

# **Physics 417/517**

## **Introduction to Particle Accelerator Physics**

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# Equilibrium Energy Spread



Quantized photon emission events act to stimulate motion in all three degrees of freedom. Thus, the oscillations do not damp to zero.

$$\langle \Delta A^2 \rangle = \langle A_1^2 - A_0^2 \rangle = \Delta e^2 \quad \Delta e = \hbar \omega$$
$$\left\langle \frac{dA^2}{dt} \right\rangle = \int_0^\infty \Delta e^2 \frac{d\dot{n}}{d(\Delta e)} d\Delta e = \dot{N}_{ph} \langle \Delta e^2 \rangle$$

In equilibrium.

$$\langle A^2 \rangle = \frac{\tau_{\Delta\phi}}{2} \dot{N}_{ph} \langle \Delta e^2 \rangle$$
$$\frac{\sigma_E^2}{E^2} = \frac{55}{32\sqrt{3}} \frac{\hbar c}{mc^2} \frac{\gamma^2}{2 + \mathcal{G}} \frac{\langle 1/\rho^3 \rangle}{\langle 1/\rho^2 \rangle}$$

# Equilibrium Emittance



$$\langle \delta a^2 \rangle = \frac{\Delta e^2}{E_o^2} H(s)$$

$$H(s) = \beta D'^2 + 2\alpha D D' + \gamma D^2$$

In equilibrium, averaged over the ring.

$$\langle a^2 \rangle = \frac{\tau_x}{2} \dot{N}_{ph} \langle \Delta e^2 \rangle$$

$$\varepsilon_x = \frac{\sigma_x^2}{\beta_x} = \frac{55}{32\sqrt{3}} \frac{\hbar c}{mc^2} \frac{\gamma^2}{1 - \mathcal{G}} \frac{\langle H / \rho^3 \rangle}{\langle 1 / \rho^2 \rangle}$$

# Emittance and energy spread increases



For recirculated linacs, there is no equilibrium and similar estimates are used to compute emittance and energy spread increases (for a bend of  $\pi = 180^\circ$ )

$$\Delta \varepsilon_{x,y} = \frac{1}{2cE_0^2} \int \dot{N}_{ph} (e^2) H(s) ds = \frac{55 C_\gamma \hbar c (mc^2)^2}{64\pi\sqrt{3}} \gamma^5 \int \frac{H}{\rho^3} ds$$

$$\begin{aligned} \Delta \frac{\sigma_E^2}{E^2} &= \frac{5\pi}{32\sqrt{3}} \frac{\hbar c}{mc^2} \frac{\gamma^2}{2 + \mathcal{G}} \left( 11 - \frac{64}{25} \right) \frac{\langle 1/\rho^3 \rangle}{\langle 1/\rho^2 \rangle} \\ &= \frac{5\pi}{32\sqrt{3}} \frac{\hbar c}{mc^2} \frac{\gamma^2}{2 + \mathcal{G}} \left( 11 - \frac{64}{25} \right) \frac{\langle 1/\rho^3 \rangle}{\langle 1/\rho^2 \rangle} \end{aligned}$$

# Independent Orbit Recirculators

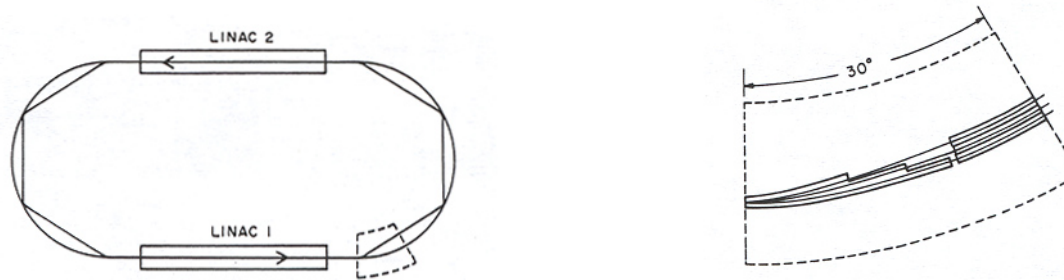
## - Motivation



- At final beam energy,  $E_f \sim$  several 100 MeV, cost of racetrack microtron is dominated by cost of end magnets
- Cost of end magnets  $\propto E_f^3$   
 $\Rightarrow$  Standard racetrack microtron (RTM) uneconomical at  $E_f \approx 500 - 1000$  MeV
- Bicyclotron and hexatron: one method to overcome the problem but they are similarly limited
- A distinctly different approach: **A recirculation system with independent or separate orbits**, *i.e.* orbits which do not share the same uniform field magnets

