USPAS Course on Recirculating Linear Accelerators

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Lecture 4
Outline

- Independent Orbit Recirculators
  - The Stanford-HEPL Superconducting “Recyclotron”
    - Basic Design Equations
    - Phase Stability Condition
  - The Wuppertal/Darmstadt “Rezyklotron”
  - The MIT-Bates Recirculator
  - CEBAF at Jefferson Lab

- Energy Recovery Linacs (ERLs)
  - The SCA/FEL Energy Recovery Experiment
  - The Los Alamos FEL Energy Recovery Experiment
  - The CEBAF Injector Energy Recovery Experiment
  - The Jefferson Lab 1.7 kW IR FEL
  - Benefits of Energy Recovery
Independent Orbit Recirculators - Motivation

- At final beam energy, $E_f \sim$ several 100 MeV, cost of racetrack microtron is dominated by cost of end magnets

- Cost of end magnets $\propto E_f^3$
  $\Rightarrow$ Standard racetrack microtron (RTM) uneconomical at $E_f \approx 500 – 1000$ MeV

- Bicyclotron and hexatron: one method to overcome the problem but they are similarly limited

- A distinctly different approach: A recirculation system with independent or separate orbits, *i.e.* orbits which do not share the same uniform field magnets

- Cost $\propto E_f$ (close to the ideal)
The “Mesotron”

- The first of independent orbit recirculating accelerator designs
- Proposed by Bathow et al., (1968) for high duty factor acceleration at very high energies – up to 60 GeV

- Although looks similar to a high order polytron, it is distinctly different because of the independent control of every orbit
- At high energies, synchrotron radiation (SR) could present problems and magnetic field values would be restricted to very low values as a consequence.
- At E > 50 GeV, the Mesotron might be cheaper to build than a synchrotron since it has independent DC magnets and can tolerate a much greater energy loss per orbit by SR.
The Stanford–HEPL Superconducting “Recyclotron”

- Main recirculation magnets incorporate four channels (tracks) in which the uniform fields are independently tailored to the momenta of the separate orbits.
  - Use a constant magnet gap with staggered coil windings which produce an appropriately stepped field profile.
Basic Design Equations

- Synchronism conditions for independent orbit recirculators are the same as for racetrack microtrons:
  - Period of the first orbit must be an integral number, m of $T_{rf}$
    \[ 2\pi \rho_1 + 2L = m\lambda \]
  - Magnitude of the magnetic field is different in each orbit, therefore
    \[ \gamma_1 \frac{B_0}{B_1} + \frac{2L}{\lambda} = m \]
    $B_1$ is the effective magnetic induction in the magnets of the first orbit, and
    \[ B_0 = \frac{2\pi mc}{\lambda e} \]
Basic Design Equations (cont’d)

- Period of each orbit must be an integral number \( n \) of \( T_{rf} \) longer than that of the previous orbit:

\[
2\pi\Delta\rho = n\lambda \quad \text{(same as in RTMs)}
\]

- For RTMs this condition implies:

\[
\Delta \gamma \frac{B_0}{B_z} = n
\]

- For independent orbit recirculators it implies:

\[
\Delta \gamma \frac{B_0}{B_l} = H_l
\]

where

\[
H_l = \frac{2\pi \rho l}{\lambda (l + i)} \quad i = \frac{E_0}{\Delta E}
\]

- \( H_l \) is different for each orbit, \( H_l \sim 1/l \) and \( H_l > n \) always

- \( H_l \) plays the same role for the independent orbit recirculators as \( n \) for the RTMs, especially with regard to phase stability.
Phase Stability in Independent Orbit Recirculators

- Can be significantly different from RTMs
- Use formalism introduced in RTMs
- Write difference equation for an electron starting at the center of the linac, traversing half of the linac through pass \( l \), going around the arc, and traversing half of the linac through pass \( l+1 \):

\[
\begin{bmatrix}
\Delta \phi_{l+1} \\
\Delta E_{l+1}
\end{bmatrix} = \begin{bmatrix}
1 & 0 \\
-e \frac{V_c}{2} \sin \phi_l & 1
\end{bmatrix} \begin{bmatrix}
1 \\
0
\end{bmatrix} \begin{bmatrix}
\frac{4 \pi^2 \rho_l}{\lambda E_l} \\
0
\end{bmatrix} \begin{bmatrix}
1 \\
0
\end{bmatrix} \begin{bmatrix}
\frac{4 \pi^2 \rho_l}{\lambda E_l} \\
0
\end{bmatrix} \begin{bmatrix}
\Delta \phi_l \\
\Delta E_l
\end{bmatrix}
\]

