

# Application of BeamBeam3D to ELIC Studies

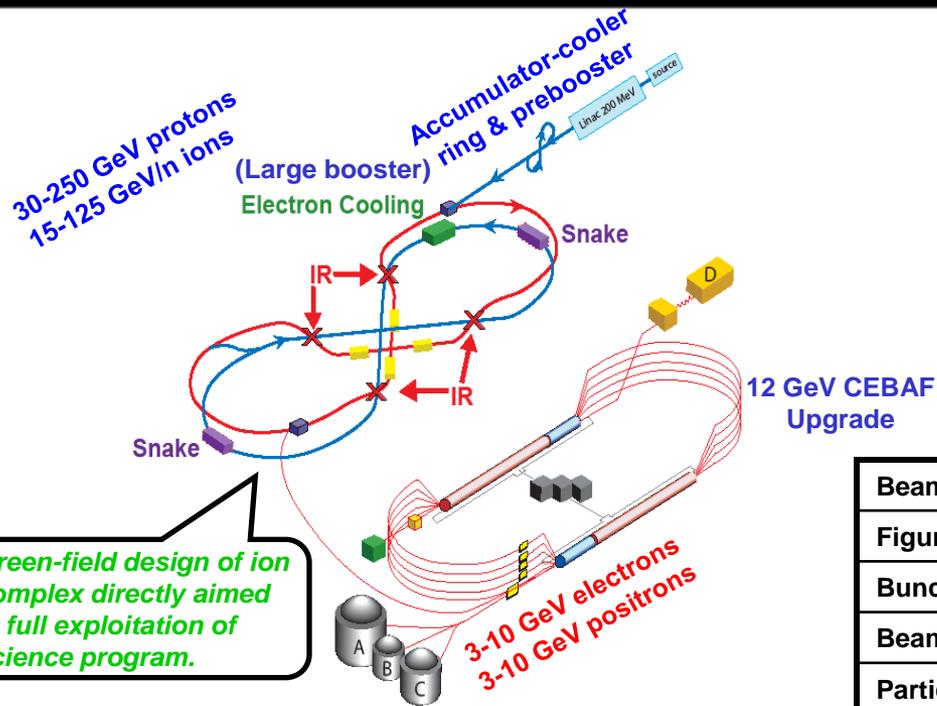
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# Outline

- Introduction
- Model, Code and ELIC Parameters
- Simulation Results with Nominal Parameters
- Parameter Dependence of ELIC Luminosity
- New Working Point
- Multiple IPs and Multiple Bunches
- Summary and Outlook

# Electron-Ion Collider at CEBAF



## Energy

CM 20~100 GeV, asymmetry ~ 10

## Luminosity

$10^{33}$  up to  $10^{35}$   $\text{cm}^{-2} \text{s}^{-1}$  per IP

## Ion Species

Polarized H, D,  $^3\text{He}$ , up to  $A = 208$

## Polarization

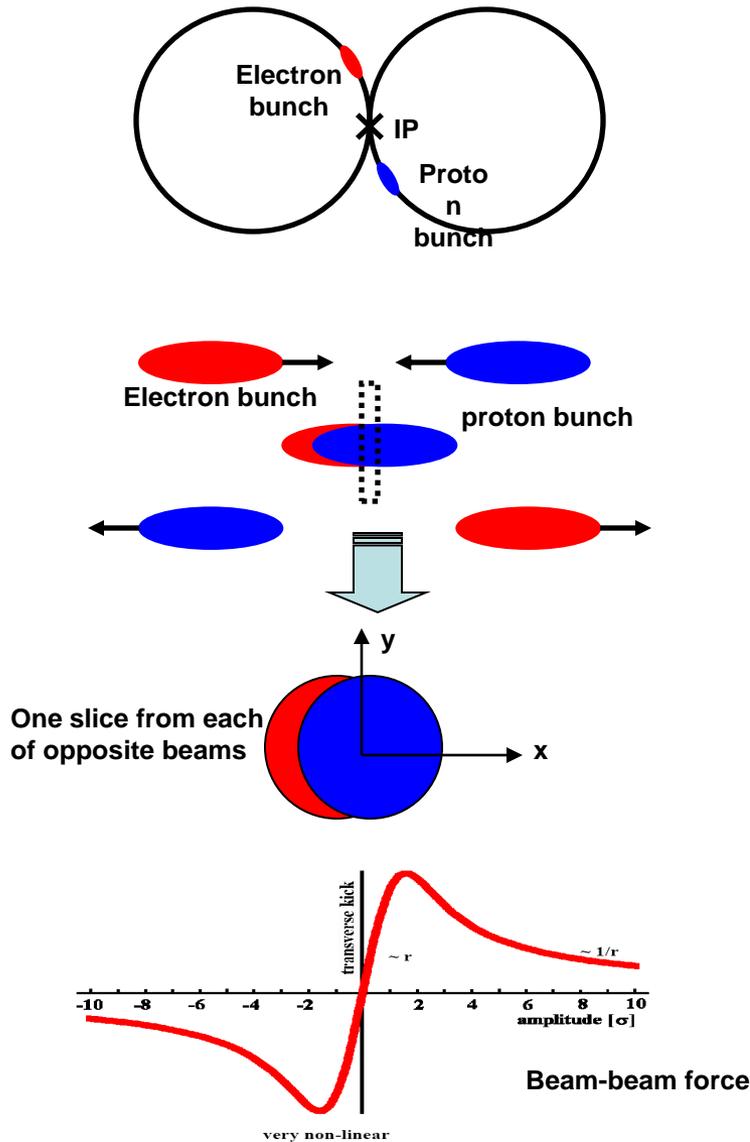
- Longitudinal at the IP for both beams
- Transverse polarization of ions
- Spin-flip of both beams
- All polarizations >70% desirable

Beam energy	GeV	250/10	150/7	50/5
Figure-8 ring	km	2.5		
Bunch collision freq	MHz	499/1499		
Beam current	A	0.66/1.65	0.46/0.99	0.57/1.15
Particles/bunch	$10^9$	2.7/6.9	1.9/4.1	2.3/4.8
Energy spread	$10^{-4}$	3/3		
Bunch length, rms	mm	5/5		
Hori. emit., norm.	$\mu\text{m}$	0.70/51	0.42/35.6	0.28/25.5
Vertical emit., norm.	$\mu\text{m}$	0.03/2.0	0.017/1.4	0.028/2.6
Beta*	mm	5/5		
Vert. b-b turn-shift/IP		0.01/0.1		
Peak lumi. per IP	$10^{34} \text{ cm}^{-2}\text{s}^{-1}$	2.9/8.6	1.2/3.6	1.1/3.3
Number of IPs		4		
Luminosity lifetime	hours	24		

## ELIC luminosity Concepts

- High bunch collision frequency (1.5 GHz)
- Short ion bunches (5 mm)
- Super strong final focusing ( $\beta^* \sim 5$  mm)
- Large beam-beam parameters
- Need High energy electron cooling
- Need crab crossing colliding beams

# Introduction: Beam-Beam Physics



## Transverse Beam-beam force between colliding bunches

- Highly nonlinear forces
- Produce transverse kick between colliding bunches

## Beam-beam effect

- Can cause beam emittance growth, size expansion and blowup
- Can induce coherent beam-beam instabilities
- Can decrease luminosity

linear part  $\rightarrow$  tune shift

nonlinear part  $\rightarrow$  tune spread & instability

# Luminosity and Beam-beam Effect

Luminosity of a storage-ring collider

(when  $\sigma_{xe}=\sigma_{xp}$ ,  $\sigma_{ye}=\sigma_{yp}$ , and  $\beta_{xe}^*=\beta_{xp}^*$ ,  $\beta_{ye}^*=\beta_{yp}^*$ )

$$L = \frac{N_e N_p f_c}{2\pi \sqrt{\sigma_{xe}^2 + \sigma_{xp}^2} \sqrt{\sigma_{ye}^2 + \sigma_{yp}^2}}$$



$$L = \frac{I_e \gamma_e \xi_{ye}}{r_c^e \beta_{ye}^*} \frac{1}{2} \left( 1 + \frac{\sigma_y}{\sigma_x} \right) \propto \xi_{ye}$$

proportional to b-b parameter

we assume both are **Gaussian** bunches,  
 $N_e$  and  $N_p$  are number of electrons and  
 protons in bunches,  $f_c$  is collision frequency,  
 $\sigma_{xe}$ ,  $\sigma_{ye}$ ,  $\sigma_{xp}$  and  $\sigma_{yp}$  are bunch spot size

Increasing beam-beam parameter

- increasing luminosity
- increasing beam-beam instability

Beam-beam parameter (tune-shift)

(characterizes how strong the beam-beam force is)

$$\xi_{ye} = \frac{r_c^e N_p \beta_{ye}^*}{2\pi \gamma_e \sigma_{yp} (\sigma_{xp} + \sigma_{yp})}$$

Where  $r_c^e$  is electron classical radius of,  $\gamma_e$  is  
 relativistic factor, and  $\beta_{ye}^*$  is vertical beta  
 function at interaction point

*Beam-beam is one of most  
 important limiting factors of  
 collider luminosity*

