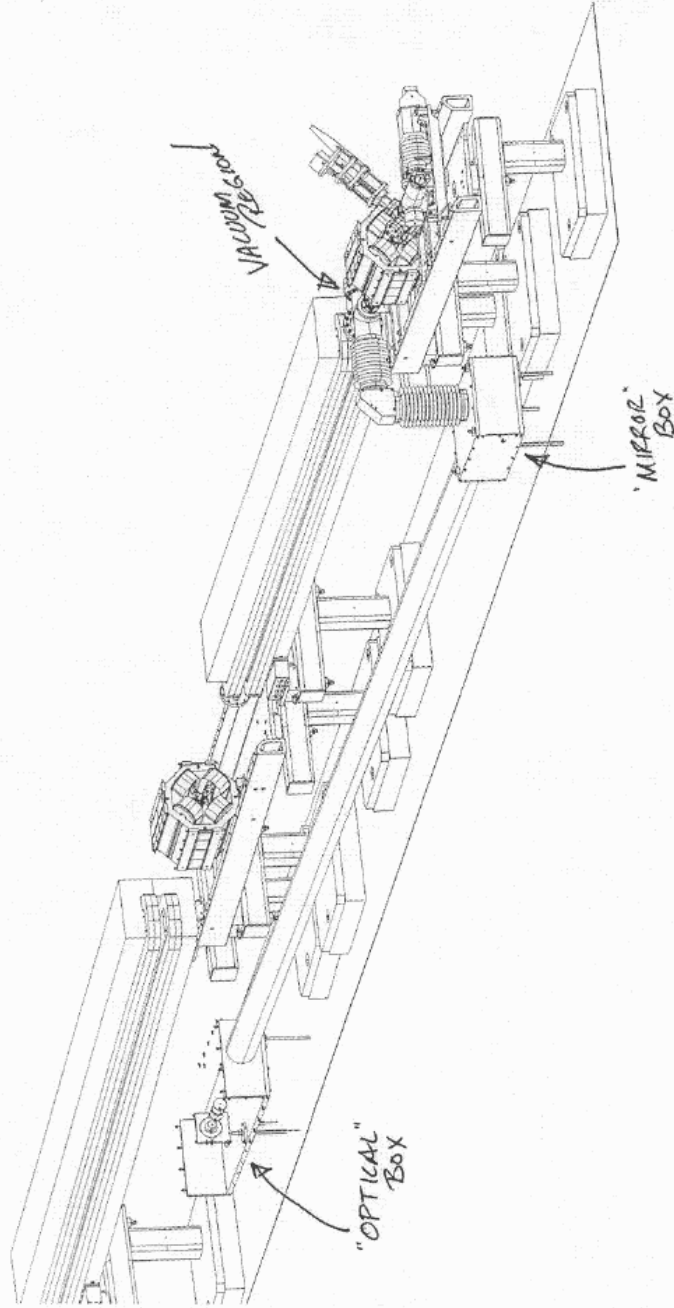


HIGH RESOLUTION SLM
@1K12

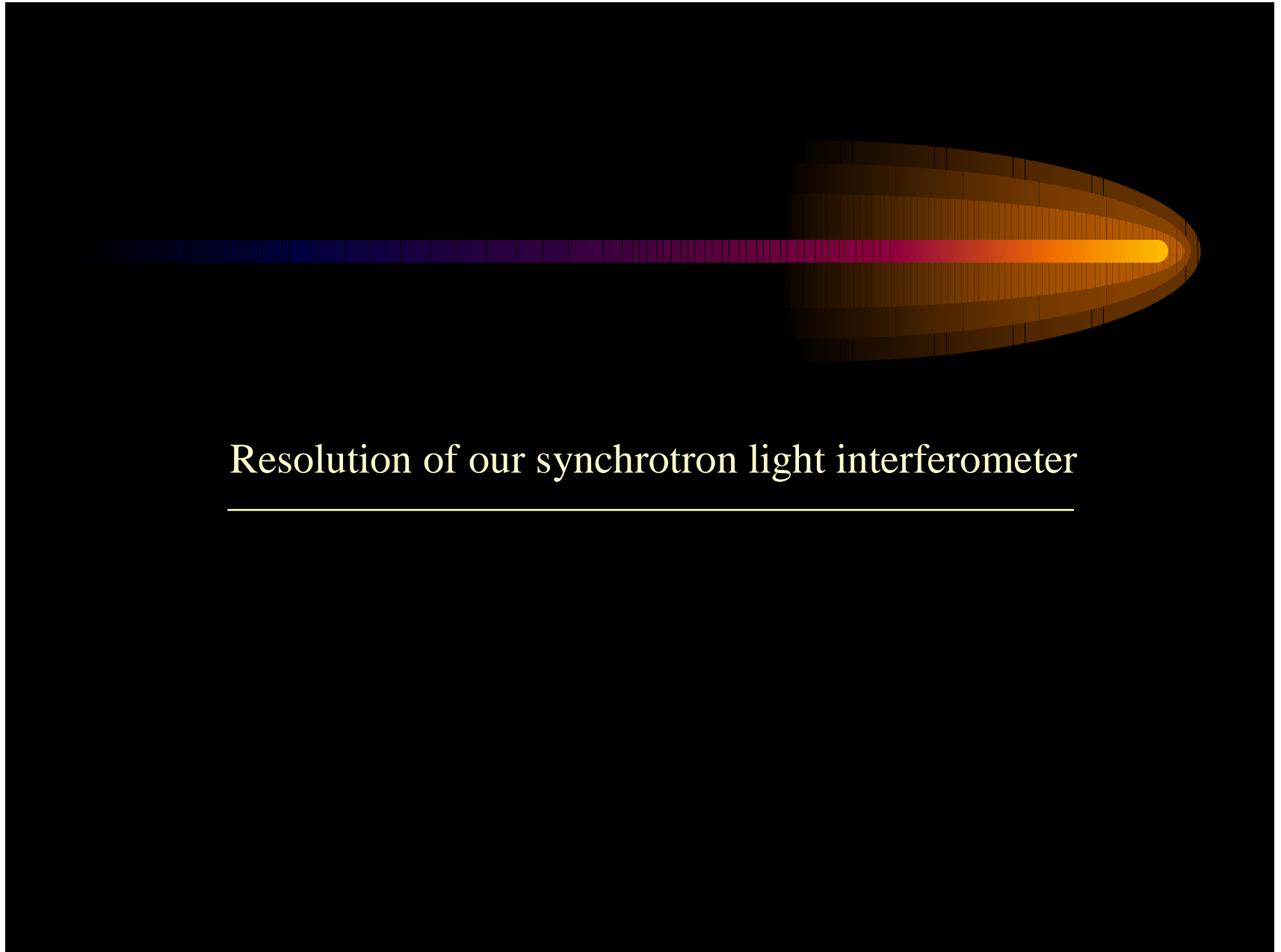






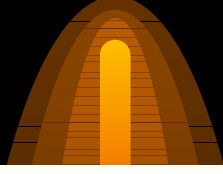
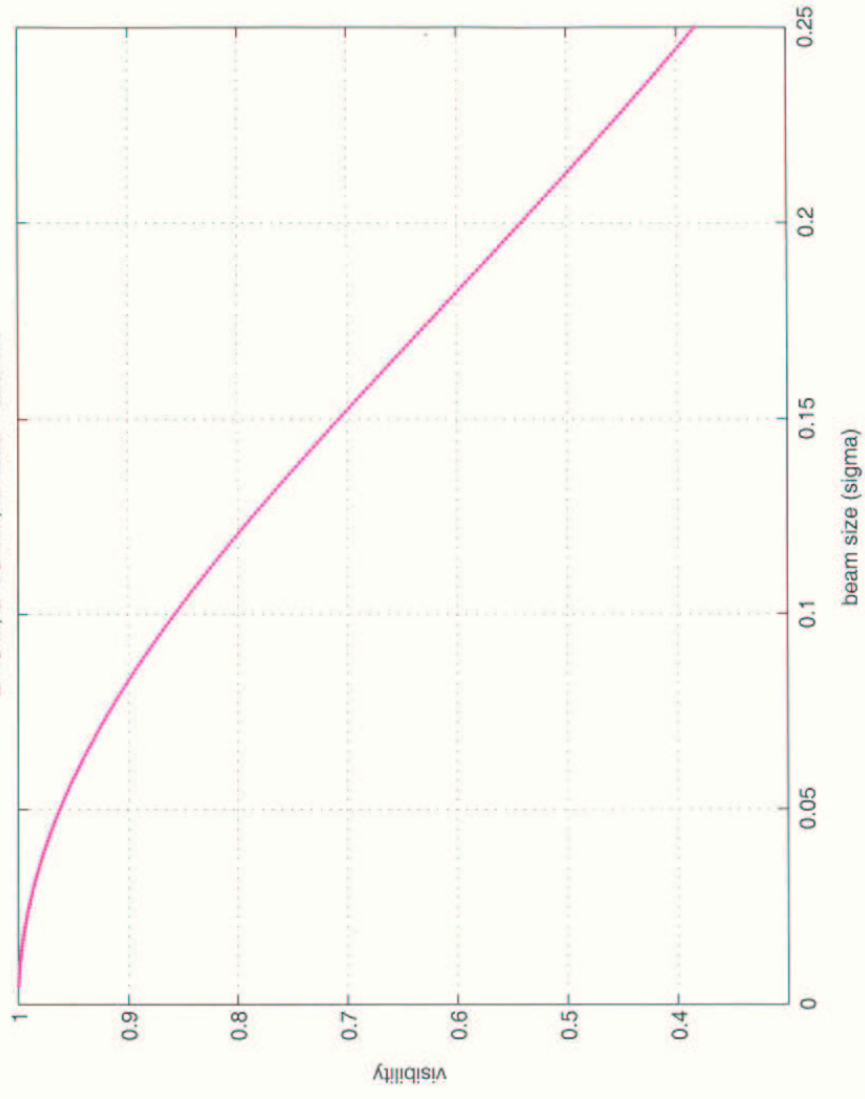


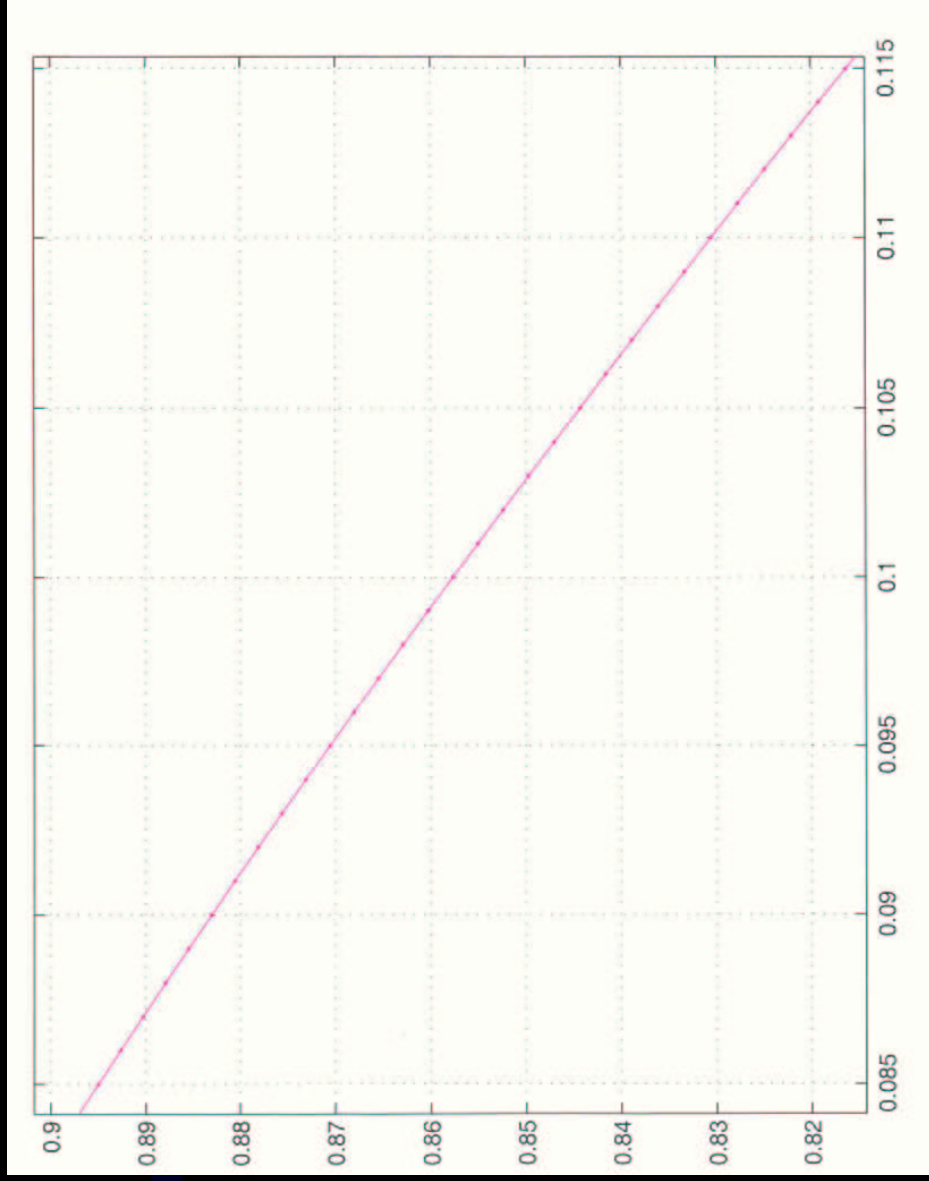
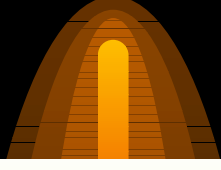
HIGH RESOLUTION SLM
@IC12