# The “Mesotron”

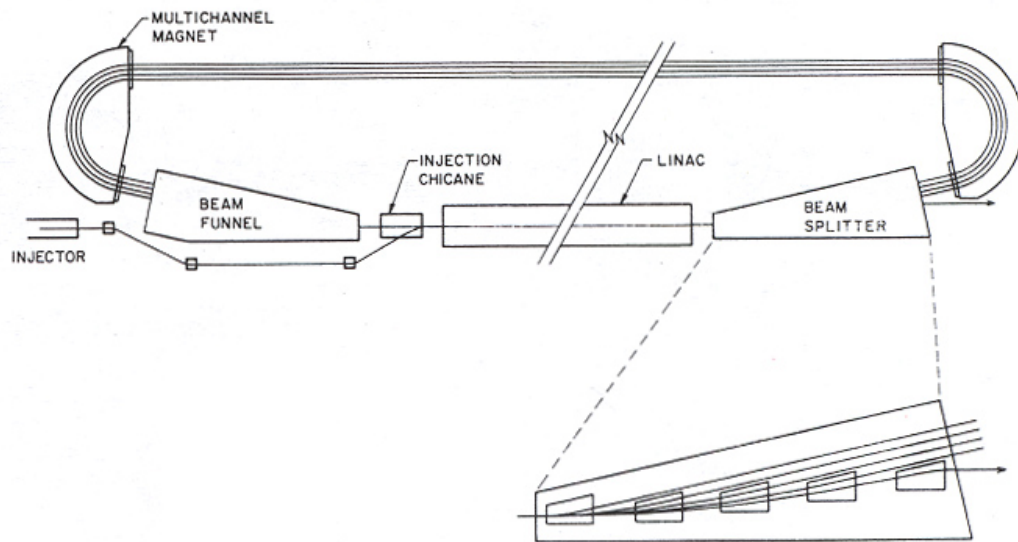
- The first of independent orbit recirculating accelerator designs
- Proposed by Bathow et al., (1968) for high duty factor acceleration at very high energies – up to 60 GeV



- Although looks similar to a high order polytron, it is distinctly different because of the independent control of every orbit
- At high energies, synchrotron radiation (SR) could present problems and magnetic field values would be restricted to very low values as a consequence.
- At  $E > 50$  GeV, the Mesotron might be cheaper to build than a synchrotron since it has independent DC magnets and can tolerate a much greater energy loss per orbit by SR.

# The Stanford–HEPL Superconducting “Recyclotron”

- Main recirculation magnets incorporate four channels (tracks) in which the uniform fields are independently tailored to the momenta of the separate orbits.
  - Use a constant magnet gap with staggered coil windings which produce an appropriately stepped field profile.



# No Phase Stability in Independent Orbit Recirculators



- For isochronous ( $M_{56} = 0$ ) transport:

$$\begin{pmatrix} \Delta\phi_{l+1} \\ \Delta E_{l+1} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -eV_c \sin \phi_s & 1 \end{pmatrix} \begin{pmatrix} \Delta\phi_l \\ \Delta E_l \end{pmatrix}$$

- Usually  $\phi_s = 0$ . Higher order effects tend to become important.



# Examples of Isochronous Recirculating Linacs



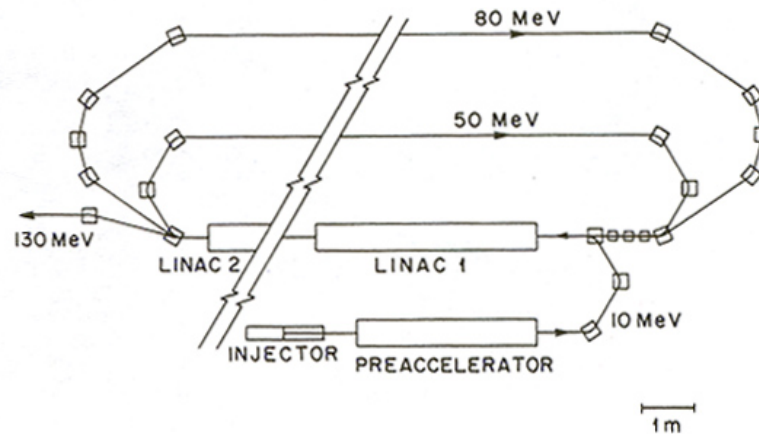
- The Wuppertal/Darmstadt “Rezyklotron”
- The MIT-Bates Recirculator
- The CEBAF at Jefferson Lab