# ELIC Beam-beam Problem

## ELIC IP Design

- Highly asymmetric beams (3-9GeV/1.85-2.5A and 30-225GeV/1A)
- Four interaction points and Figure-8 rings
- Strong final focusing (beta-star 5 mm)
- Very short bunch length (5 mm)
- Employs crab cavity
- Electron and proton beam vertical b-b parameters are 0.087 and 0.01
- Very large electron synchrotron tune (0.25) due to strong RF focusing
- Equal betatron phase advance (fractional part) between IPs

## Short bunch length and small beta-star

- Longitudinal dynamics is important, can't be treated as a pancake
- Hour glass effect, 25% luminosity loss

## Large electron synchrotron tune

- Could help averaging effect in longitudinal motion
- Synchro-betatron resonance

# Simulation Model, Method & Codes

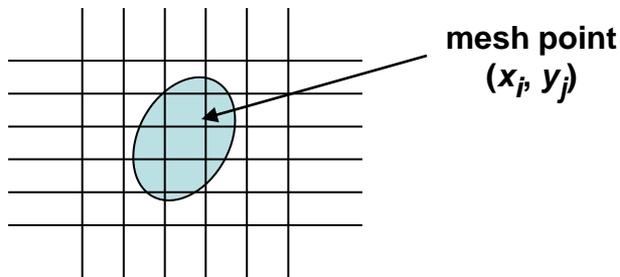
## Basic Idea of Simulations

### *Collision @ IP + transport @ ring*

- Simulating particle-particle collisions by particle-in-cell method
- Tracking particle transport in rings

## Particle-in-Cell Method

- Bunches modeled by macro-particles
- Transverse plane covered with a 2D mesh
- Solve Poisson equation over 2D mesh
- Calculate beam-beam force using EM fields on mesh points
- Advance macro-particles under b-b force



## BeamBeam3D Code

- Developed at LBL by Ji Qiang, etc. (*PRST 02*)
- Based on particle-in-cell method
- A ***strong-strong self-consistent*** code
- Includes longitudinal dim. (multi-slices)

## Code Benchmarking

- several codes including SLAC codes by Y. Cai etc. & JLab codes by R. Li etc.
- Used for simulations of several lepton and hadron colliders including KEKB, RHIC, Tevatron and LHC

## SciDAC Joint R&D program

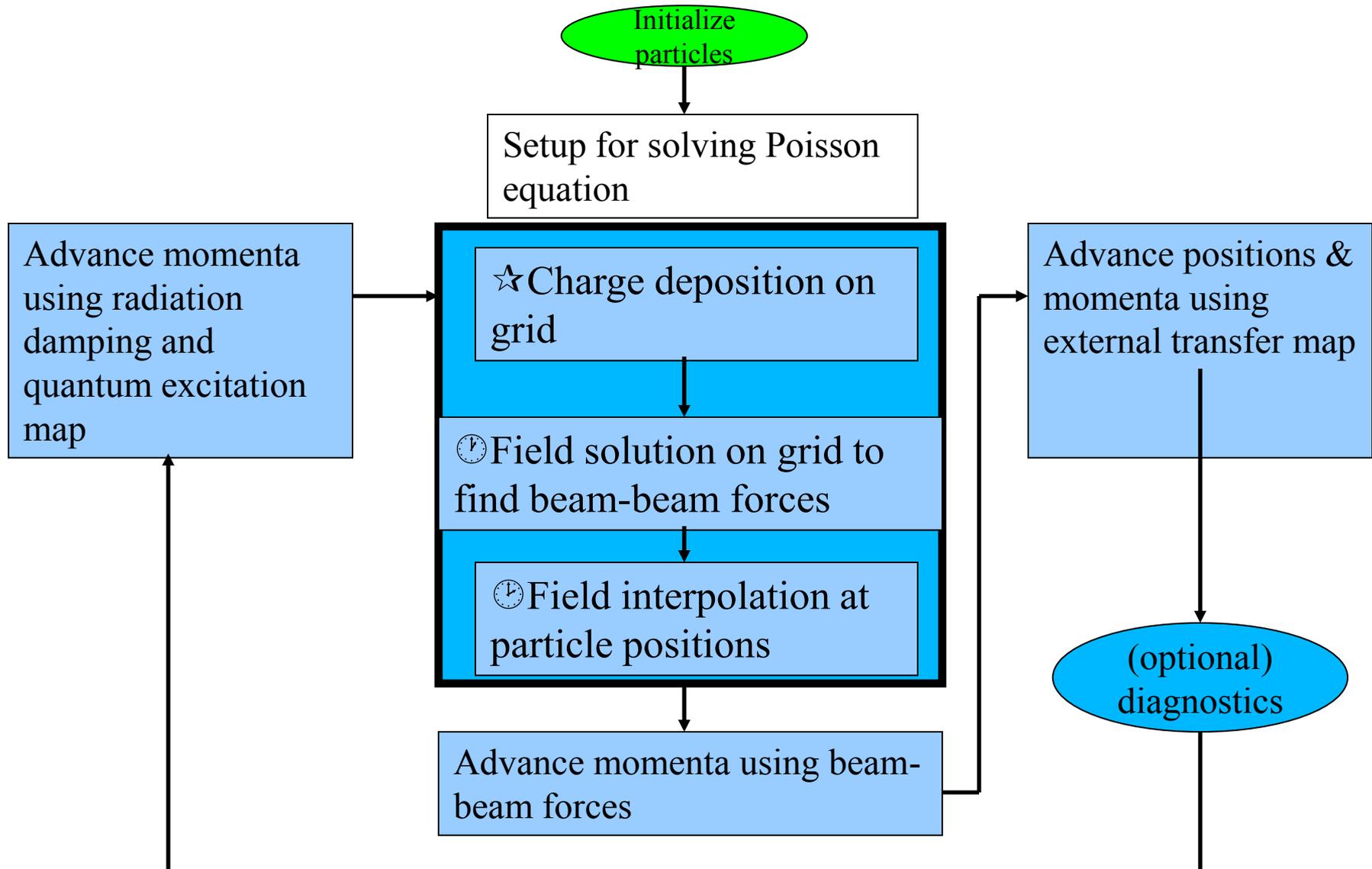
- SciDAC grant COMPASS , a dozen national labs, universities and companies
- JLab does beam-beam simulation for ELIC. LBL provides code development, enhancement and support

# BeamBeam3D:

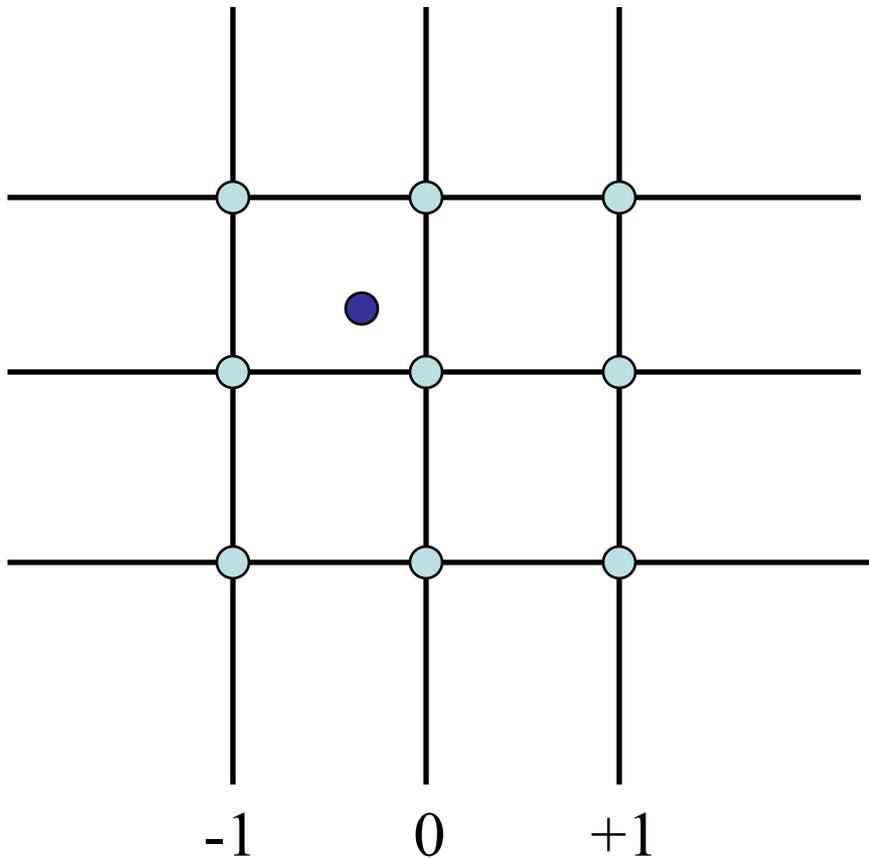
## Parallel Strong-Strong / Strong-Weak Simulation Code

- Multiple physics models:
  - strong-strong (S-S); weak-strong (W-S)
- Multiple-slice model for finite bunch length effects
- New algorithm -- shifted Green function -- efficiently models long-range parasitic collisions
- Parallel particle-based decomposition to achieve perfect load balance
- Lorentz boost to handle crossing angle collisions
- Multi-IP collisions, varying phase adv,...
- Arbitrary closed-orbit separation (static or time-dep)
- Independent beam parameters for the 2 beams
- Conducting wire, crab cavity, electron lens compensations