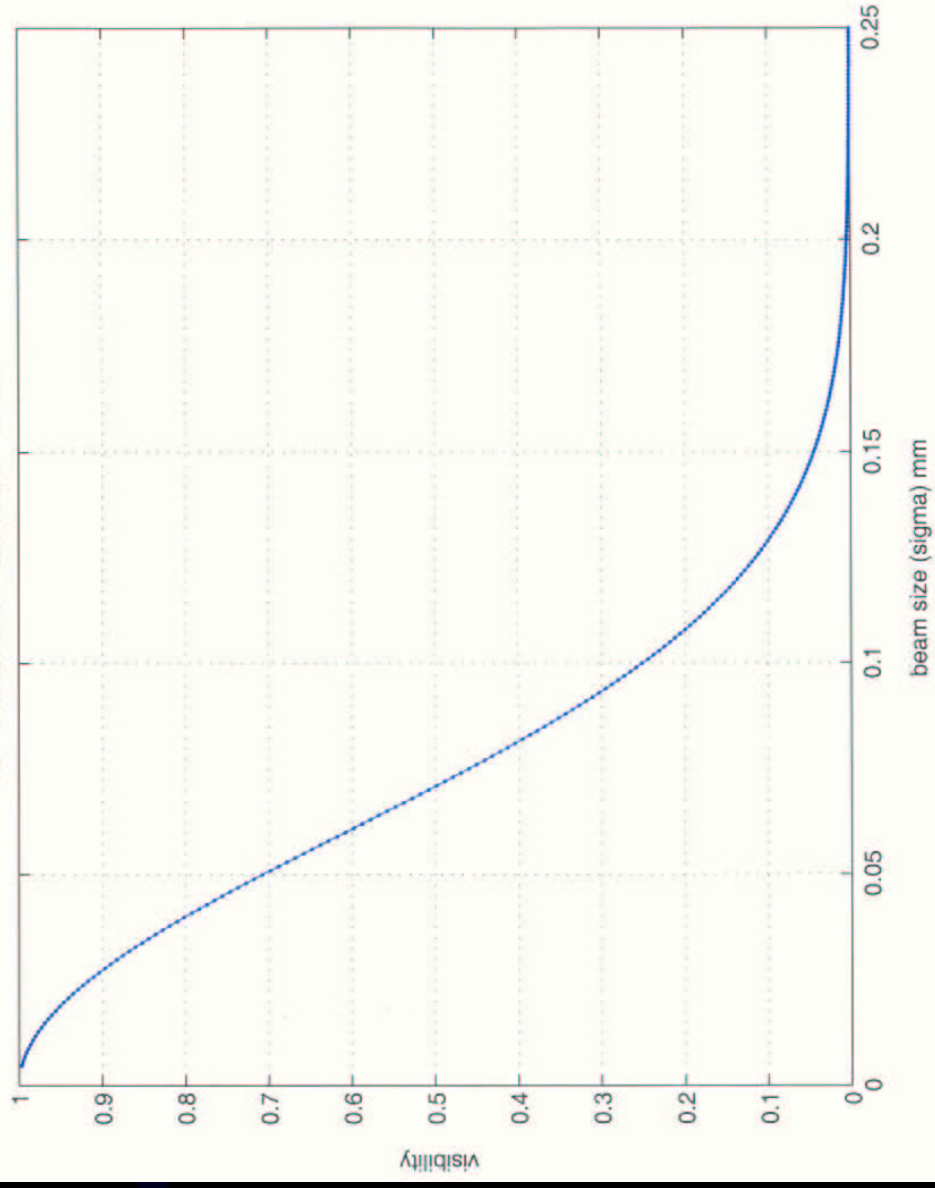
Resolution of our synchrotron light interferometer

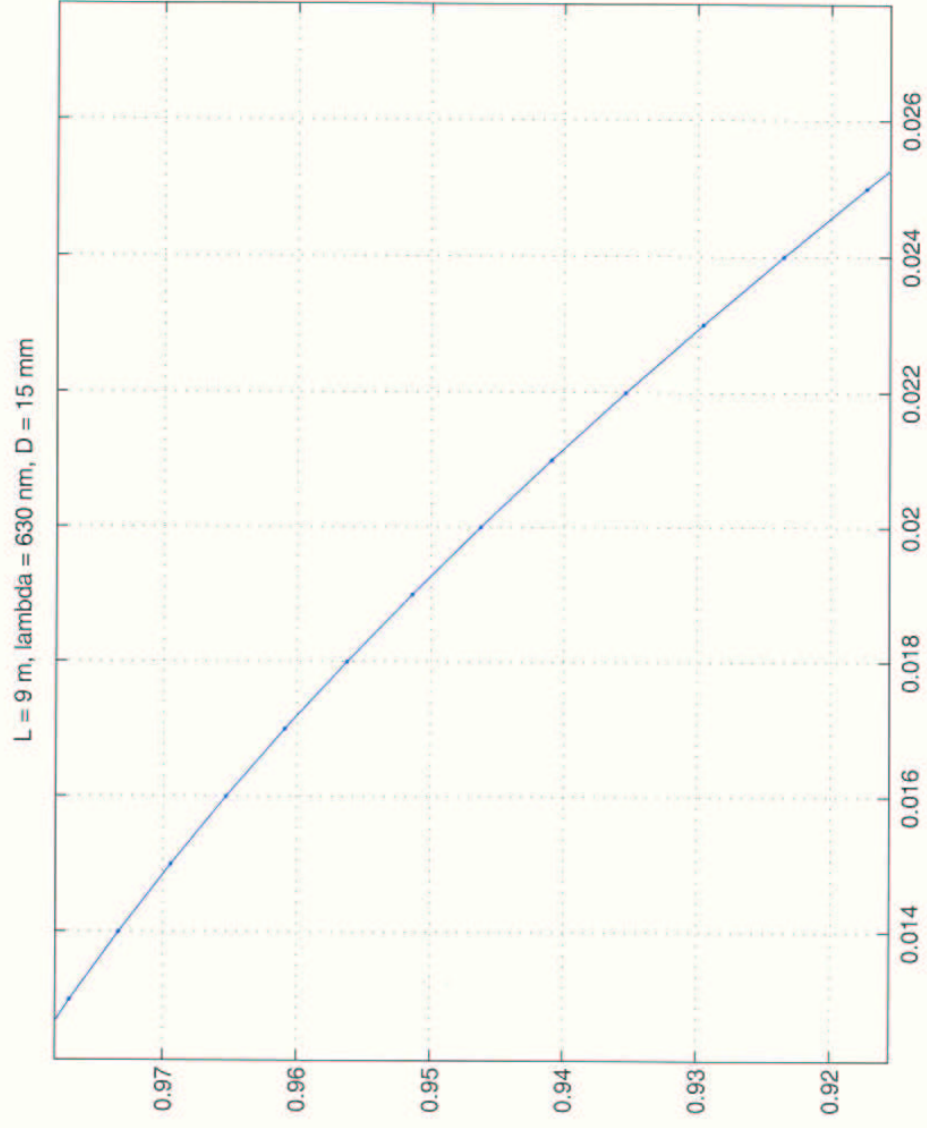
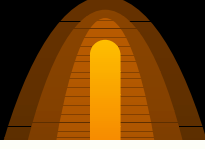
$L = 9 \text{ m}$, $D = 5 \text{ mm}$, $\lambda = 630 \text{ nm}$





$L = 9 \text{ m}$, $\lambda = 630 \text{ nm}$, $D = 15 \text{ mm}$



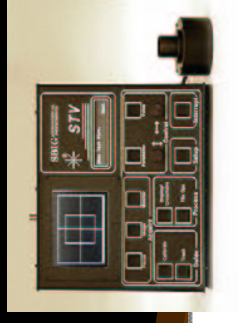
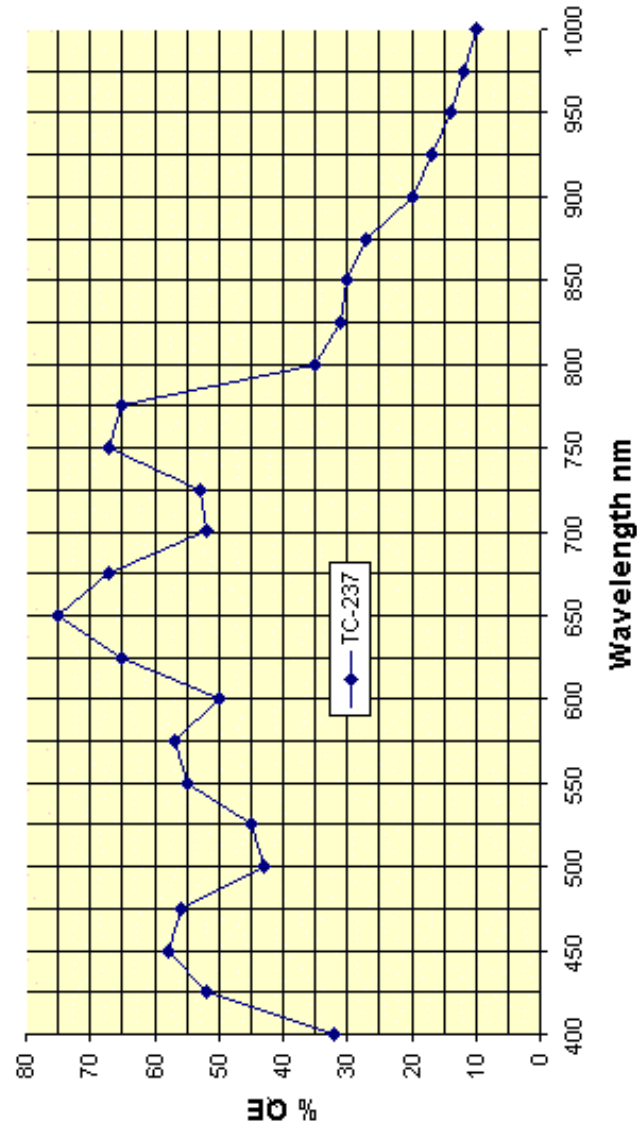