“Synchronous” electron during pass \( l \), has phase \( \phi_l \) and energy \( E_l = E_0 + l e V_c \cos \phi_l \)
Phase Stability in Independent Orbit Recirculators (cont’d)

\[
\begin{pmatrix}
\Delta \phi_{l+1} \\
\Delta E_{l+1}
\end{pmatrix}
= \begin{pmatrix}
1 - eV_c \sin \phi_l \frac{2\pi^2 \rho_l}{\lambda E_l} & \frac{4\pi^2 \rho_l}{\lambda E_l} \\
-eV_c \sin \phi_l \left(1 - eV_c \sin \phi_l \frac{\pi^2 \rho_l}{\lambda E_l}\right) & 1 - eV_c \sin \phi_l \frac{2\pi^2 \rho_l}{\lambda E_l}
\end{pmatrix}
\begin{pmatrix}
\Delta \phi_l \\
\Delta E_l
\end{pmatrix}
\]

• Stability condition \( \left[ \frac{\text{TrM}}{2} \right]^2 < 1 \) implies: \( 0 < \pi H_l \tan \phi_l < 2 \)

where \( H_l = \Delta \gamma \frac{B_0}{B_l} \)

• Recall \( H_l \) is generally large and decreases as \( 1/l \)
  \( \Rightarrow \) phase stable region is initially small and increases with orbit number.
Phase Stability in Independent Orbit Recirculators (cont’d)

• For isochronous transport:

\[
\begin{pmatrix}
\Delta \phi_{l+1} \\
\Delta E_{l+1}
\end{pmatrix} =
\begin{pmatrix}
1 & 0 \\
-eV_c \sin \phi_s & 1
\end{pmatrix}
\begin{pmatrix}
\Delta \phi_l \\
\Delta E_l
\end{pmatrix}
\]

• Usually \(\phi_s = 0\). Higher order effects tend to become important.
Examples of Isochronous Recirculating Linacs

- The Wuppertal/Darmstadt “Rezyklotron”
- The MIT-Bates Recirculator
- The CEBAF at Jefferson Lab
The Wuppertal/Darmstadt “Rezyklotron”

- The “Rezyklotron” incorporates a superconducting linac at 3 GHz.
- Beam injection energy = 11 MeV, variable extraction energy up to 130 MeV, beam current 20 µA, 100% duty factor. Energy resolution = 2 x 10^{-4}.
- Two orbits designed with 180° isochronous and achromatic bends and two quadrupole doublets and two triplets in the backleg.
- Isochronous beam optics
  Phase oscillations do not occur and energy resolution is determined primarily by second order effects in the linac.
The MIT-BATES Recirculator

- The MIT-Bates, one-orbit recirculator: An isochronous recirculator
- Severe transient beam loading dictates the isochronous nature of MIT-Bates transport system.
  - a) Fluctuations of beam current during each pulse cause variable beam loading. The resulting first pass energy variation of ±0.15%. At a magnet bending radius of about 1m, this energy fluctuation would result in bunch length, after recirculation in a non-isochronous orbit, of almost 90° of rf phase!
  - b) Total accelerating potential drops by 6% when recirculated beam re-enters the linac and total beam current goes from 8mA to 16 mA. With non-isochronous transport, resulting change in orbit energy would be equivalent to a path length change of many $\lambda_{rf}$.
- Both effects were eliminated by an isochronous recirculation design that could accommodate a 6% energy change.
- Flanz et al. (1980) successfully designed a recirculator that satisfies all these conditions.
The MIT-BATES Recirculator (cont’d)

- Injection energy = 20 MeV
- Each end of the transport system consists of 5 uniform field dipole magnets which bend by 20°, −20°, 180°, −20° and 20°.
- Edge focusing in these magnets is the only form of focusing in these parts of the orbit.
- Four sextupoles control higher order optical aberrations
- Straight section in the backleg contains 5 quadrupole triplets
- Final energy to date is 750 MeV (?) at an average current of 100 µA (?) (5 mA pulse current) with energy resolution ±0.15% have been achieved.
The CEBAF at Jefferson Lab

- The CEBAF accelerator is a 5-pass recirculating srf linac with cw beams of up to 200 $\mu$A, geometric emittance $< 10^{-9}$ m, and relative momentum spread of a few $10^{-5}$.

- The present full energy is nearly 6 GeV. An upgrade to 12 GeV is planned.
The CEBAF at Jefferson Lab (cont’d)

- Most radical innovations (had not been done before on the scale of CEBAF):
  - choice of srf technology
  - use of multipass beam recirculation
- Until LEP II came into operation, CEBAF was the world’s largest implementation of srf technology.
The CEBAF at Jefferson Lab (cont’d)

- SRF Technology

  - srf at 1500 MHz is adopted for CEBAF: result of optimization but ultimately Cornell design had well developed understanding of HOM impedances and Q’s and had demonstrated effectiveness of the waveguide-type HOM couplers.