# Particle-In-Cell Method



# Quadratic Deposition/Interpolation

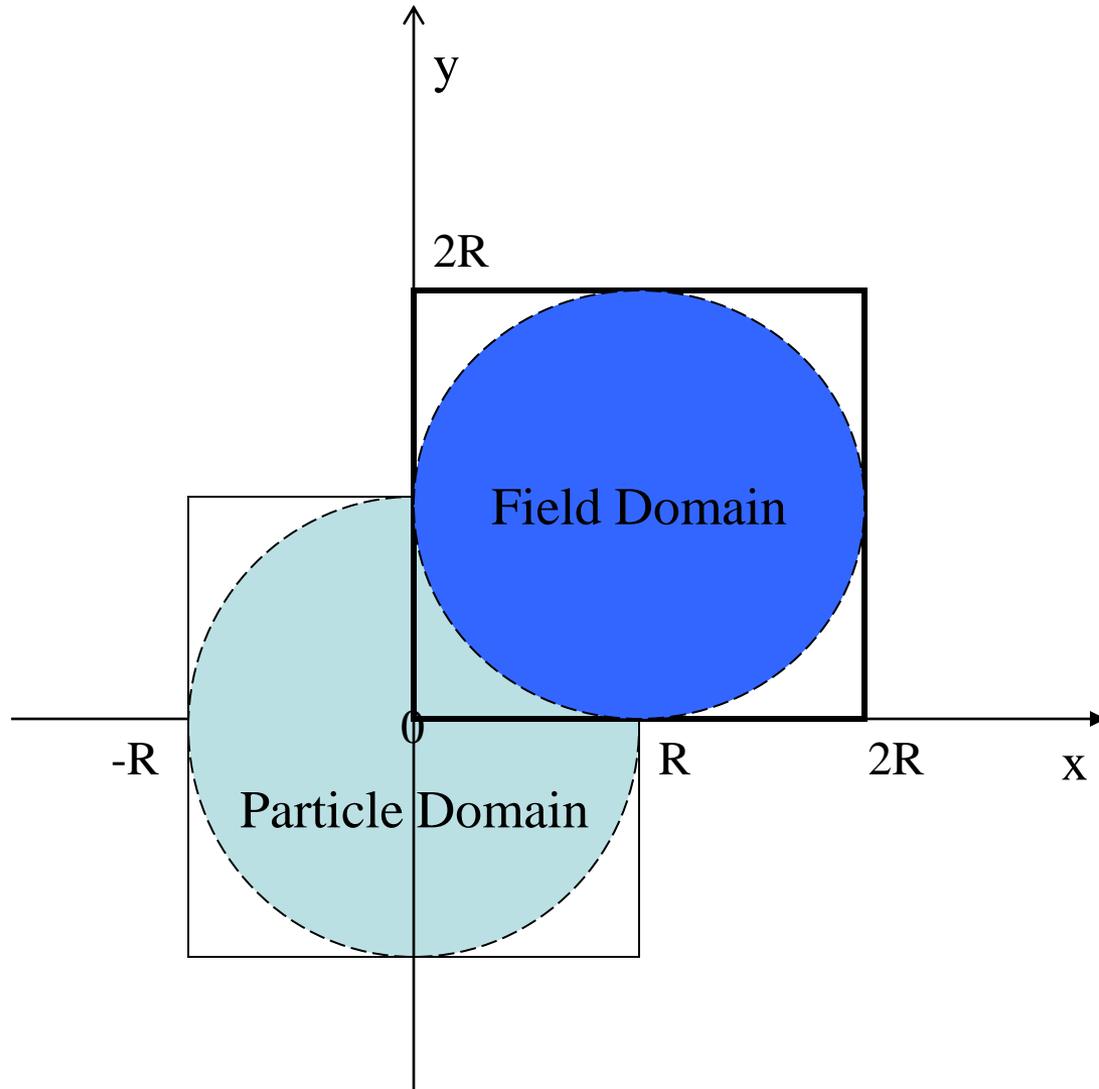


$$w_x^{+1} = \frac{1}{2} \left( \frac{1}{4} - r_x + r_x^2 \right)$$

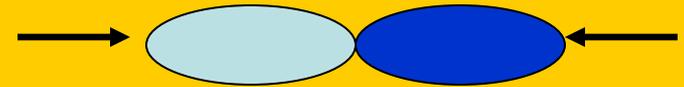
$$w_x^0 = \frac{3}{4} - r_x^2$$

$$w_x^{-1} = \frac{1}{2} \left( \frac{1}{4} + r_x + r_x^2 \right)$$

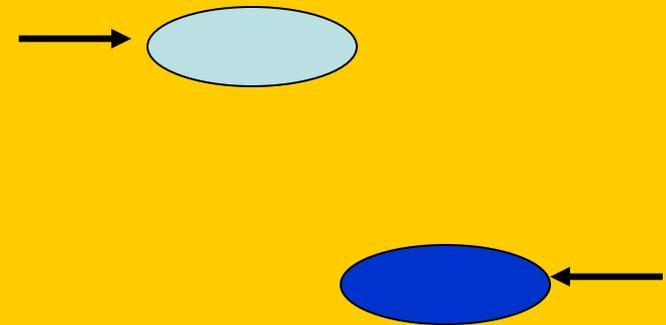
# A Schematic Plot of the Geometry of Two Colliding Beams



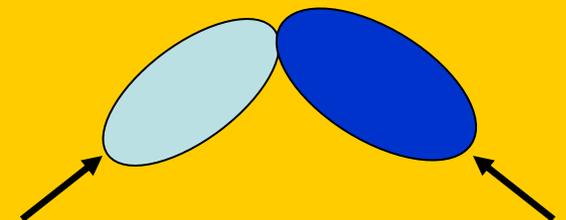
Head-on collision



Long-range collision



Crossing angle collision



# Green Function Solution of Poisson's Equation

$$\phi(r) = \int G(r, r') \rho(r') dr' ; r = (x, y)$$

$$\phi(r_i) = h \sum_{i'=1}^N G(r_i - r_{i'}) \rho(r_{i'})$$

$$G(x, y) = -\frac{1}{2} \log(x^2 + y^2)$$

Direct summation of the convolution scales as  $N^4$  !!!!  
 $N$  – grid number in each dimension

# Green Function Solution of Poisson's Equation (cont'd)

Hockney's Algorithm:- *scales as  $(2N)^2 \log(2N)$*

- Ref: Hockney and Easwood, *Computer Simulation using Particles*, McGraw-Hill Book Company, New York, 1985.

$$\phi_c(r_i) = h \sum_{i'=1}^{2N} G_c(r_i - r_{i'}) \rho_c(r_{i'})$$

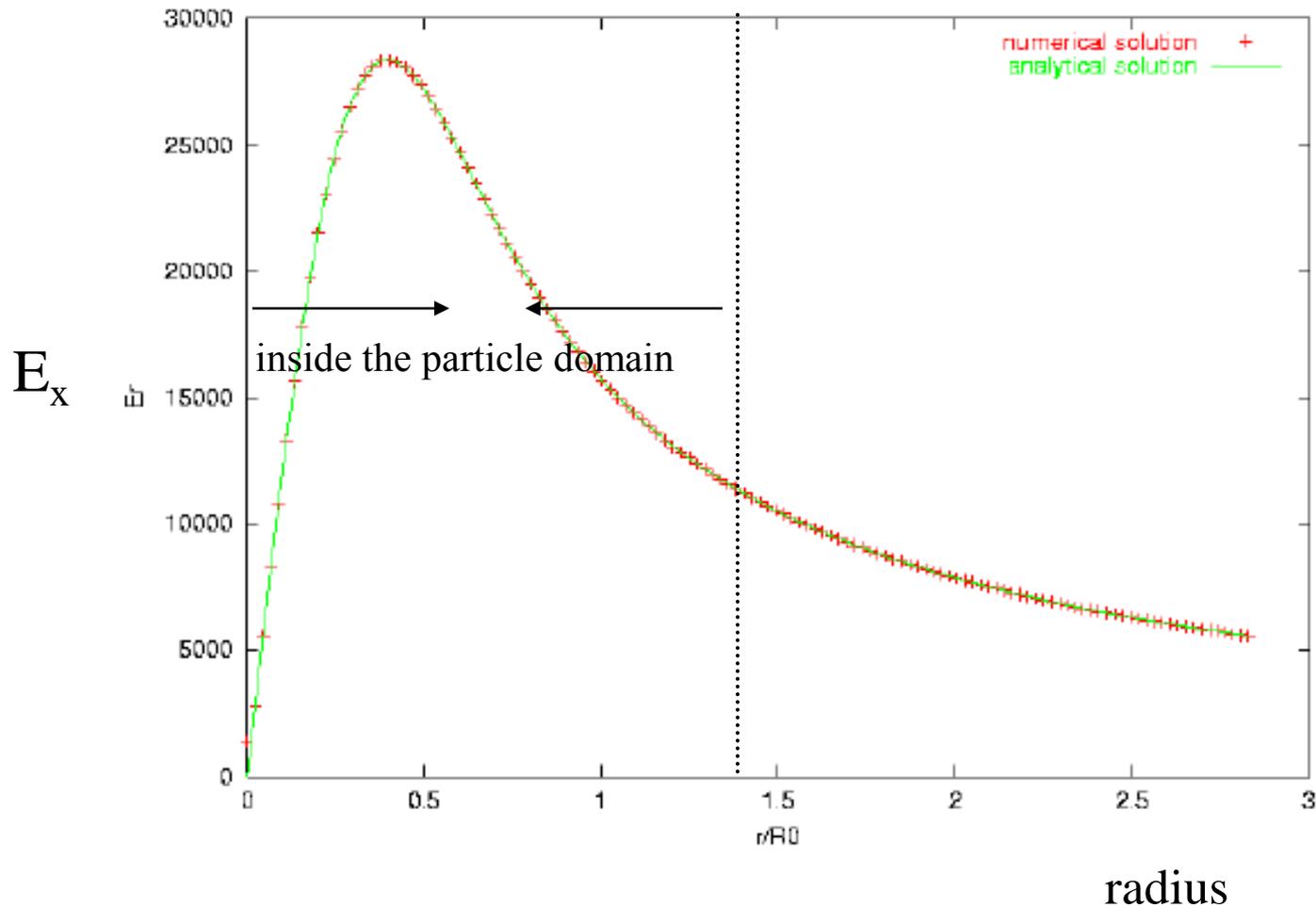
$$\phi(r_i) = \phi_c(r_i) \quad \text{for } i = 1, N$$