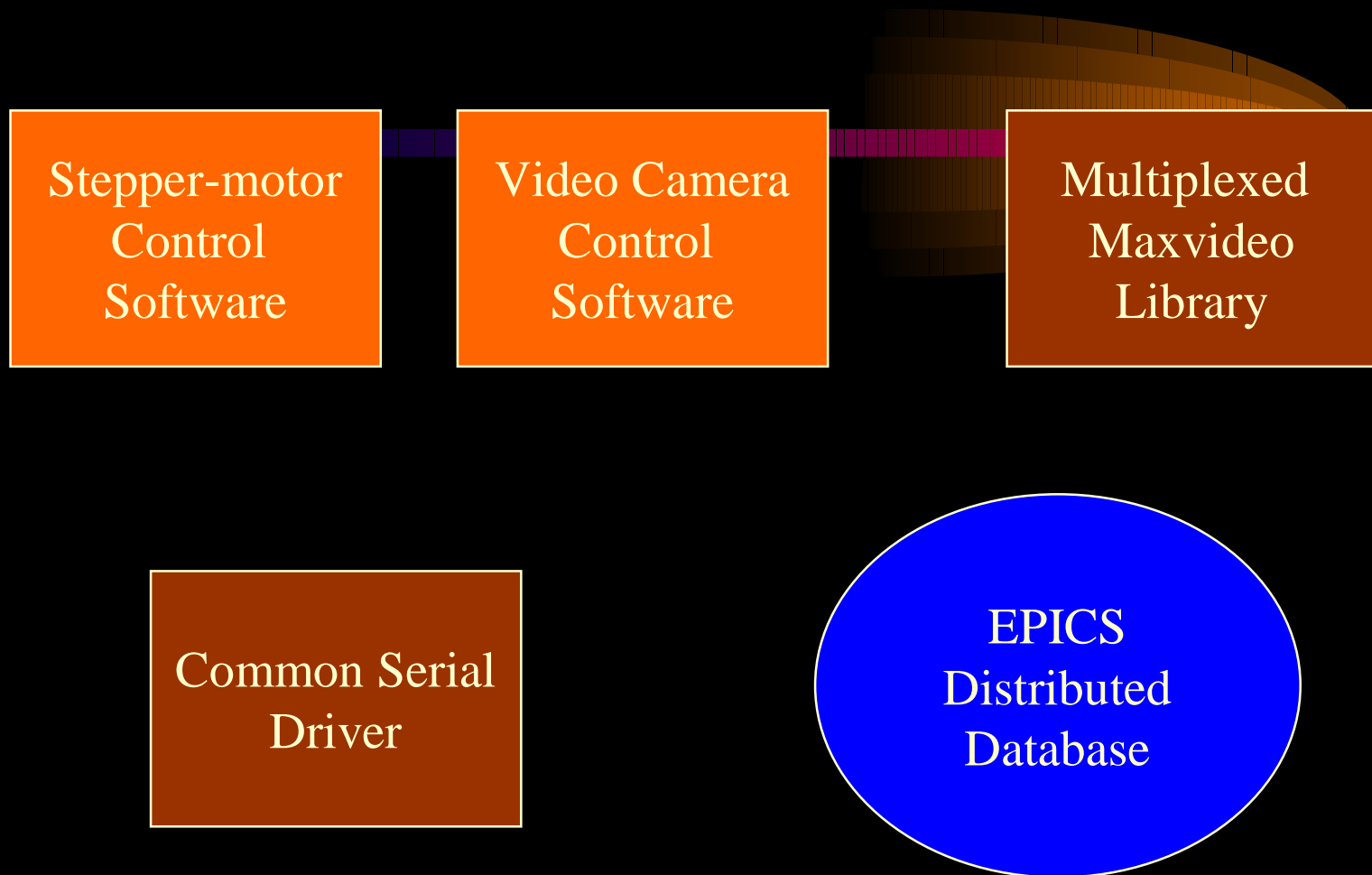
Our Synchrotron Light Interferometer

Main Control Components

Quantum Efficiency ST-237 / Pixel 237 / STV



Control Software Structure



DAQ_O_DataCube_1C12_slm.adl

(2002-04-15, Chevtsov)

DataCube Setup for Hall A 1C12 SLM - Multiplex

video

disabled

enabled

Video camera

Control

Diffraction

slit control

Current

0.016

microAmp

Units

mm

mm

X Position

251.8

X Width (rms)

59.1

Y Position

197.3

Y Width (rms)

122.9

Advanced

Display

Trouble

Rescue

Calibration screen

HALL A

Acquire Gain

1.000

1.0

LUT1 Mode

Subtract

LUT1 Threshold

65

Setup Scripts

!

Masks

enable mask

enable disp mask

MASK OUTSIDE

X1:

192

Y1:

2

X2:

385

Y2:

355

Saturated

2

Max Pixel

255

X profile

Y profile

ISR_O_synclightctrl.a

Synchrotron Light Monitor

Slit Control

Position 64500

Home

Pos 1

Pos 2

Pos 3

Pos 4

Moving

+ Limit

- Limit

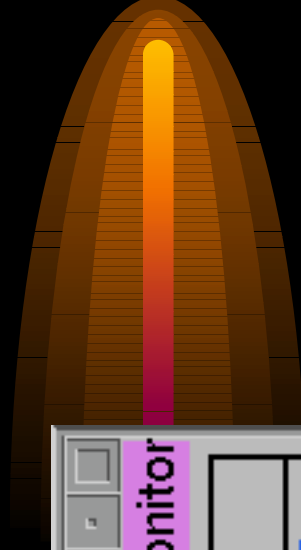
Move To 64500

Jog

<-

1000

->



STV CCD CAMERA

CONTROL PANEL

IMAGE Norm, Exp=2.0s
øBright Contrastø

focus

image

monitor

Acquire

parameter

left right

value

left right

Control

calibrate

track

Guide

display

fileops

Process

Interrupt

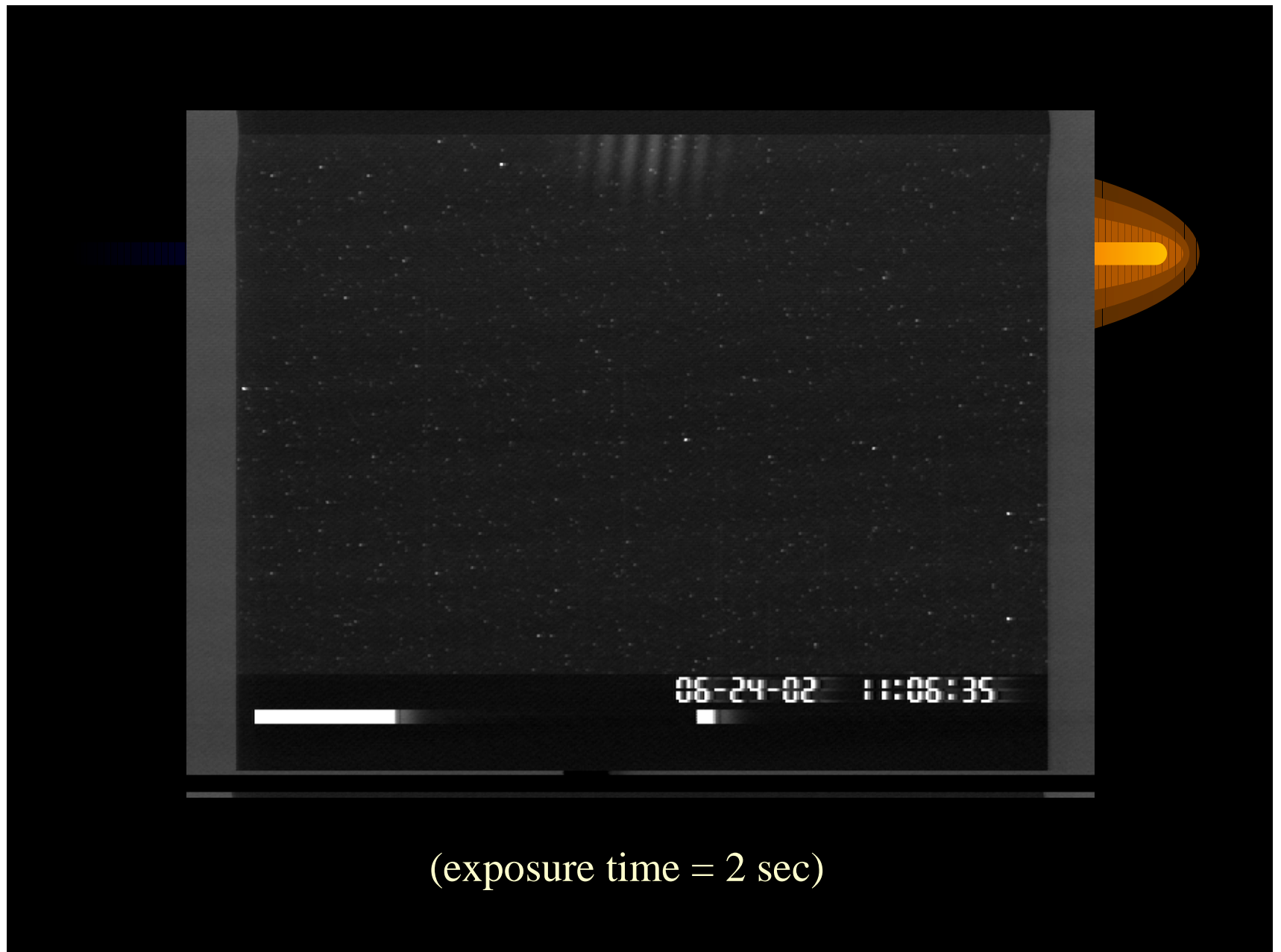
Interrupt

setup

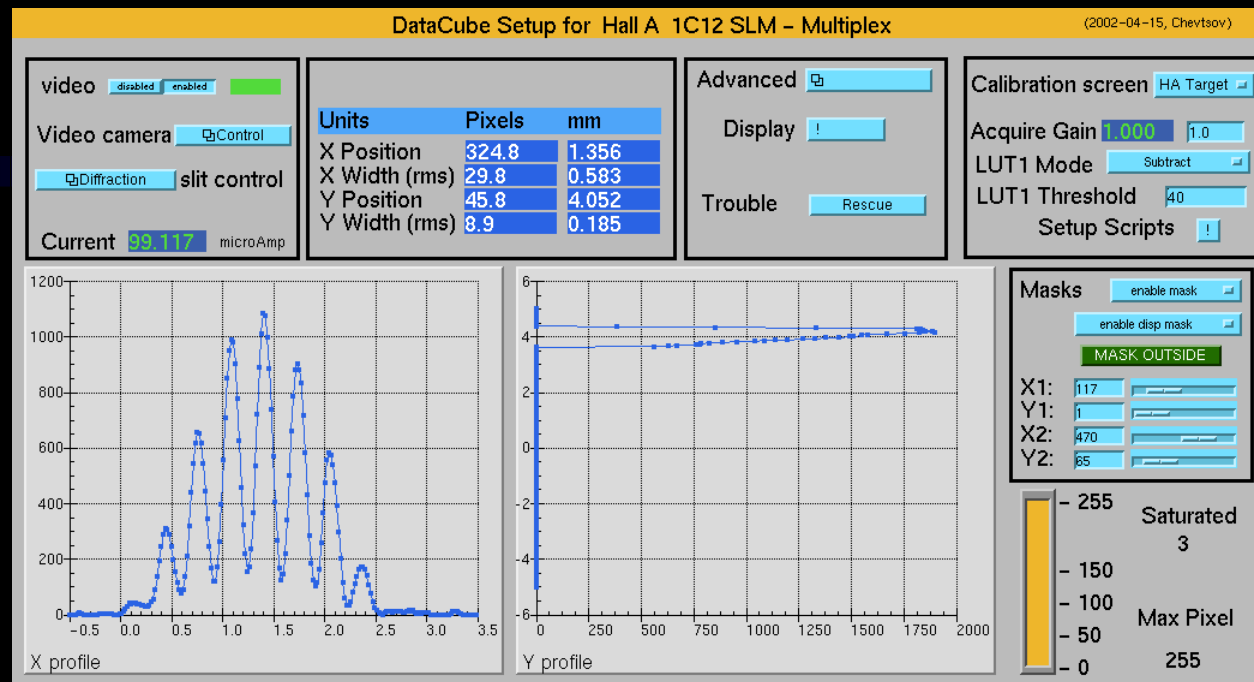
Setup



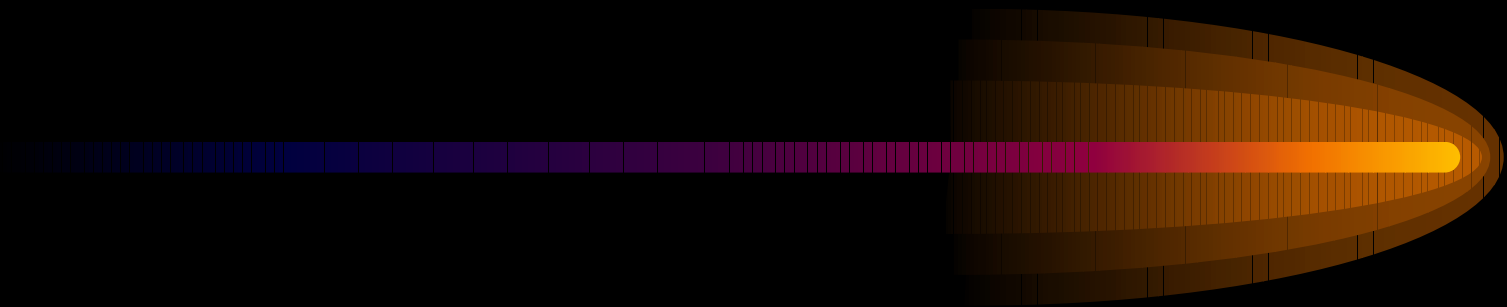
Very First Experimental Results



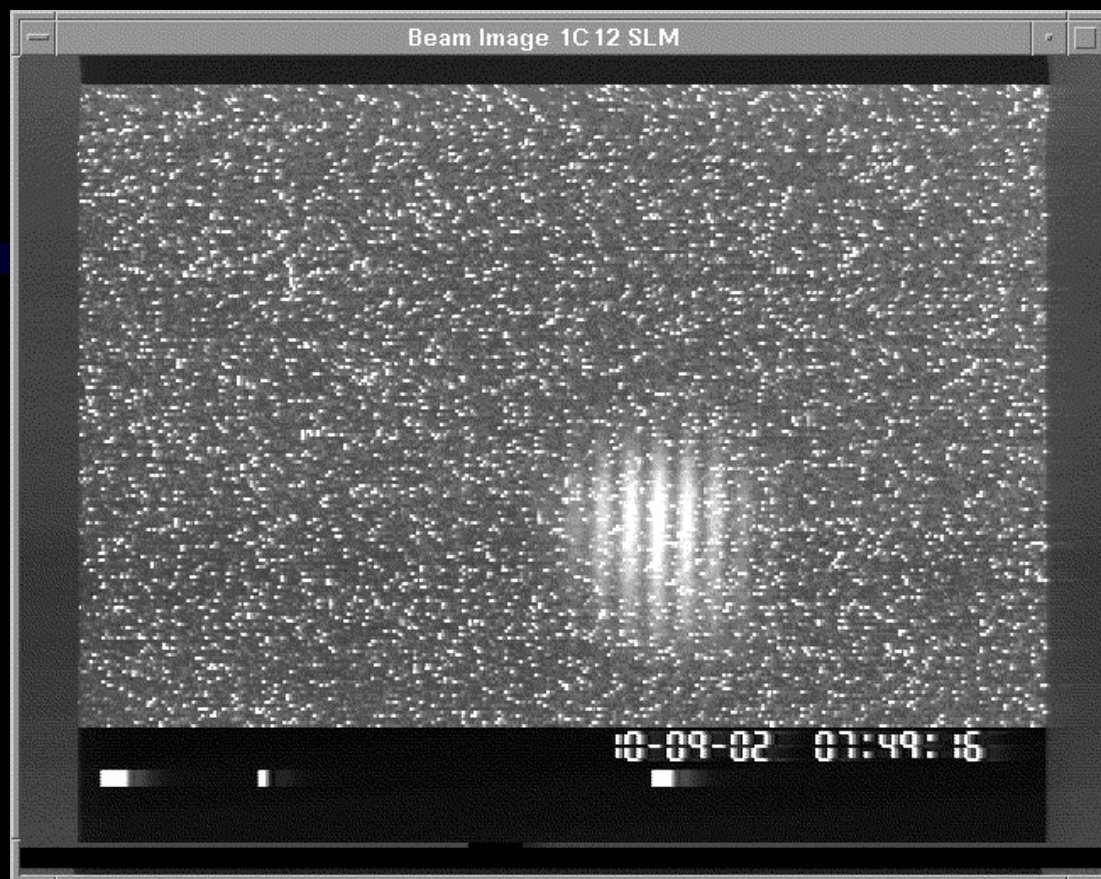
(exposure time = 2 sec)



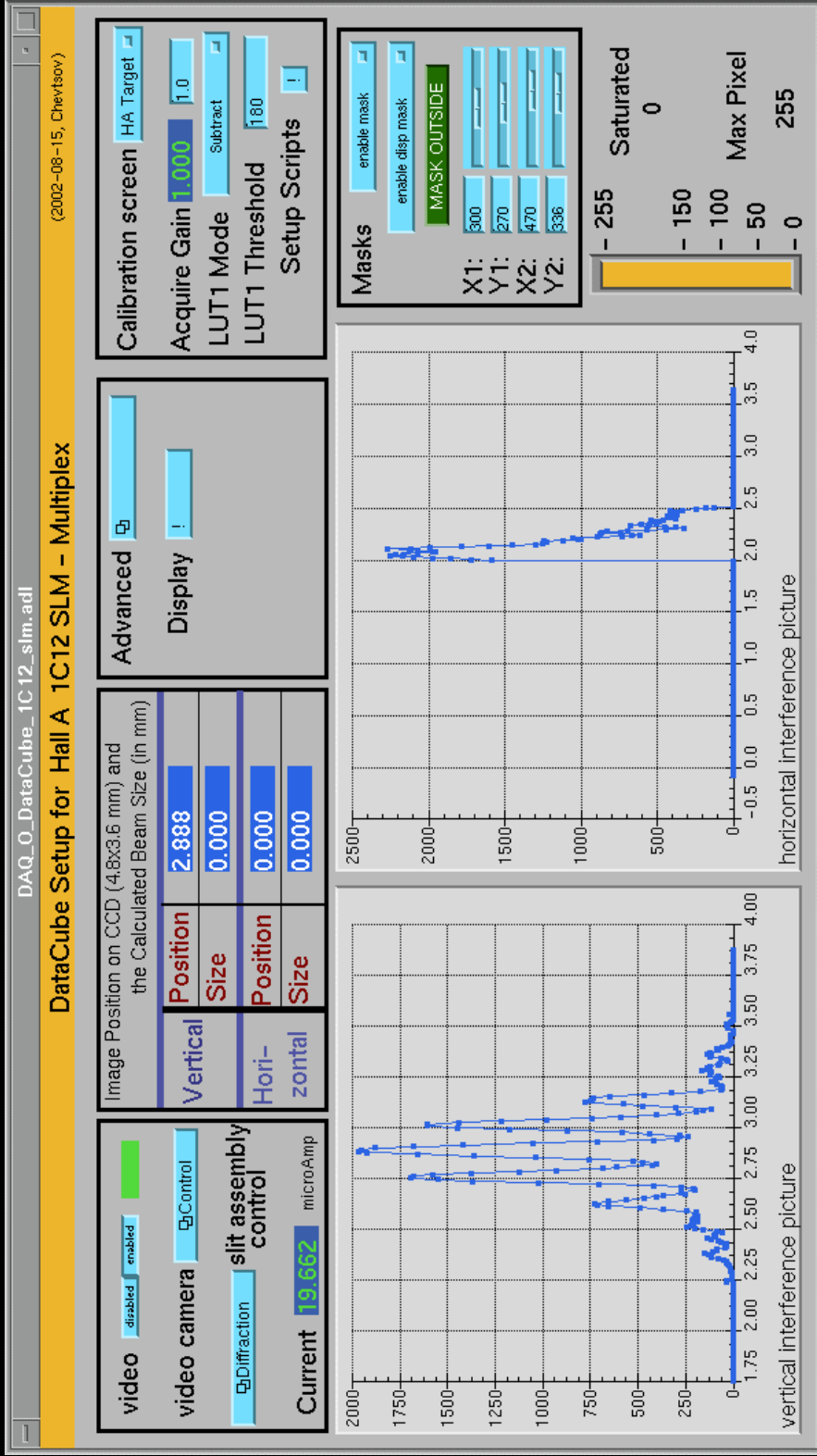
$$V = 0.8 \quad \sigma_S = 0.12 \text{ mm}$$

