

Homework Problems 2

1. Show that for any two-by-two unimodular real matrix M ($\det(M)=1$), the condition that the eigenvalues of M remain on the unit circle is equivalent to

$$\left(\frac{\text{Tr } M}{2}\right)^2 < 1.$$

Show the stability condition follows from this condition on M , applied to the single pass longitudinal transfer matrix. Note ρ_l is proportional to E_l .

Compute the synchrotron phase advance per pass in the microtron as a function of ν and the synchronous phase φ_s .

2. Verify this table from the lectures, for constant K and ρ

	$K < 0$	$K = 0$	$K > 0$
$D_{p,0}(s)$	$\frac{1}{ K \rho} \left(1 - \cosh(\sqrt{ K }s)\right)$	$-\frac{s^2}{2\rho}$	$\frac{1}{K\rho} \left(\cos(\sqrt{K}s) - 1\right)$
$D'_{p,0}(s)$	$-\frac{1}{\sqrt{ K }\rho} \sinh(\sqrt{ K }s)$	$-\frac{s}{\rho}$	$-\frac{1}{\sqrt{K}\rho} \sin(\sqrt{K}s)$

3. Verify, using the polytron bender magnet geometry, that

$$\Delta\gamma = v \frac{f_c}{f_{RF}} \frac{1}{1 - (p/2\pi) \sin(2\pi/p)}$$

This figure may be helpful