Shifted Green function Algorithm:

$$\phi_F(r) = \int G_s(r, r') \rho(r') dr'$$

$$G_s(r, r') = G(r + r_s, r')$$

# Comparison between Numerical Solution and Analytical Solution (Shifted Green Function)



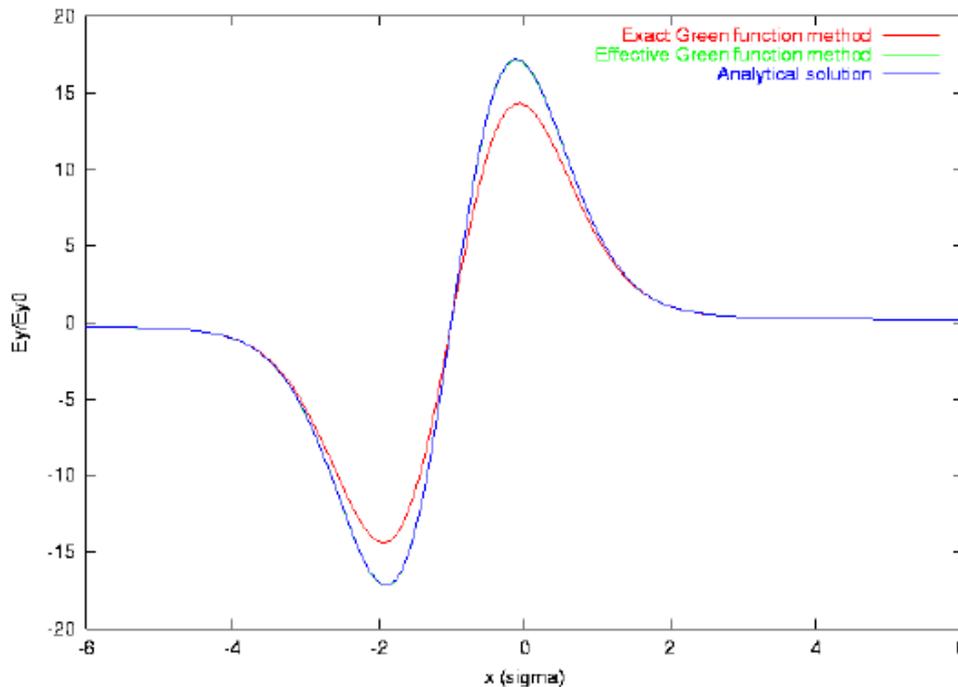
# Green Function Solution of Poisson's Equation (Integrated Green Function)

Integrated Green function Algorithm for large aspect ratio:

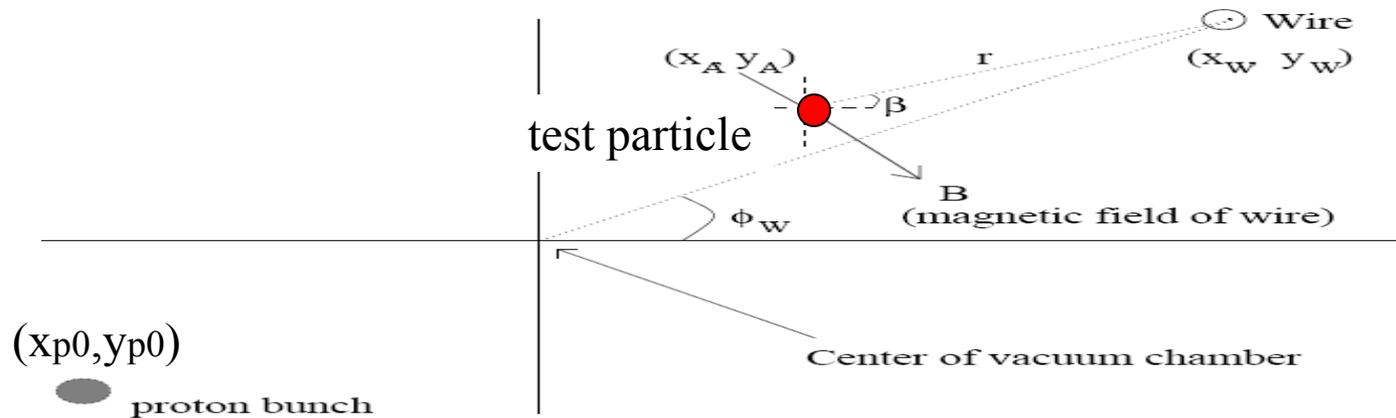
$$\phi_c(r_i) = \sum_{i'=1}^{2N} G_i(r_i - r_{i'}) \rho_c(r_{i'})$$

$$G_i(r, r') = \oint G_s(r, r') dr'$$

$E_y$



# Model of Conducting Wire Compensation



$$\Delta x'_{BB} = \frac{2N_p r_p}{\gamma_p} \frac{x_A - x_{P0}}{[(x_A - x_{P0})^2 + (y_A - y_{P0})^2]} \left\{ 1 - \exp\left[-\frac{1}{2\sigma^2}[(x_A - x_{P0})^2 + (y_A - y_{P0})^2]\right] \right\}$$

$$\Delta y'_{BB} = \frac{2N_p r_p}{\gamma_p} \frac{y_A - y_{P0}}{[(x_A - x_{P0})^2 + (y_A - y_{P0})^2]} \left\{ 1 - \exp\left[-\frac{1}{2\sigma^2}[(x_A - x_{P0})^2 + (y_A - y_{P0})^2]\right] \right\}$$

$$\Delta x'_W = -\frac{B_y L}{(B\rho)} = \frac{\mu_0 I_W L}{2\pi (B\rho)} \frac{x_W - x_A}{(x_W - x_A)^2 + (y_W - y_A)^2}$$

$$\Delta y'_W = \frac{B_x L}{(B\rho)} = \frac{\mu_0 I_W L}{2\pi (B\rho)} \frac{y_W - y_A}{(x_W - x_A)^2 + (y_W - y_A)^2}$$

$$x_W = x_{P0}, \quad y_W = y_{P0},$$

$$\frac{\mu_0 I_W L}{2\pi (B\rho)} = \frac{2N_p r_p}{\gamma_p} \Rightarrow I_W L = ecN_p$$

B.Erdelyi and T.Sen, "Compensation of beam-beam effects in the Tevatron with wires," (FNAL-TM-2268, 2004).

# Thin Lens Approximation for Crab Cavity Deflection

$$x^{n+1} = x^n$$

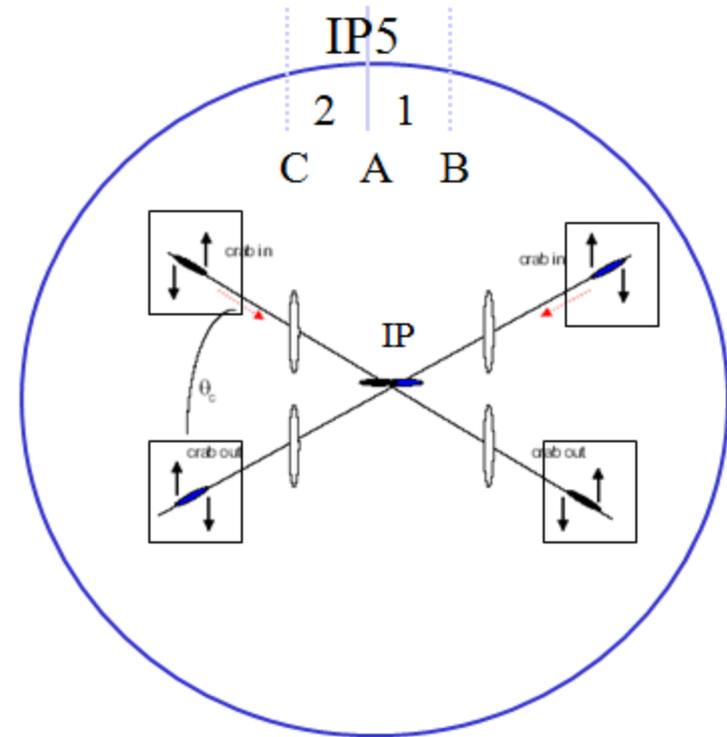
$$Px^{n+1} = Px^n + \frac{qV}{E_s} \sin(\omega z^n / c)$$

$$z^{n+1} = z^n$$

$$\delta E^{n+1} = \delta E^n + \frac{qV}{E_s} \cos(\omega z^n / c)$$

here:

$$V = \frac{cE_s \tan \phi}{\omega \sqrt{\beta_{x,crab} \beta_x^*}}$$



# ELIC e-p Nominal Parameters

## Simulation Model

- Single or multiple IP, head-on collisions
- Ideal rings for electrons & protons
  - Using a linear one-turn map
  - Does not include nonlinear optics
- Include radiation damping & quantum excitations in the electron ring