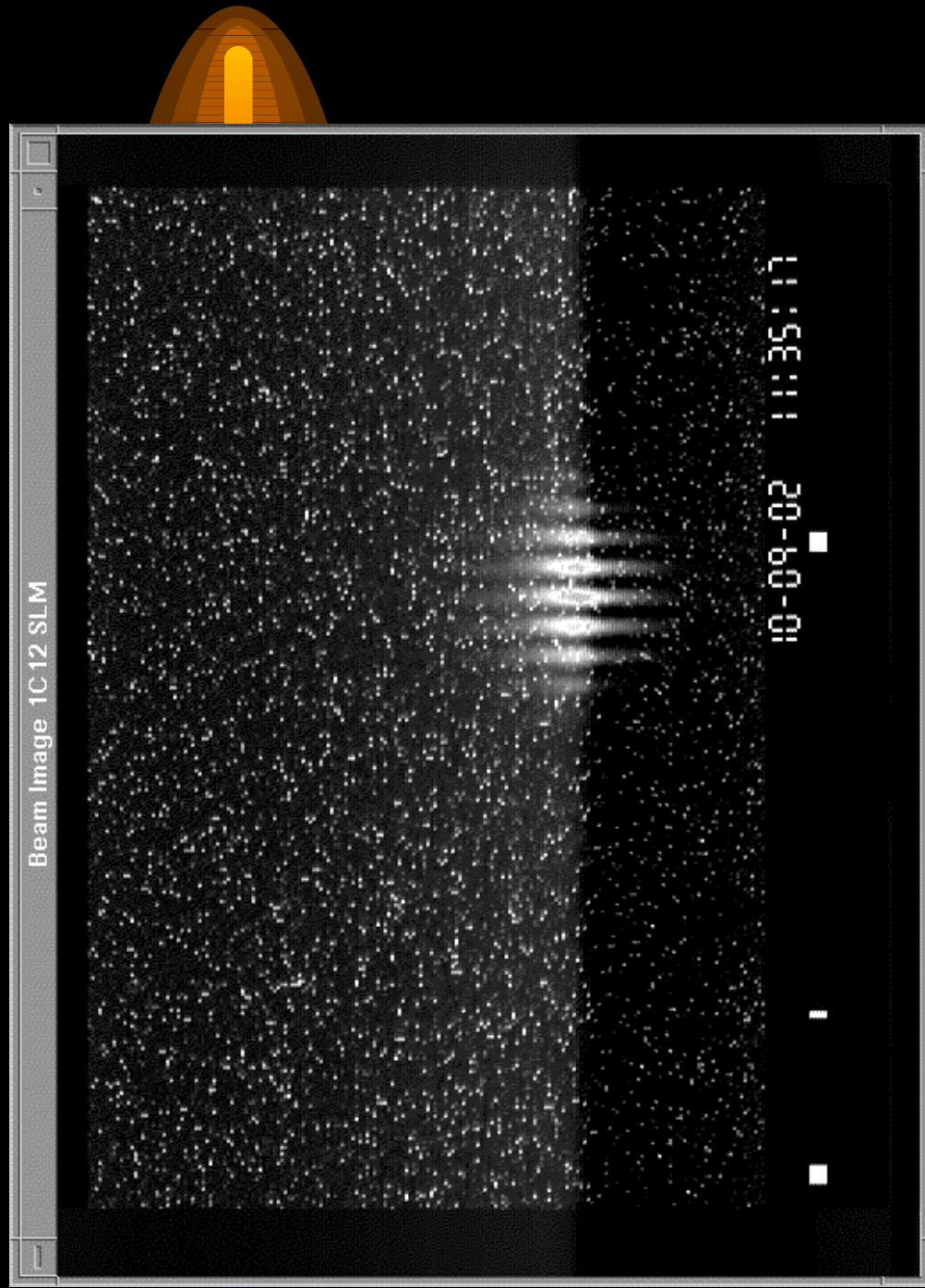


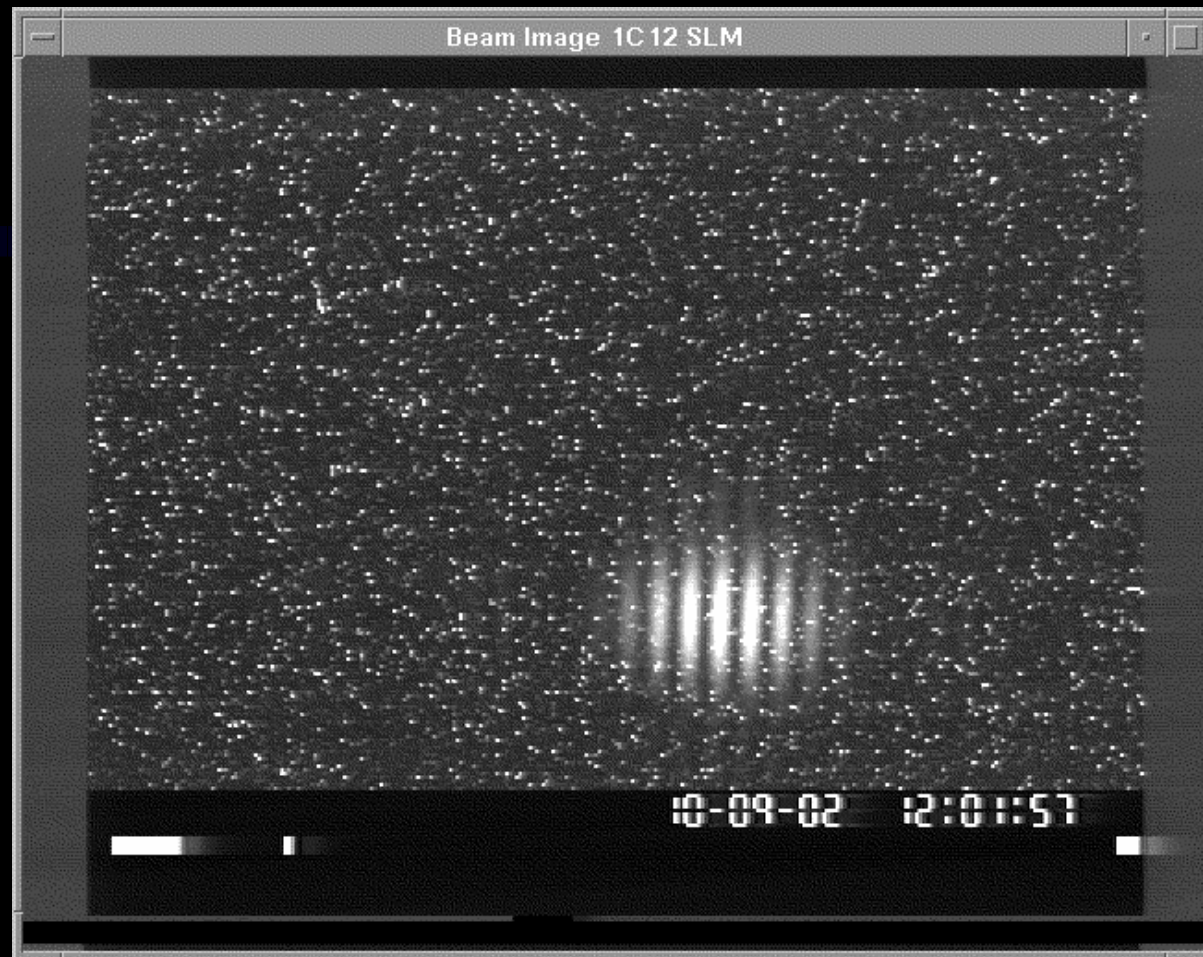
SLI Data After 2002 Summer Shutdown



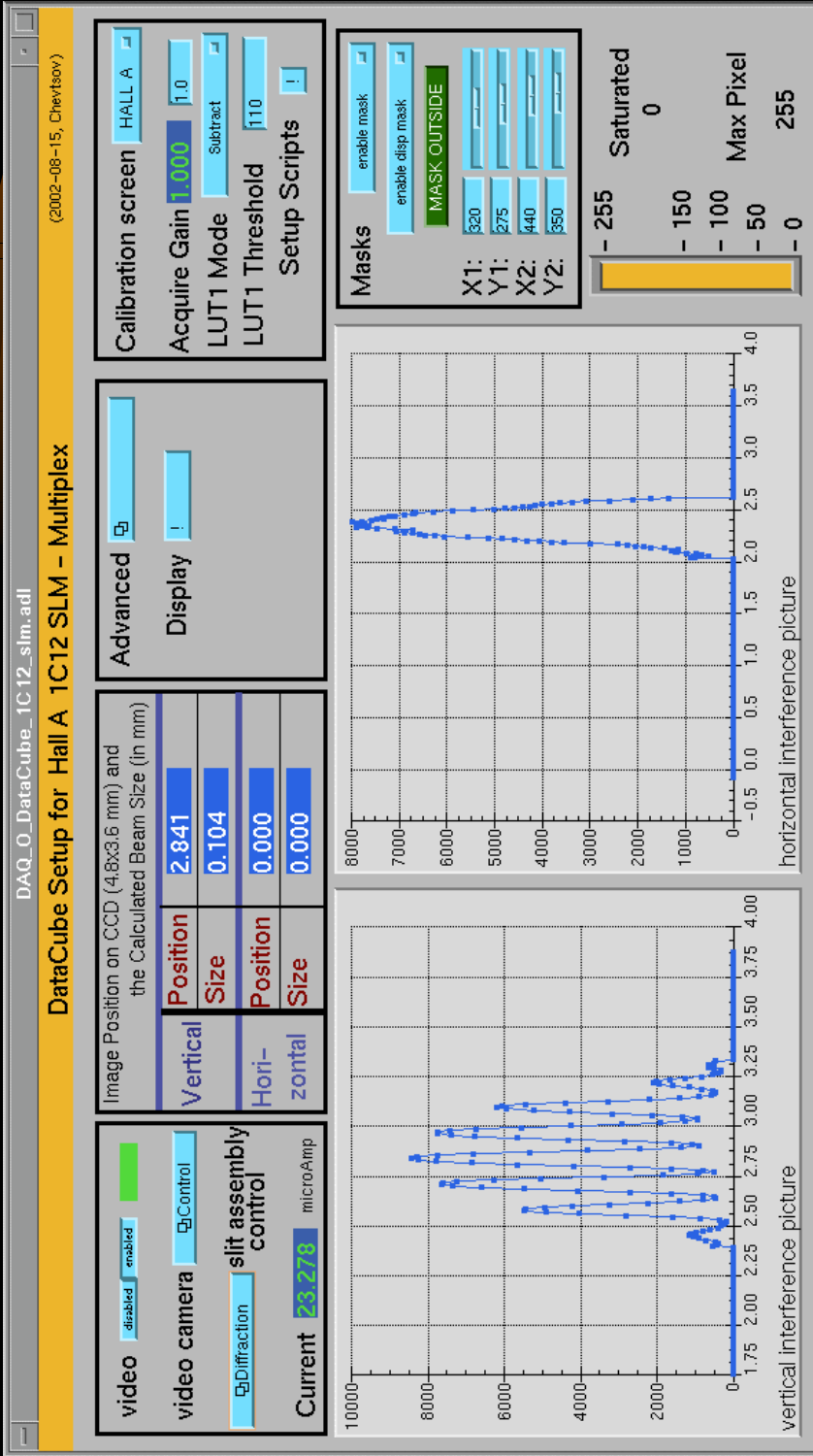
(exposure time = 50 sec)







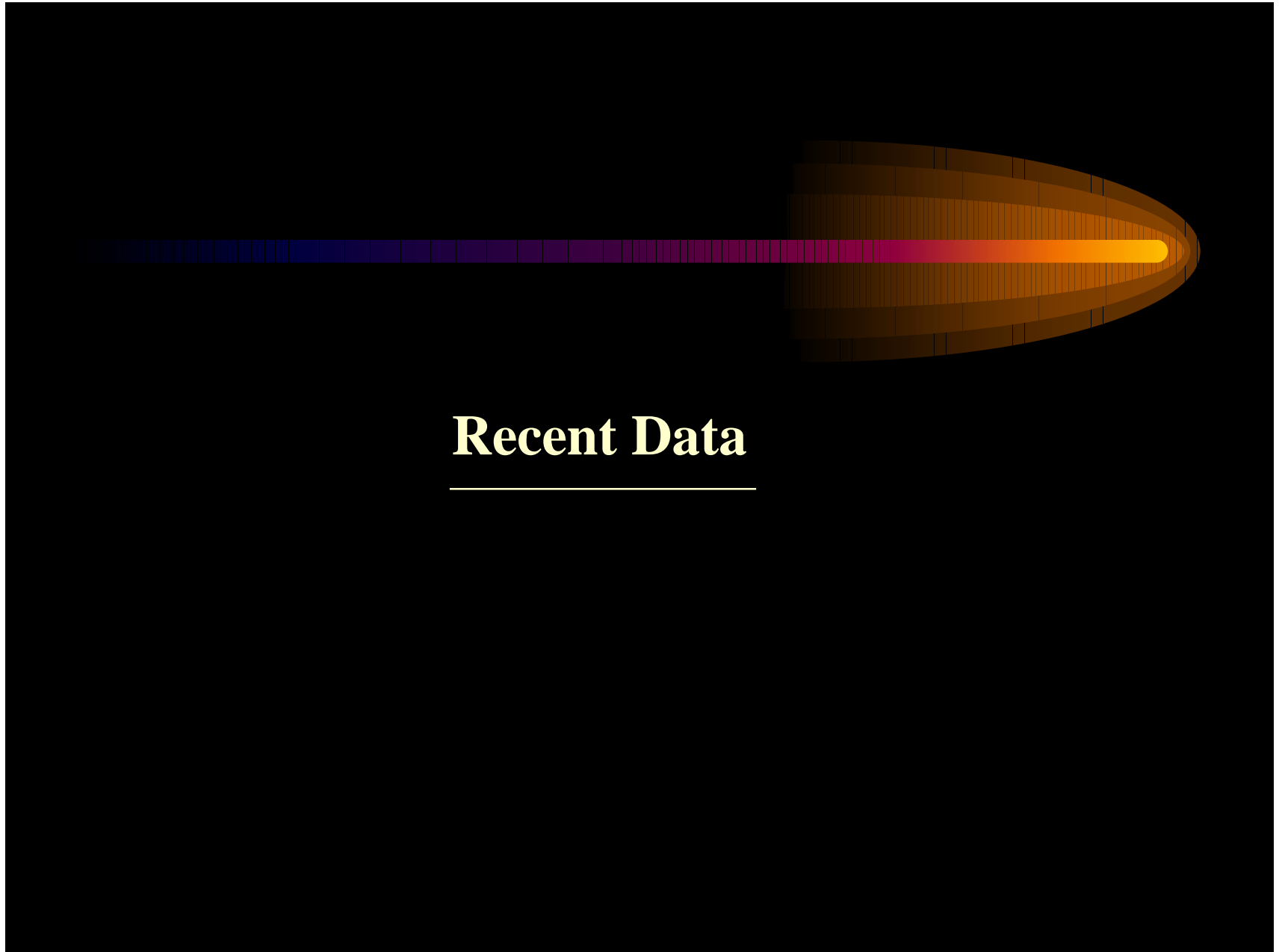
(exposure time = 10 sec)