  - Advantage of the design: small energy spread ~ 2.5 x 10^{-5} and similar relative energy stability are possible
    ⇒ tight control of rf phase and amplitude in each cavity is required

  - srf cavities have ~150 Hz bandwidth
    ⇒ experience microphonics (mechanical vibrations leading to oscillations in their resonant frequency)
    These oscillations lead to tuning errors of up to 25°.

  - The need to meet tight control requirements led to a defining characteristic of CEBAF rf system: each cavity has its own klystron and low-level rf control system.
Recirculation and Beam Optics

- A straightforward linac would exceed the projects’ cost boundaries adopt beam recirculation.

- Relativistic electrons travel at \( \sim c \) independent of energy. They stay within \(< 1^\circ\) of rf phase at 1500 MHz of a phase reference point over many kilometers.

- A recirculating linac sends a beam \( n \) times through a linac section \( 1/n \) the length of a full-energy linac by means of \( n \) transport systems tuned to the energy of the \( n \)th path.

- Each transport system must be unique to accommodate the momentum of the specific beam energy it propagates, but in the accelerating sections bunches of different energy occupy the same spatial locations, and because of \( c \), they stay in phase.
The CEBAF at Jefferson Lab (cont’d)

- Recirculation and Beam Optics (cont’d)

  • Each recirculation path is handled by an independent transport system ⇒ individual beam-line designs can be evolved to manage SR-induced degradation of emittance and energy spread ⇒ Recirculating linacs provide an effective path to very high beam energies while allowing preservation of high beam quality!

  • Decisions were made to
    ♦ Have linac sections in both legs of the racetrack for shorter length.
    ♦ Operate in “linac fashion” (on crest) without phase focusing (unlike RTMs):
      ▪ it makes optimal use of installed accelerating structures and
      ▪ phase focusing is not needed with relativistic beam bunches of subpicosecond duration and appropriate precision rf control.
The CEBAF at Jefferson Lab (cont’d)

- From these decisions flow several requirements:
  - Linac-to-linac system: achromatic and isochronous \((M_{56} < 0.2 \text{ m})\) on all passes
  - Pass-to-pass tolerance for phase or path length < 100 \(\mu\text{m}\).
  - Vertical dispersion in the arcs is corrected locally.

- Accelerator Physics

  - Multibunch beam breakup: Threshold current \(~ 20\) times higher than operating current
Energy Recovery Linacs

- Beam current at CEBAF is limited by the rf power installed and by the beam power on the beam dump, already at 1 MW at 5 GeV and 200 µA.

- **Energy recovery** is a way to overcome these limits: one can increase the beam current (almost) without increasing the rf power or the beam dump size.

- Basic idea: Bring the beam through the accelerating structures timed in a way so that the second-pass beam is decelerated, i.e. delivering its energy to the cavity fields.

- First demonstration of energy recovery in an rf linac at Stanford University (1986)

- Energy recovery demonstration at world-record current at the Jefferson Lab IR FEL
The SCA/FEL Energy Recovery Experiment

- Same-cell energy recovery was first demonstrated in the SCA/FEL in July 1986
- Beam was injected at 5 MeV into a ~50 MeV linac (up to 95 MeV in 2 passes), 150 µA average current (12.5 pC per bunch at 11.8 MHz)
- The previous recirculation system (SCR, 1982) was unsuccessful in preserving the peak current required for lasing and was replaced by a doubly achromatic single-turn recirculation line.
- All energy was recovered. FEL was not in place.
The Los Alamos FEL Energy Recovery Experiment

- Accelerator consists of injector, buncher, and two 10-MeV accelerator sections at 1300 MHz.
- Beam is transported around a 180° bend and through decelerators to a spectrometer.
- Decelerators are coupled to accelerators and klystrons through resonant bridge couplers.
- Electrons lose energy in the decelerators (21 MeV -> 5 MeV), and the rf power generated is shared with the accelerators through the resonant bridge couplers.