## Numerical Convergence Tests

to reach reliable simulation results, we need

- Longitudinal slices  $\geq 20$
- Transverse mesh  $\geq 64 \times 128$
- Macro-particles  $\geq 200,000$

## Simulation Scope and Limitations

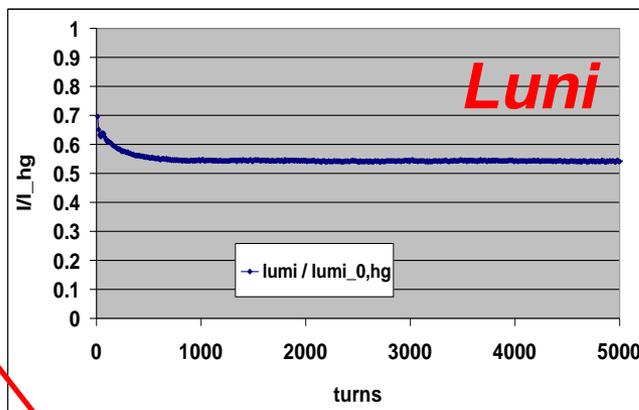
- 10k ~ 30k turns for a typical simulation run (multi-days of NERSC supercomputer)
- 0.15 s of storing time (12 damping times)
  - reveals short-time dynamics with accuracy
  - can't predict long term ( $> \text{min}$ ) dynamics

		Proton	Electron
Energy	GeV	150	7
Current	A	1	2.5
Particles	$10^{10}$	1.04	0.42
Hori. Emit., norm.	$\mu\text{m}$	1.06	90
Vert. Emit., norm.	$\mu\text{m}$	0.042	3.6
$\beta_x / \beta_y$	mm	5 / 5	5 / 5
$\sigma_x / \sigma_y$	$\mu\text{m}$	5.7/1.1	5.7/1.1
Bunch length	mm	5	5
Damping time	turn	---	800
Beam-beam parameter		0.002 0.01	0.017 0.086
Betatron tune $\nu_x$ and $\nu_y$		0.71 0.70	0.91 0.88
Synchrotron tune		0.06	0.25
Peak luminosity	$\text{cm}^{-2}\text{s}^{-1}$	7.87 x 10 <sup>34</sup>	
Luminosity with hour-glass effect	$\text{cm}^{-2}\text{s}^{-1}$	5.95 x 10 <sup>34</sup>	

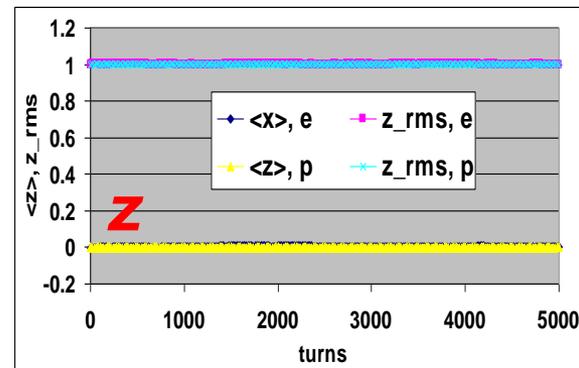
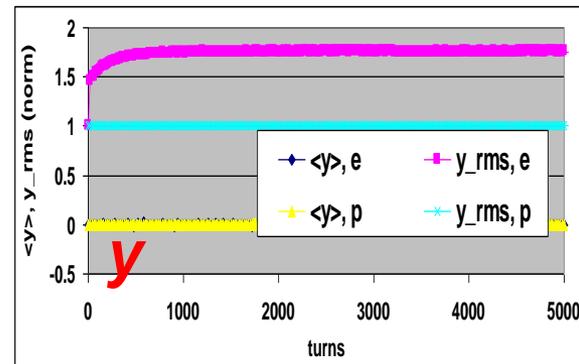
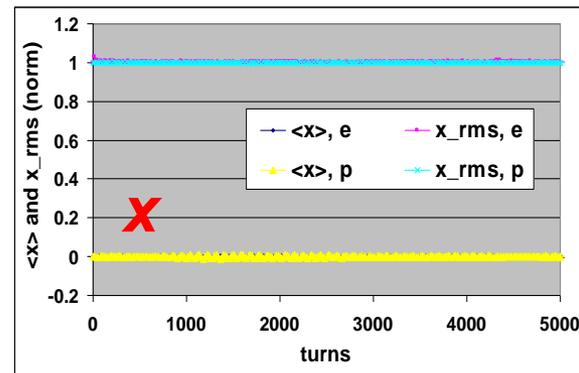
# Simulation Results: Nominal Parameters

- Simulations started with two Gaussian bunches with design parameters, reached equilibrium after one damping time
- No coherent beam-beam instability observed.
- Luminosity stabled at  $4.3 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  after damping time
- Sizes & lengths for both bunches remain design values except
- Vertical size & emittance of electron bunch increased by a factor of 1.8 and 2.7 respectively

	Electron	proton
Luminosity	$4.3 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$	
x_rms (norm)	1.00	1.00
x_emit (norm)	0.97	1.00
y_rms (norm)	<b>1.76</b>	1.00
y_emit (norm)	<b>2.73</b>	1.01
z_rms (norm)	1	1
z_emit (norm)	1	1
h. tune shift	0.017	0.002
v. tune shift	<b>0.087</b>	0.010

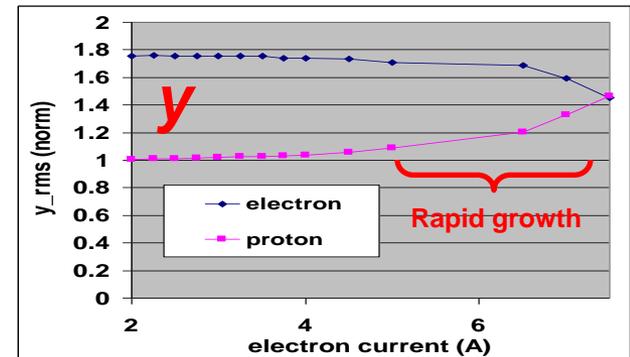
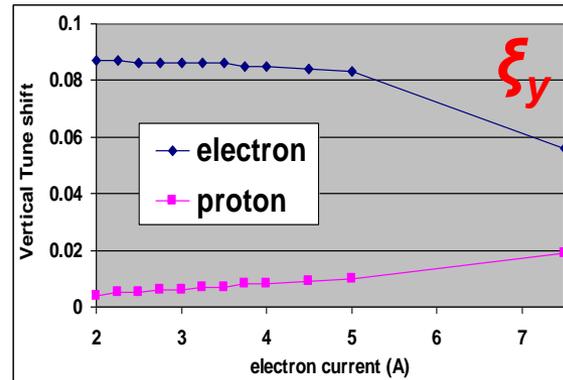
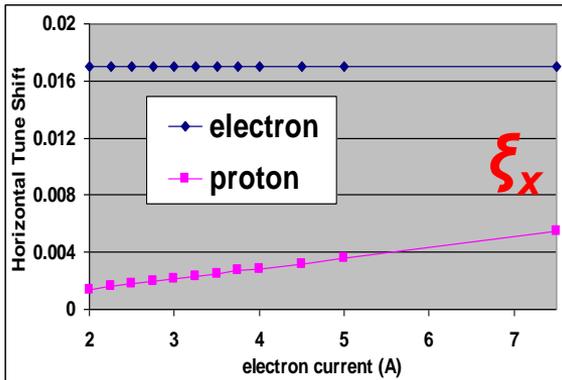
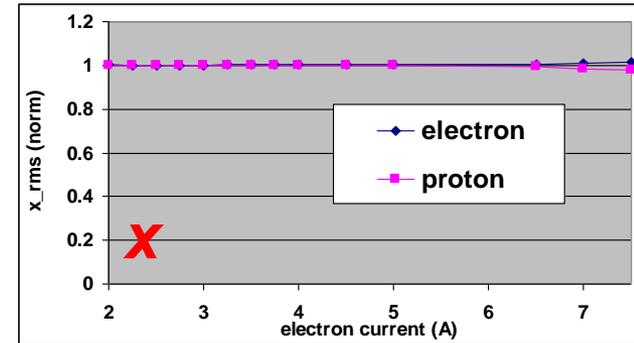
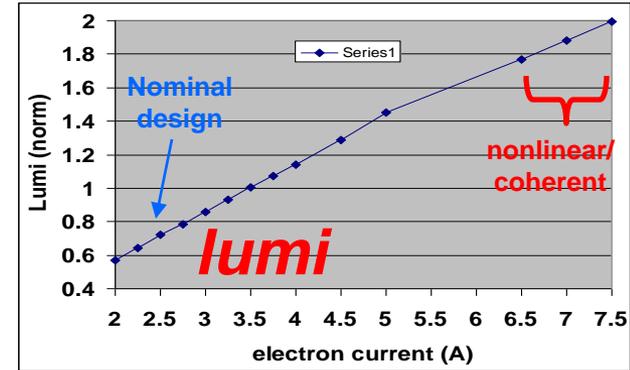