From - Thu Oct 10 10:44:23 2002
Received: (from majordom@localhost)
by mailer.jlab.org (8.11.6/8.11.6) id g9ADBv915120;
Thu, 10 Oct 2002 09:11:57 -0400 (EDT)
Received: from jlab.org (localhost [127.0.0.1])
by mailer.jlab.org (8.11.6/8.11.6) with ESMTTP id g9ADBsx15113;
Thu, 10 Oct 2002 09:11:55 -0400 (EDT)
Message-ID: <3DA57C9A.7C97CC1A@jlab.org>
Date: Thu, 10 Oct 2002 09:11:54 -0400
From: Jay Benesch <benesch@jlab.org>
X-Mailer: Mozilla 4.78 [en] (X11; U; HP-UX B.10.20 9000/785)
X-Accept-Language: en
MIME-Version: 1.0
To: machine-ops@jlab.org
Subject: 8am mtg 10/10/02
Content-Type: text/plain; charset=us-ascii
Content-Transfer-Encoding: 7bit
Sender: owner-machine-ops@jlab.org
Precedence: bulk
Reply-To: Jay Benesch <benesch@jlab.org>

Day SHIFT SUMMARY

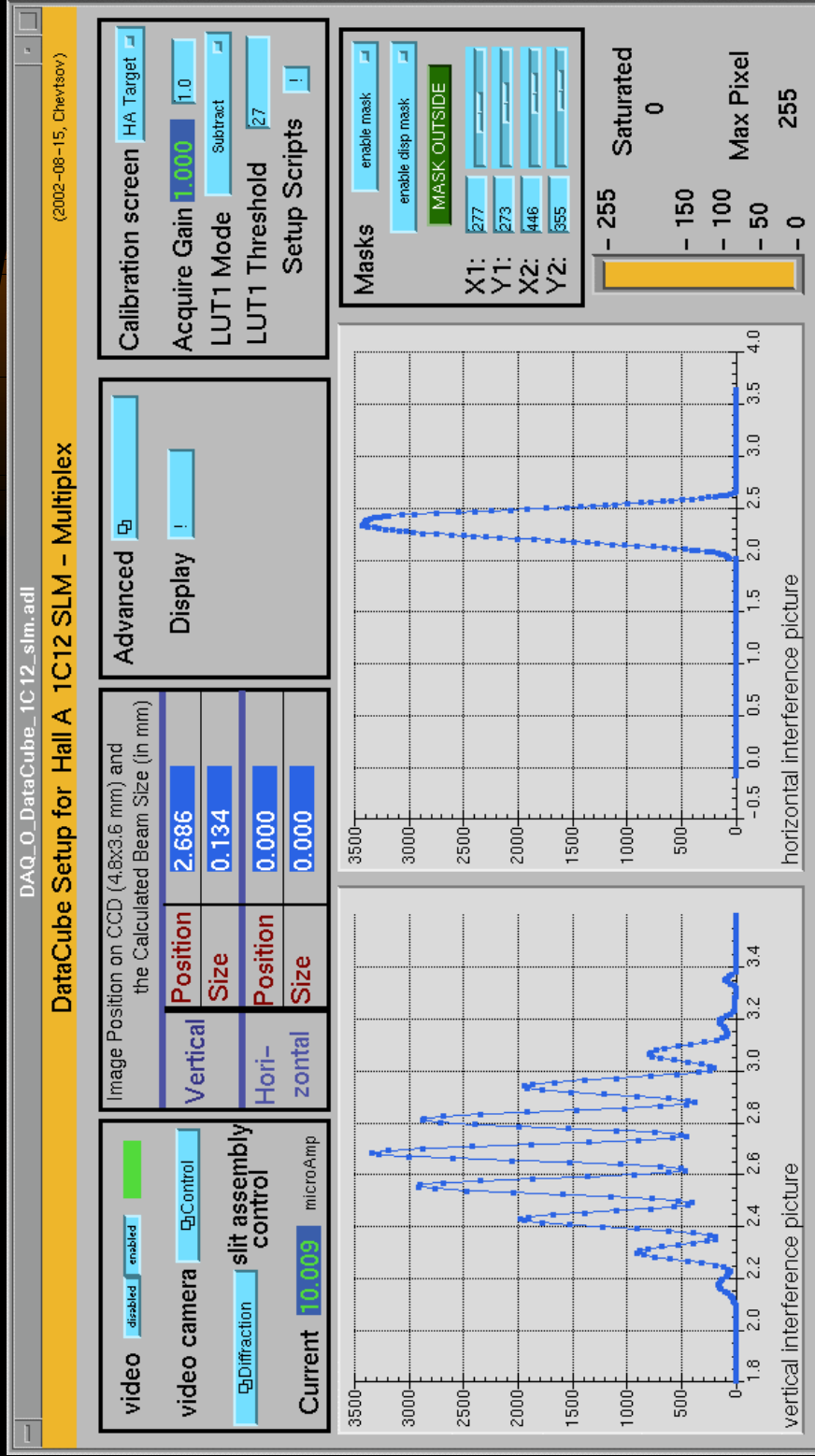
Shift began with beam delivery to both halls. At 10:00 we terminated beam delivery to the halls to do a spot move, repair Fast Feedback, and send CW G0 beam to the BSY dump. All of these things were achieved :) Spot move increased A current to ~24uA. FFB restored by returning missing trim cards. Steered ~12uA CW G0 beam to BSY dump. G0 beam delivery continued in parallel with delivery to halls A and B.

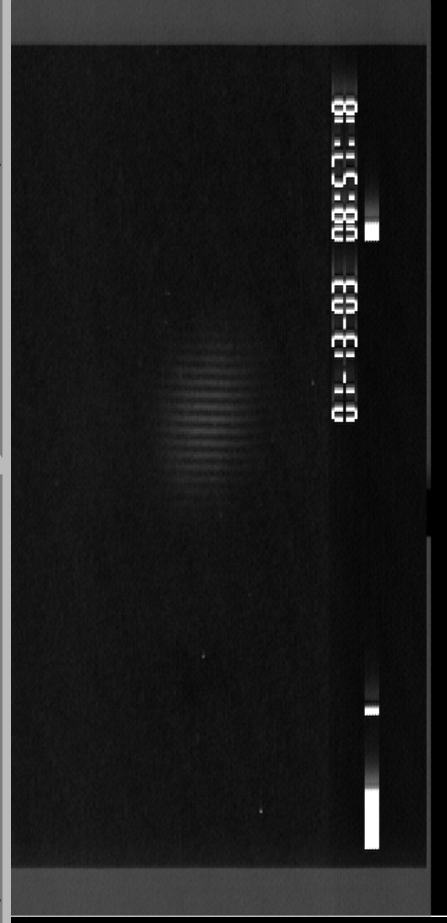
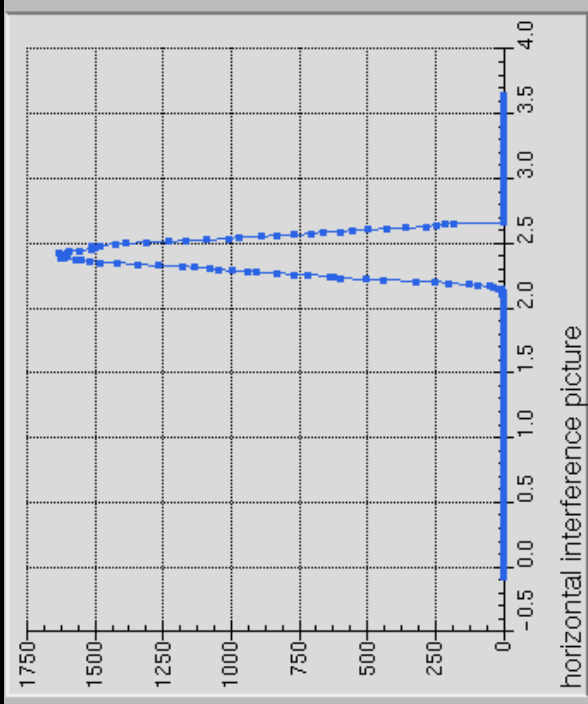
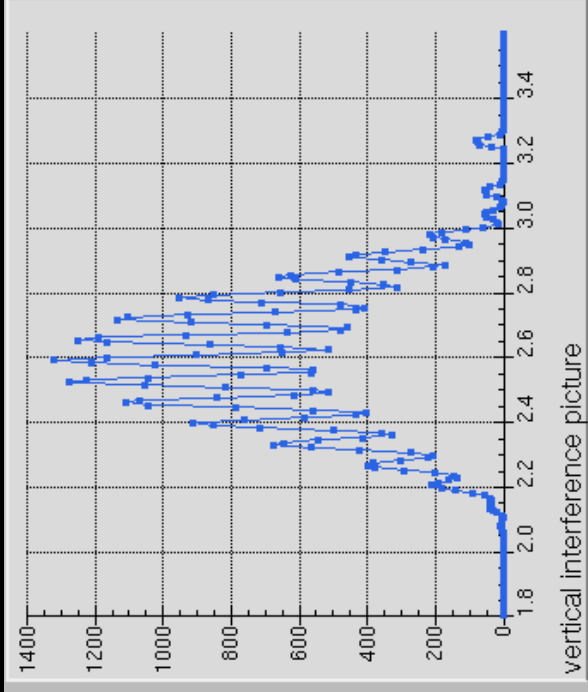


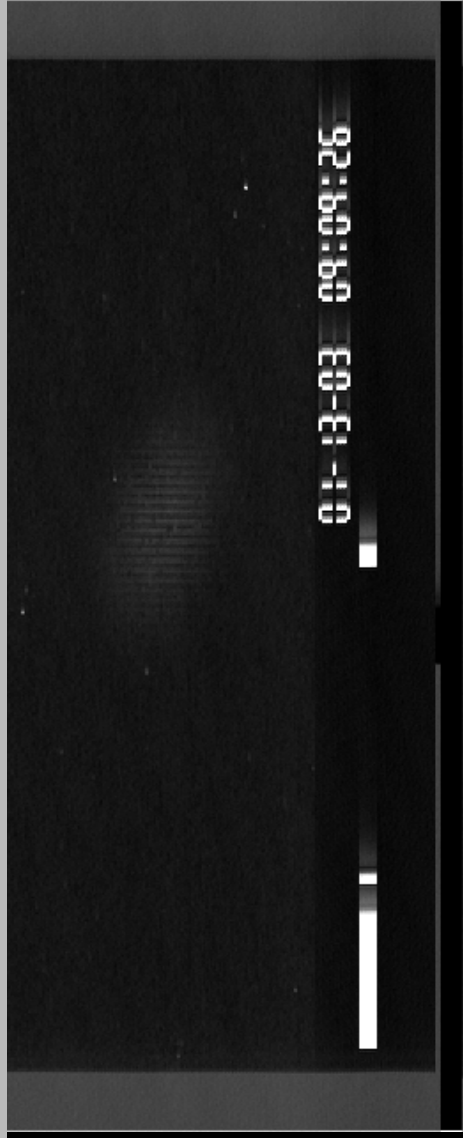
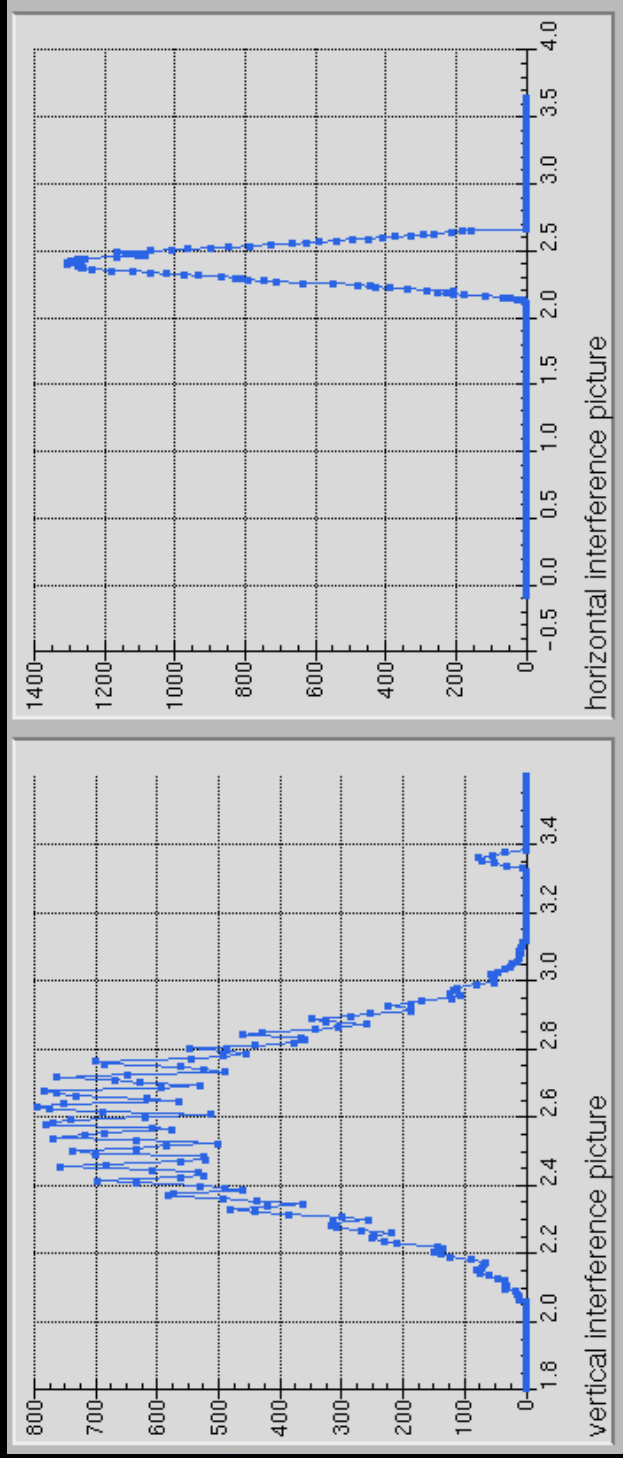
Recent Data