W – Wiggler
R – 180° bend
C and D – Decelerators
A and B – Accelerators
BC – Resonant Bridge couplers
The CEBAF Injector Energy Recovery Experiment


64 – 215 uA in accelerating mode
up to 30 uA in energy recovery mode
The JLab 2.13 kW IRFEL and Energy Recovery Demonstration

## IR FEL Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal</th>
<th>Achieved</th>
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</thead>
<tbody>
<tr>
<td>Beam energy at wiggler</td>
<td>42 MeV</td>
<td>20-48 MeV</td>
</tr>
<tr>
<td>Beam current</td>
<td>5 mA</td>
<td>5 mA</td>
</tr>
<tr>
<td>Single bunch charge</td>
<td>60 pC</td>
<td>60-135 pC</td>
</tr>
<tr>
<td>Bunch repetition rate</td>
<td>74.85 MHz</td>
<td>18.7-74.85 MHz</td>
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<tr>
<td>Normalized emittance</td>
<td>13 mm-mrad</td>
<td>5-10 mm-mrad</td>
</tr>
<tr>
<td>RMS bunch length at wiggler</td>
<td>0.4 psec</td>
<td>0.4 psec</td>
</tr>
<tr>
<td>Peak current</td>
<td>60 A</td>
<td>60 A</td>
</tr>
<tr>
<td>FEL extraction efficiency</td>
<td>$\frac{1}{2}$%</td>
<td>&gt;1%</td>
</tr>
<tr>
<td>dp/p</td>
<td></td>
<td></td>
</tr>
<tr>
<td>rms before FEL</td>
<td>$\frac{1}{2}$%</td>
<td>$\frac{1}{4}$%</td>
</tr>
<tr>
<td>full after FEL</td>
<td>5%</td>
<td>6-8%</td>
</tr>
<tr>
<td>CW FEL Power</td>
<td>~1 kW</td>
<td>2.13 kW</td>
</tr>
</tbody>
</table>
Energy Recovery Works

Gradient modulator drive signal in a linac cavity measured without energy recovery (signal level around 2 V) and with energy recovery (signal level around 0).
With energy recovery the required linac rf power is ~ 16 kW, nearly independent of beam current. It rises to ~ 36 kW with no recovery at 1.1 mA.
JLab 10kW IR FEL and 1 kW UV FEL

Achieved 8.5 kW CW IR power on June 24, 2004!
Energy recovered up to 5mA at 145 MeV, up to 9mA at 88 MeV
## System Parameters for Upgrade (IR&UV)

<table>
<thead>
<tr>
<th></th>
<th>Demo</th>
<th>IR Upgrade</th>
<th>UV Upgrade</th>
<th>Achieved</th>
</tr>
</thead>
<tbody>
<tr>
<td>Energy (MeV)</td>
<td>35-48</td>
<td>80-210</td>
<td>200</td>
<td>20-48</td>
</tr>
<tr>
<td>I_{ave} (mA)</td>
<td>5</td>
<td>10</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Beam Power (kW)</td>
<td>200</td>
<td>2000</td>
<td>1000</td>
<td>240</td>
</tr>
<tr>
<td>Charge/bunch (pC)</td>
<td>60</td>
<td>135</td>
<td>135</td>
<td>135</td>
</tr>
<tr>
<td>Rep. Rate (MHz)</td>
<td>18.75-75</td>
<td>4.7-75</td>
<td>2.3-75</td>
<td>18.75-75</td>
</tr>
<tr>
<td>Bunch Length* (psec)</td>
<td>0.4</td>
<td>0.2</td>
<td>0.2</td>
<td>0.4(60 pC)</td>
</tr>
<tr>
<td>Peak Current (A)</td>
<td>60</td>
<td>270</td>
<td>270</td>
<td>&gt;60 A</td>
</tr>
<tr>
<td>σE/E</td>
<td>0.5%</td>
<td>0.5%</td>
<td>0.125%</td>
<td>&lt;0.25%</td>
</tr>
<tr>
<td>e_N (mm-mrad)</td>
<td>&lt;13</td>
<td>&lt;30</td>
<td>&lt;11</td>
<td>5-10</td>
</tr>
<tr>
<td>FEL ext. efficiency</td>
<td>0.5%</td>
<td>1%</td>
<td>0.25%</td>
<td>&gt;0.75%</td>
</tr>
<tr>
<td>FEL power (kW)</td>
<td>1</td>
<td>&gt;10</td>
<td>&gt;1</td>
<td>2.1</td>
</tr>
<tr>
<td>Induced energy spread (full)</td>
<td>5%</td>
<td>10%</td>
<td>5%</td>
<td>6-8%</td>
</tr>
</tbody>
</table>

* rms value
Rf to Beam Efficiency

\[ \eta_b^{RF} = \frac{P_{beam}}{P_{RF}} \approx \frac{JE_f}{(J - 1)E_{inj} + E_f} \]

\[ J = \frac{4I(r/\bar{Q})Q_L}{G_a} \]
Benefits of Energy Recovery

- Required rf power becomes nearly independent of beam current.
- Increases overall system efficiency.
- Reduces electron beam power to be disposed of at beam dumps (by ratio of $E_{\text{fin}}/E_{\text{inj}}$).
- More importantly, reduces induced radioactivity (shielding problem) if beam is dumped below the neutron production threshold.