Normalized to design parameters



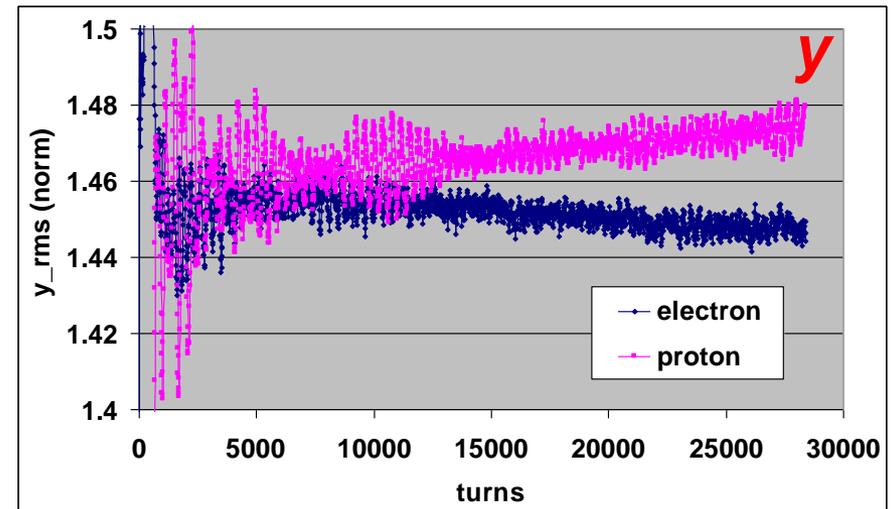
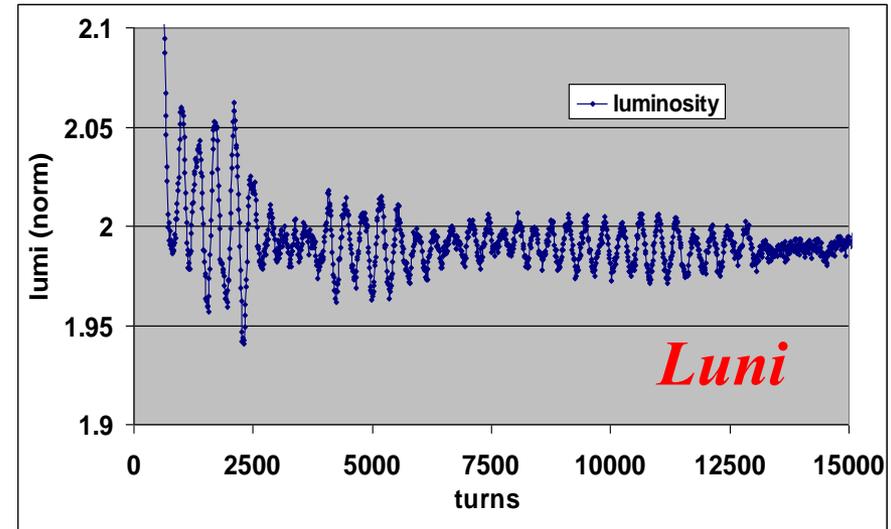
# Electron current dependence of Luminosity

- Increasing electron beam current by increasing bunch charge while bunch repetition rate remains the same, hence also increasing beam-beam interaction
- Luminosity increase as electron current almost linearly (up to 6.5 A)
- Proton bunch vertical size/emittance blowup when electron current is at above 7 A
- When electron beam reaches 5 A, proton dynamical vertical tune shift is 0.01 and above, while electron vertical tune shift goes down due to blowup of proton beam
- Coherent b-b instability observed at 7 ~ 7.5 A



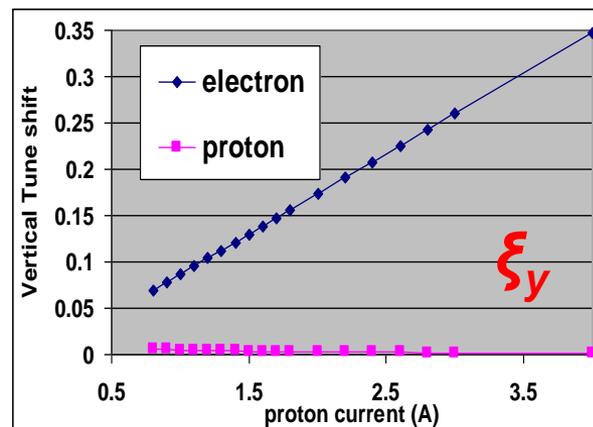
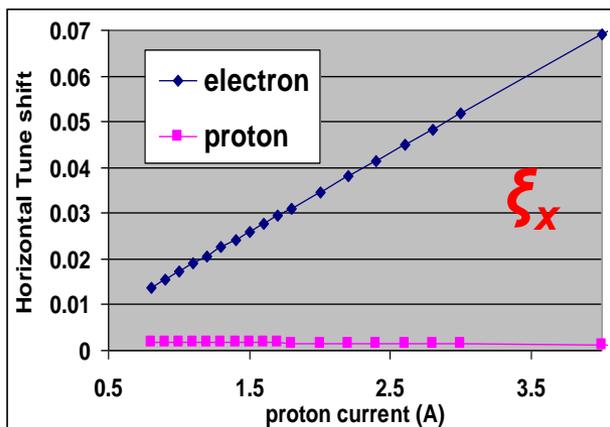
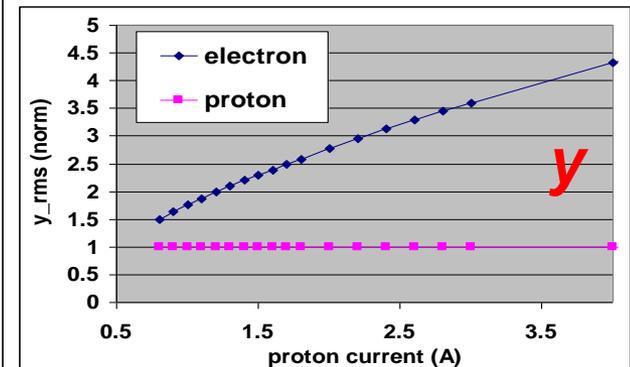
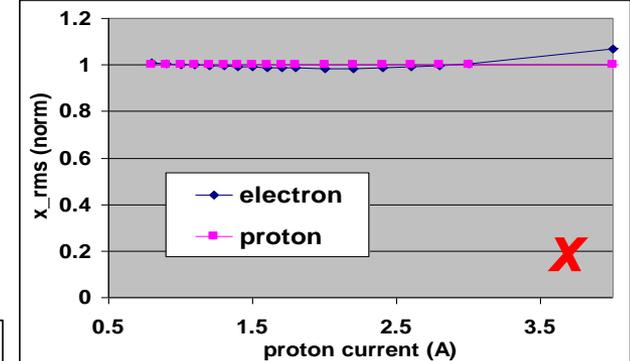
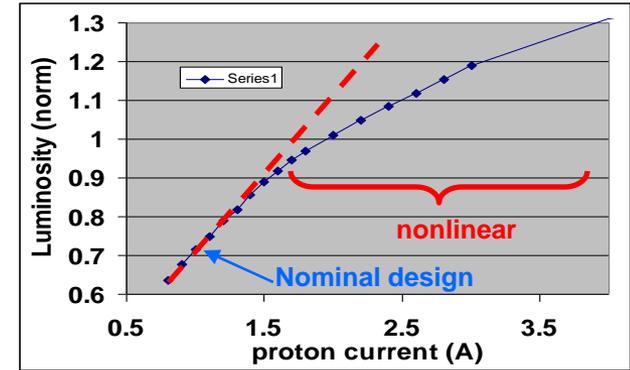
# Coherent Beam-Beam Instability

- Electron current is 7.5 A
- Coherent motion only in vertical size
- Not a dipole mode since  $\langle x \rangle = \langle y \rangle = 0$
- Proton vertical beam size blowup at and above this beam current value
- Period of coherent motion is a fraction of damping time



# Proton current dependence of Luminosity

- Increasing proton beam current by increasing proton bunch charge while bunch repetition rate remain same, hence also increasing beam-beam interaction
- Luminosity increase as proton beam current first approximately linearly (up to 1.5 A), then slow down as nonlinear beam-beam effect becomes important
- Electron beam vertical size/emittance increase rapidly
- Electron vertical and horizontal beam-beam tune shift increase as proton beam current linearly