(exposure time = 15 sec)

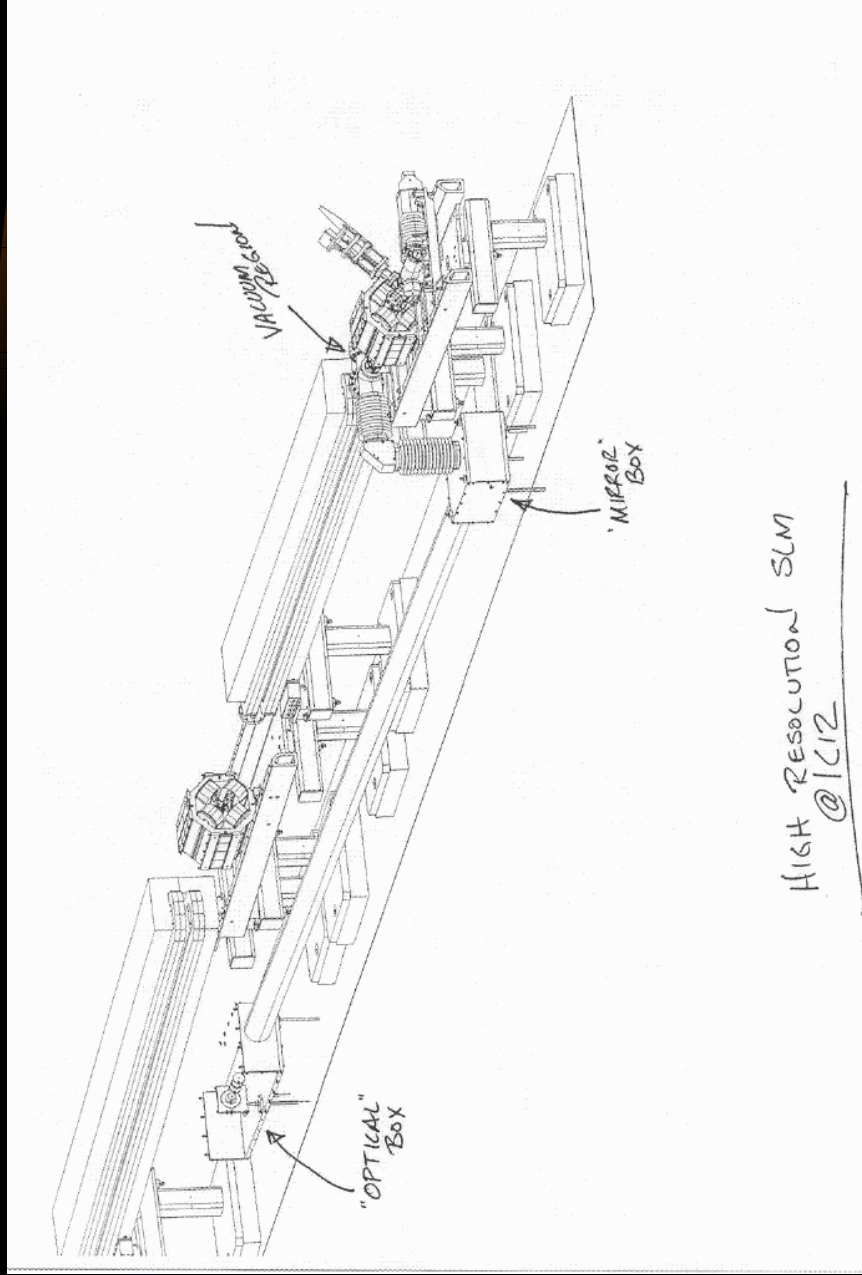








Very Last Data



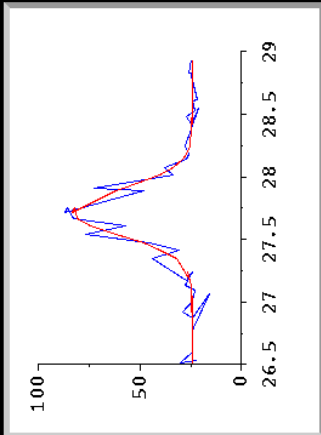
HIGH RESOLUTION SLM
@K12

Quadrupoles for the 1C Region

STATUS	EXCH	ADJUST	RESET	MAGNET NAME	HYSTERESIS LOOP SWITCH	INTEGRATED FIELD SET POINT DIPOLE UNITS IN GAUSS-CM QUADRUPOLE UNITS IN GAUSS SEXTUPOLE UNITS IN GAUSS-CM	CURRENT SETPOINT (amps)	CURRENT READBACK (amps)	STATUS
●	●	●	●	MQA1C01	● On Off	32991.699	3.065	3.063	●
●	●	●	●	MQA1C02	● On Off	-53771.199	-5.495	-5.494	●
●	●	●	●	MQA1C03	● On Off	33732.102	3.139	3.137	●
●	●	●	●	MQA1C04	● On Off	40372.398	3.800	3.798	●
●	●	●	●	MQA1C05	● On Off	-21106.400	-2.249	-2.248	●
●	●	●	●	MQA1C06	● On Off	2735.050	0.091	0.089	●
●	●	●	●	MQA1C07	● On Off	-18061.000	-1.950	-1.949	●
●	●	●	●	MQA1C08	● On Off	25156.598	2.291	2.286	●
●	●	●	●	MQA1C09	● On Off	0.000	-0.177	-0.178	●
●	●	●	●	MQA1C10	● On Off	0.000	-0.177	-0.178	●
●	●	●	●	MQA1C11	● On Off	-20419.801	-2.182	-2.181	●
●	●	●	●	MQA1C12	● On Off	40953.801	3.858	3.854	●
●	●	●	●	MQA1C13	● On Off	-17858.699	-1.930	-1.929	●
●	●	●	●	MQA1C14	● On Off	0.000	-0.177	-0.177	●
●	●	●	●	MQA1C15	● On Off	0.000	-0.177	-0.178	●
●	●	●	●	MQA1C16	● On Off	22431.900	2.022	2.018	●
●	●	●	●	MQA1C17	● On Off	-13819.199	-1.533	-1.533	●
●	●	●	●	MQA1C18	● On Off	13867.000	1.192	1.190	●
●	●	●	●	MQA1C19	● On Off	-50556.801	-5.172	-5.172	●
●	●	●	●	MQA1C20	● On Off	41559.500	3.918	3.918	●
●	●	●	●	MQA1H01	● On Off	-6500.000	-0.815	-0.815	●
●	●	●	●	MQA1H04	● On Off	4081.280	0.222	0.215	●
●	●	●	●	MQA1H04A	● On Off	0.000	-0.177	-0.178	●

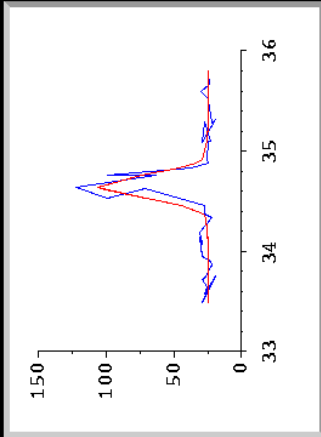
This screen is generated from the routine ..\screen_codes\magnets\magpanel.c V3.64 (Green, 2002-09-16)

Horizontal Profile



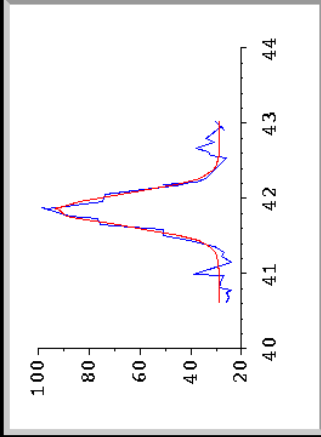
Sigma(mm) [0.19] RMS(mm) [0.61]
Position [27.72] Centroid [27.71]

X-Y Coupling Profile



Sigma(mm) [0.11] RMS(mm) [0.59]
Position [34.65] Centroid [34.63]

Vertical Profile



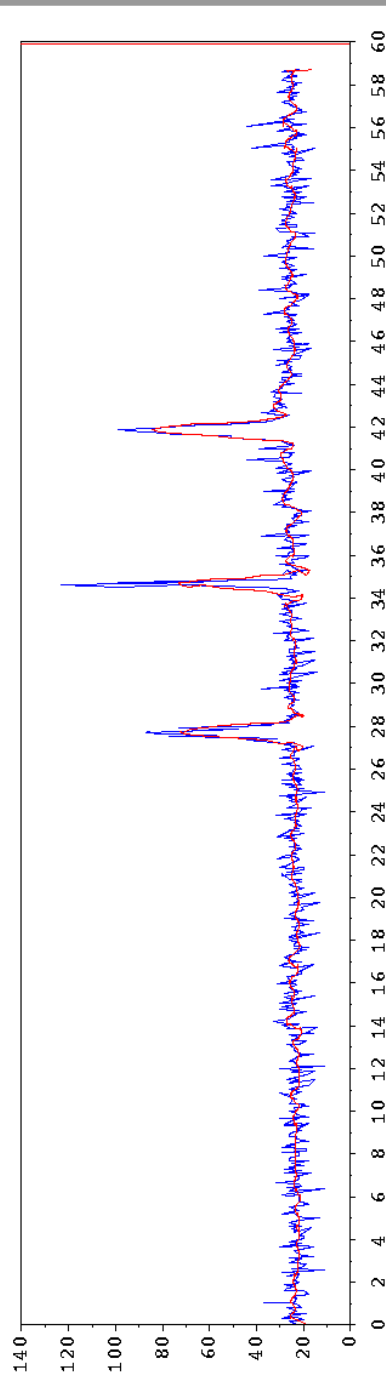
Sigma(mm) [0.20] RMS(mm) [0.61]
Position [41.85] Centroid [41.84]