# The Wuppertal/Darmstadt “Rezyklotron”



- The “Rezyklotron” incorporates a superconducting linac at 3 GHz.
- Beam injection energy = 11 MeV, variable extraction energy up to 130 MeV, beam current 20  $\mu\text{A}$ , 100% duty factor. Energy resolution =  $2 \times 10^{-4}$ .
- Two orbits designed with 180° **isochronous and achromatic bends** and two quadrupole doublets and two triplets in the backleg.
- **Isochronous beam optics**

Phase oscillations do not occur and energy resolution is determined primarily by second order effects in the linac.



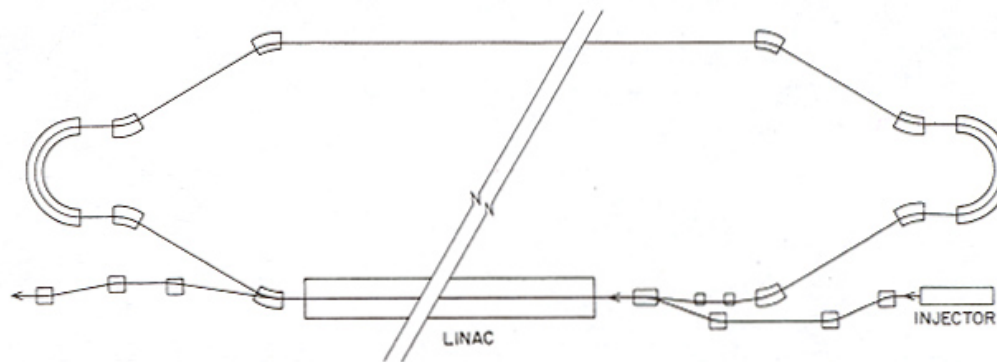
# The MIT-BATES Recirculator



- The MIT-Bates, one-orbit recirculator: An isochronous recirculator
- Severe transient beam loading dictates the isochronous nature of MIT-Bates transport system.
  - a) Fluctuations of beam current during each pulse cause variable beam loading The resulting first pass energy variation of  $\pm 0.15\%$ . At a magnet bending radius of about 1m this energy fluctuation would result in bunch length, after recirculation in a non-isochronous orbit, of almost  $90^\circ$  of rf phase!
  - b) Total accelerating potential drops by 6% when recirculated beam re-enters the linac and total beam current goes from 8mA to 16 mA. With non-isochronous transport, resulting change in orbit energy would be equivalent to a path length change of many  $\lambda_{\text{rf}}$ .
- Both effects were eliminated by an isochronous recirculation design that could accommodate a 6% energy change.
- Flanz *et al.* (1980) successfully designed a recirculator that satisfies all these conditions.

# The MIT-BATES Recirculator (cont'd)

- Injection energy = 20 MeV
- Each end of the transport system consists of 5 uniform field dipole magnets which bend by  $20^\circ$ ,  $-20^\circ$ ,  $180^\circ$ ,  $-20^\circ$  and  $20^\circ$ .
- Edge focusing in these magnets is the only form of focusing in these parts of the orbit.
- Four sextupoles control higher order optical aberrations
- Straight section in the backleg contains 5 quadrupole triplets
- Final energy to date is 750 MeV (?) at an average current of  $100 \mu\text{A}$  (?) (5 mA pulse current) with energy resolution  $\pm 0.15\%$  have been achieved.

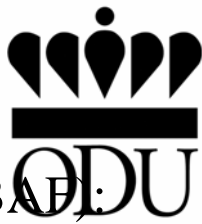


# The CEBAF at Jefferson Lab



- The CEBAF accelerator is a 5-pass recirculating srf linac with cw beams of up to 200  $\mu\text{A}$ , geometric emittance  $< 10^{-9}$  m, and relative momentum spread of a few  $10^{-5}$ .
- The present full energy is nearly 6 GeV. An upgrade to 12 GeV is planned.

# The CEBAF at Jefferson Lab (cont'd)



- Most radical innovations (had not been done before on the scale of CEBAF)
  - choice of srf technology
  - use of multipass beam recirculation
- Until LEP II came into operation, CEBAF was the world's largest implementation of srf technology.