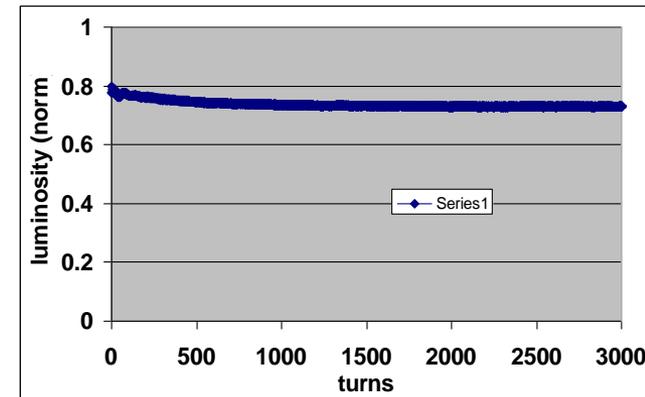
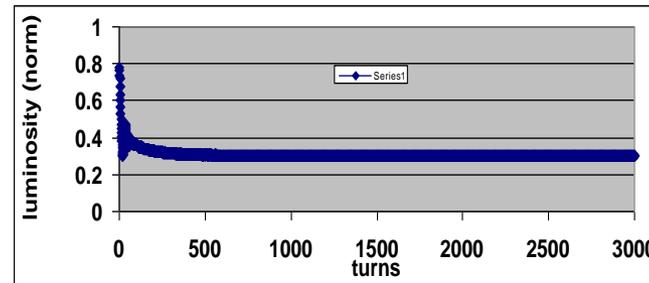
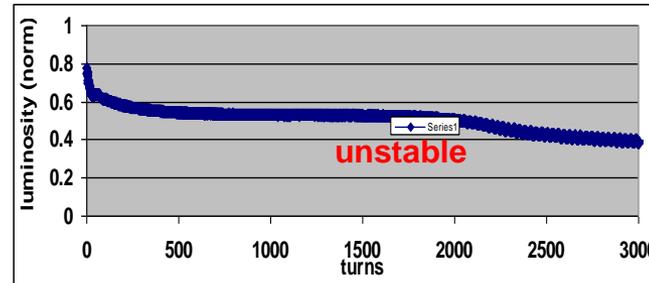
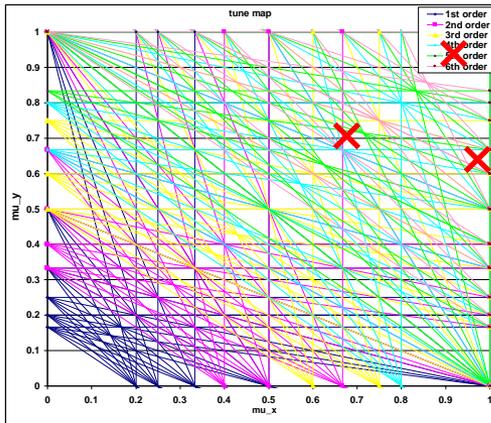


# Betatron Tune Working Point

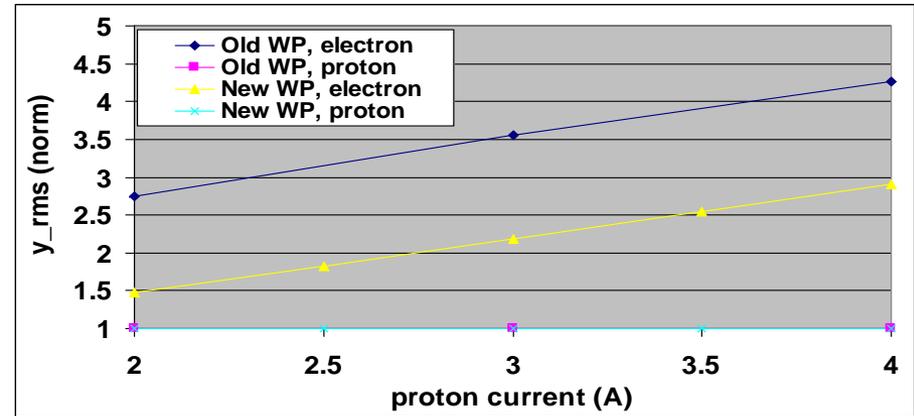
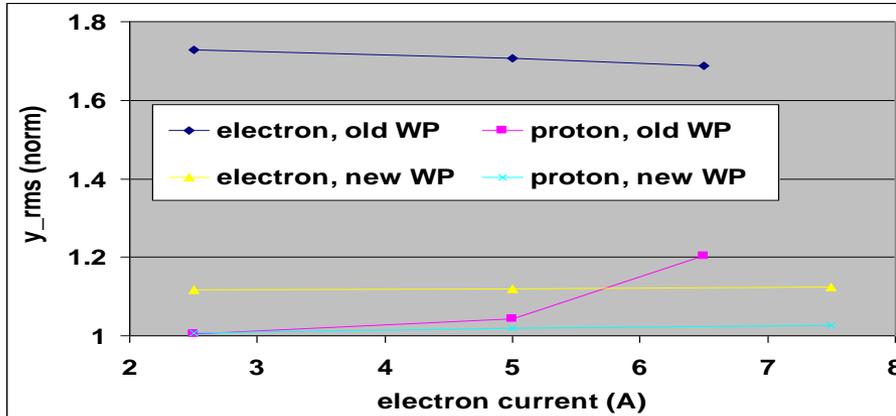
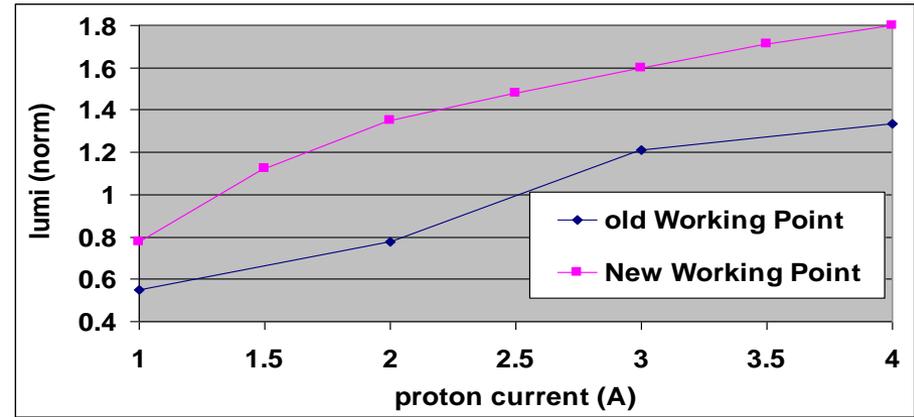
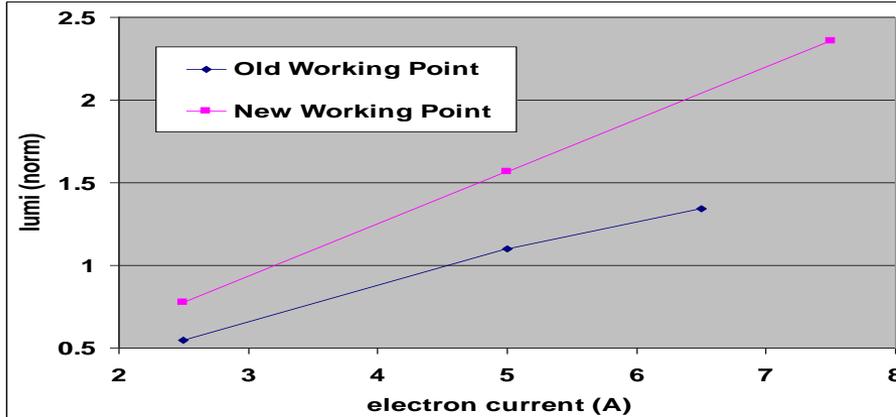
- Equilibrium luminosity strongly depends on synchrotron and betatron tune working point
- Working point should be away from synchrotron-betatron resonance lines
- Tune footprint, enlarged by beam-beam effect should avoid cross low order resonance lines
- Simulations have shown a *better working point*

Electron $\nu_x, \nu_y$	Proton $\nu_x, \nu_y$	Luminosity $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
0.91, 0.88	0.71, 0.7	4.15
0.71, 0.7	0.91, 0.88	3.22
0.73, 0.725	0.91, 0.9	Unstable
0.748, 0.75	0.91, 0.88	Unstable
0.63, 0.645	0.71, 0.7	5.77
0.91, 0.88	0.63, 0.645	Unstable
0.96, 0.46	0.71, 0.7	2.38

nominal



# New Working Point (cont.)



Simulation studies show

- systematic better luminosity over beam current regions with new working point,
- coherent instability is excited at same electron beam current,  $\sim 7$  A

# Multiple IPs and Multiple Bunches

## ELIC full capacity operation

- 4 interaction points, 1.5 GHz collision frequency
- 20 cm bunch spacing, over 10500 bunches stored for each beams
- Theoretically, these bunches are coupled together by collisions at 4 IPs
- Bunches may be coupled through other beam physics phenomena
- A significant challenges for simulation studies