Select Harp IHA1101 ☐

***Cycle Harp**

Transfer Profile

IHA1C12 Feb 11, 2003 10:23:07.1700 Scan Complete



LPOff

LP05

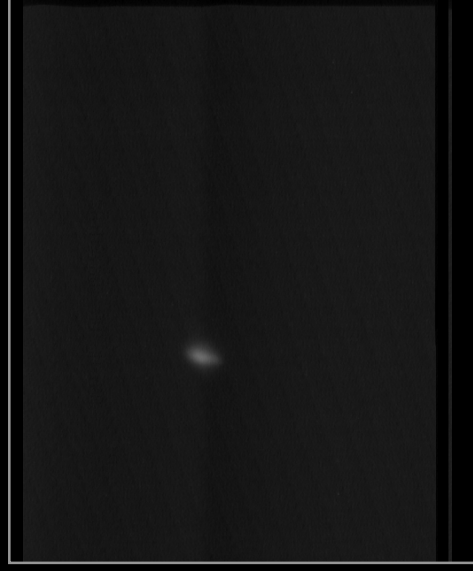
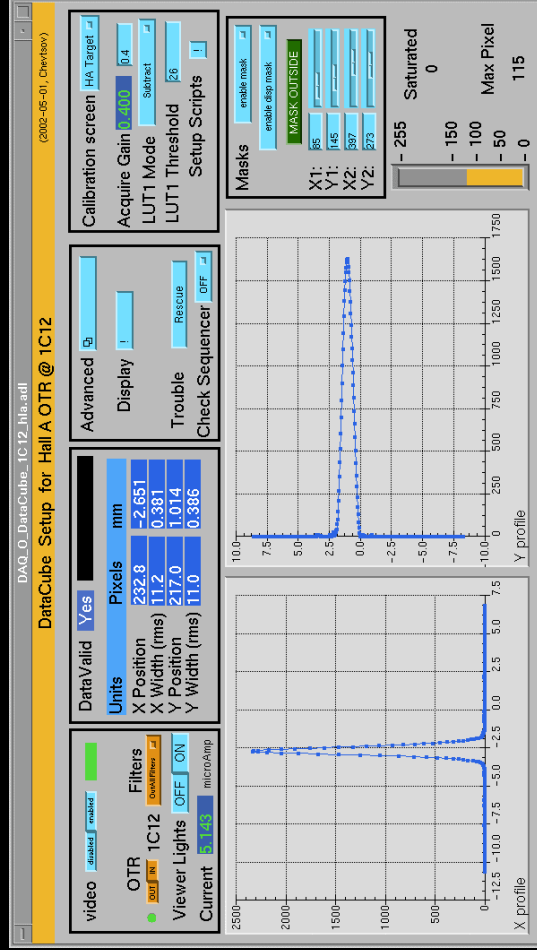
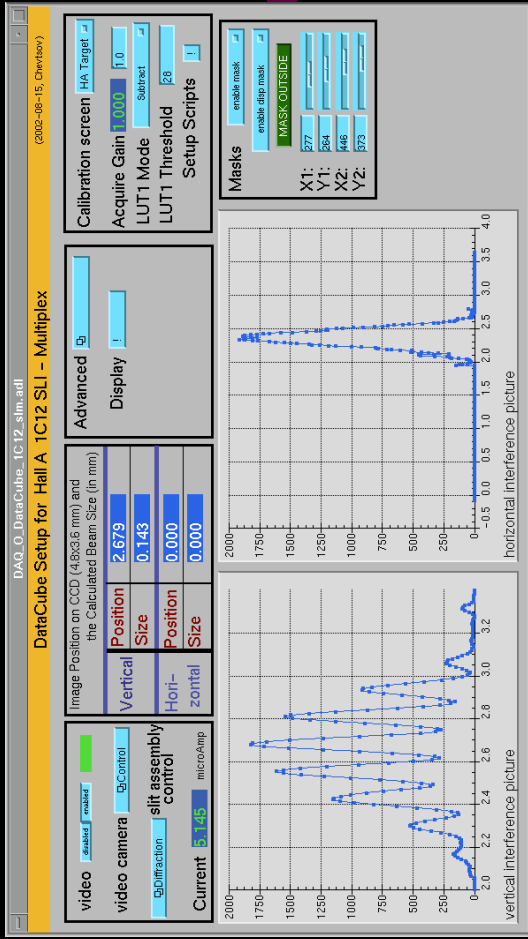
LP10

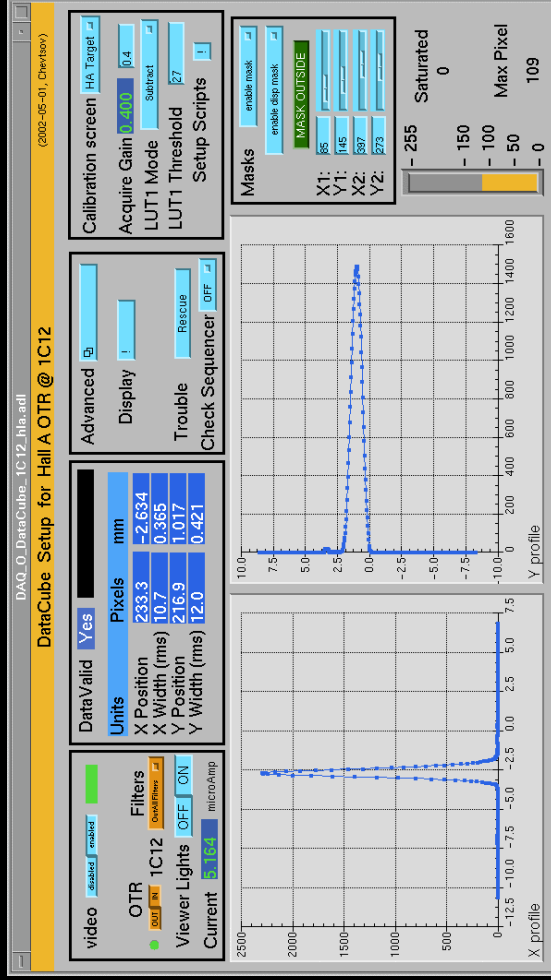
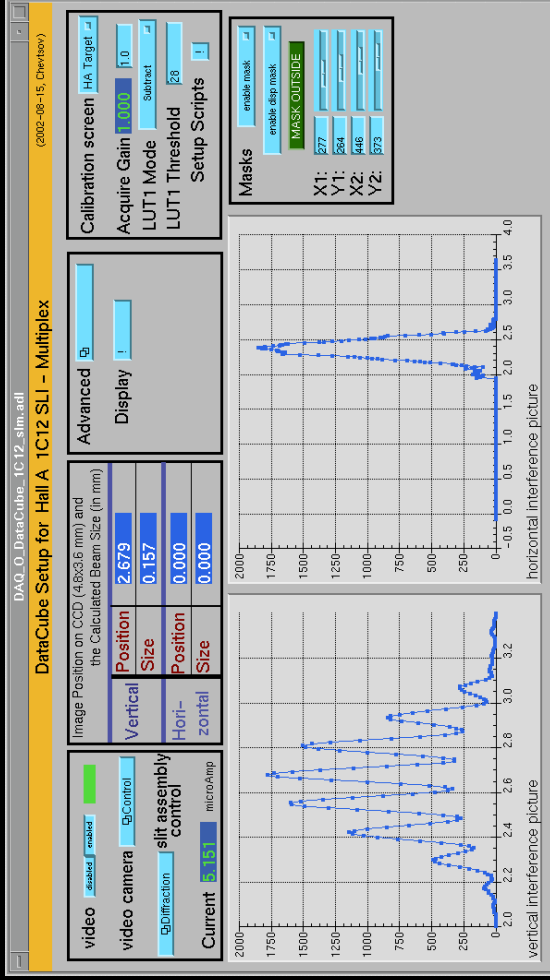
LP20

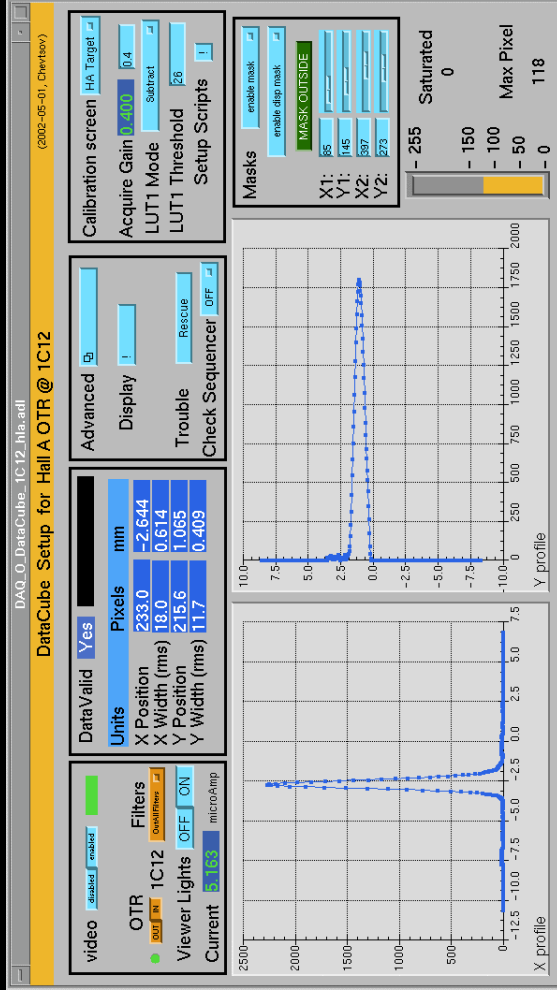
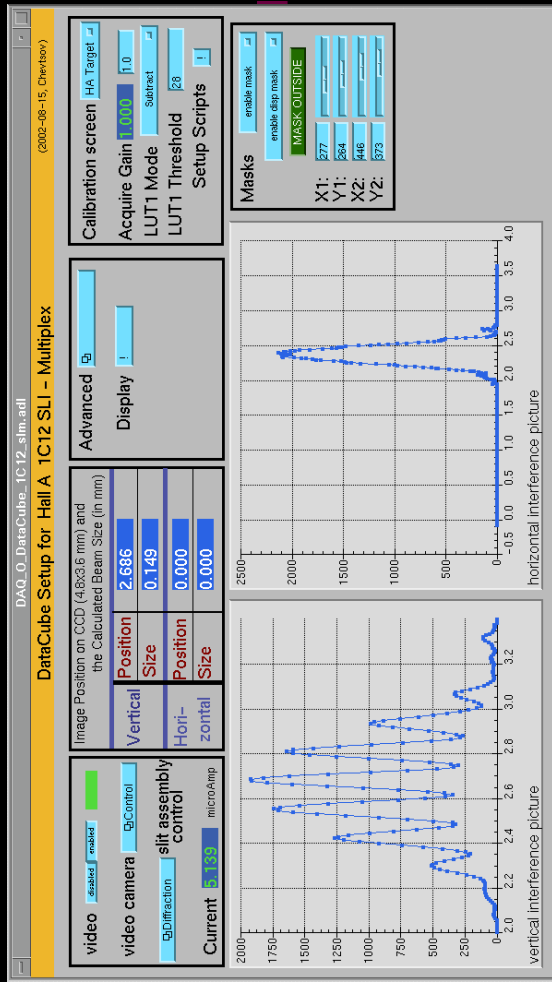
LP30

Version 3.0

DSP Lpf .10 Xd->62.51 Yd->22.00 Loc@ 900







Summary

- Jefferson Lab has a modern beam diagnostic device based on non-invasive technology
- Jefferson Lab has a great experience in design and installation of such a device
- The resolution of this device can be made less than $10\text{ }\mu\text{m}$
- The device's operational current range:
a few microamps \rightarrow milliamps

SLI team:

P. Chevtsov, J.-C. Denard, R. Hicks, K. Capek, D. Hardy,
D. Wetherholt, Z. Kurzun

Special thanks to:

M. Tiefenback, G. Krafft, H. Areti, L. Merminga, J. Benesch,
A. Bogacz, A. Freyberger, Y. Derbenev, A. Hutton, K. White.

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technicians.