## What concerns us

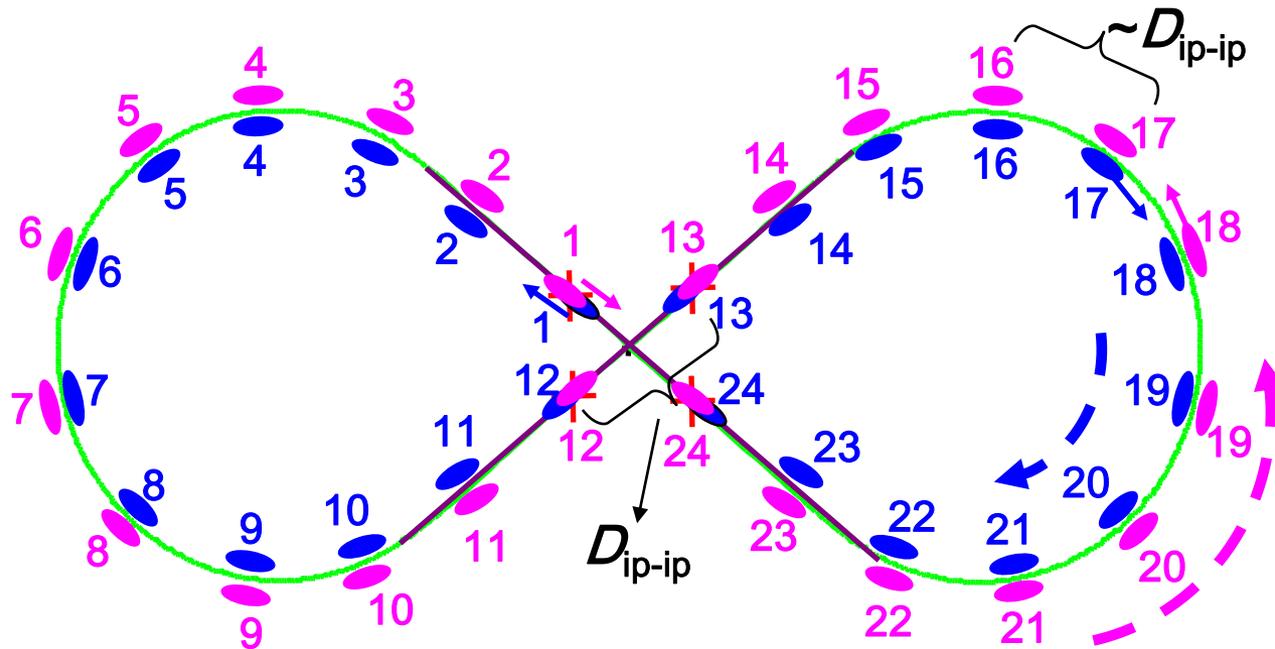
- Multiple bunch coupling
- Multiple IP effect
- Introducing new instability and effect on working point
- Earlier inciting of coherent beam-beam instability
- New periodicity and new coherent instability (eg. Pacman effect)

# Reduction of Coupled Bunch Set

ELIC ring cir.: ~ 2100 m, IP-IP distance: ~ 90 m      2100/90 ~23.3

Simplified model:      ring cir. = 24  $D_{ip-ip}$

- A 24-bunch set of one beam will collide with only a 24 bunch set of the other beam
- 10k bunches decoupled into multiple 24-bunch independent sets



# Multiple IPs and Multiple Bunches

Collision Table

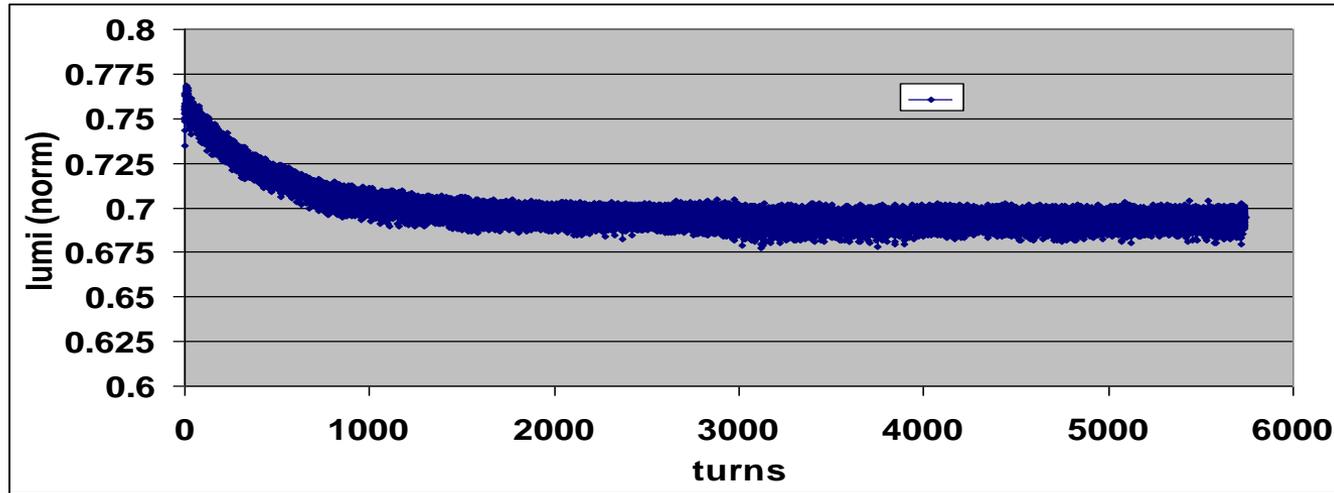
step	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
IP1	1 1	24 2	23 3	22 4	21 5	20 6	19 7	18 8	17 9	16 10	15 11	14 12	13 13	12 14	11 15	10 16	9 17	8 18	7 19	6 20	5 21	4 22	3 23	2 24
IP2	2 2	1 3	24 4	23 5	22 6	21 7	20 8	19 9	18 10	17 11	16 12	15 13	14 14	13 15	12 16	11 17	10 18	9 19	8 20	7 21	6 22	5 23	4 24	3 1
IP3	13 13	12 14	11 15	10 16	9 17	8 18	7 19	6 20	5 21	4 22	3 23	2 24	1 1	24 2	23 3	22 4	21 5	20 6	19 7	18 8	17 9	16 10	15 11	14 12
IP4	14 14	13 15	12 16	11 17	10 18	9 19	8 20	7 21	6 22	5 23	4 24	3 1	2 2	1 3	24 4	23 5	22 6	21 7	20 8	19 9	18 10	17 11	16 12	15 13

- Even and odd number bunches also decoupled
- When only one IP, one e bunch always collides one p bunch
- When two IPs opens on separate crossing straights and in symmetric positions, still one e bunch collides with one p bunch

## Full scale ELIC simulation model

- 12 bunches for each beam
- Collisions in all 4 IPs
- Bunch takes 24 steps for one complete turn in Figure-8 rings
- Total 48 collisions per turn for two 12-bunch sets

# Multiple IPs and Multiple Bunches (cont.)



- Simulated system stabilized (luminosity, transverse size/emittance) after one damping time (more than 100k collisions)
- Luminosity per IP reaches  $5.48 \times 10^{34} \text{ m}^{-1} \text{ s}^{-2}$ , a 5% additional loss over hour-glass effect
- Very small additional loss due to multiple-bunch coupling
- No coherent beam-beam instability observed at ELIC nominal design parameters
- More studies (parameter dependence, coherent instability, etc.) in progress

# Summary

- Beam-beam simulations were performed for ELIC ring-ring design with nominal parameters, single and multiple IP, head-on collision and ideal transport in Figure-8 ring
- Simulation results indicated stable operation of ELIC over simulated time scale (10k ~ 25k turns), with equilibrium luminosity of  $4.3 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ , roughly 25% reduction for each of hour-glass and beam-beam effects
- Studies of dependence of luminosity on electron & proton beam currents showed that the ELIC design parameters are safely away from beam-beam coherent instability
- Search over betatron tune map revealed a better working point at which the beam-beam loss of luminosity is less than 4%, hence an equilibrium luminosity of  $5.8 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Multiple IP and multiple bunch simulations have not shown any new coherent instability. The luminosity per IP suffers only small decay over single IP operation

# Outlook

- Toward more realistic model of beam transport
  - Needs of including real lattice and magnet imperfections
  - Trade-off (due to computing power limit): full particle-tracking in ring and weak-strong beam model
  - Short term accurate vs. long term (inaccurate) behavior
- Move to space charge dominated low ion energy domain
  - pancake approximation of beam-beam force vs. full 3D mash calculation
  - New limit = Laslett tune-shift + beam-beam tune-shift ?
- Advanced interaction region design
  - Crab crossing
  - Traveling focusing
  - Crab waist

# Future Plan

- Continuation of code validation and benchmarking
- Single IP and head-on collision
  - Coherent beam-beam instability
  - Synchrot-betatron resonance and working point
  - Including non-linear optics and corrections
- Multiple IPs and multiple bunches
  - Coherent beam-beam instability
- Collisions with crossing angle and crab cavity
- Beam-beam with other collective effects
  
- Part of SciDAC COMPASS project
- Working with LBL and TechX and other partners for developing and studying beam dynamics and electron cooling for ELIC conceptual design

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