

# Microbunching Instability in FEL Linear Accelerators

***Zhirong Huang (SLAC)***



**October 20, 2005**

**presented at**

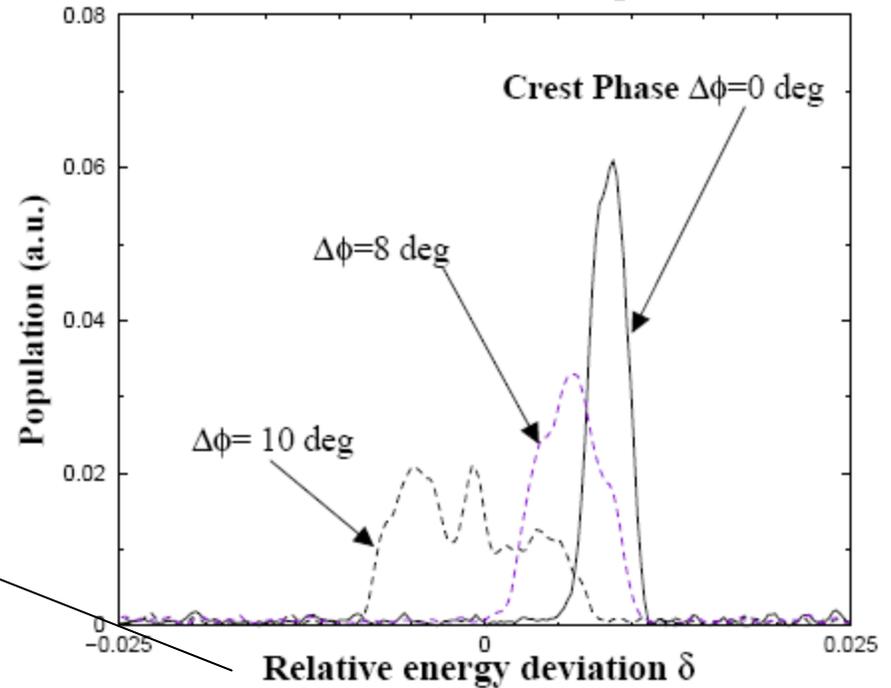
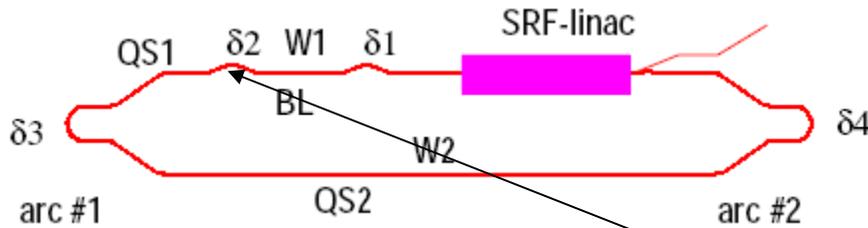


# Outline

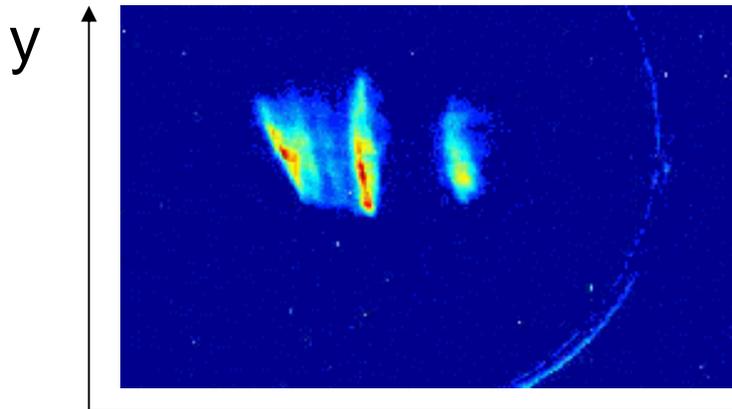
- Introduction
- Microbunching instability driven by CSR and LSC
- LCLS analysis and cures
- DUV-FEL beam modulation studies
- Conclusions

# Microbunch structures observed after compression

- JLab (*Piot et al., EPAC 2000*)



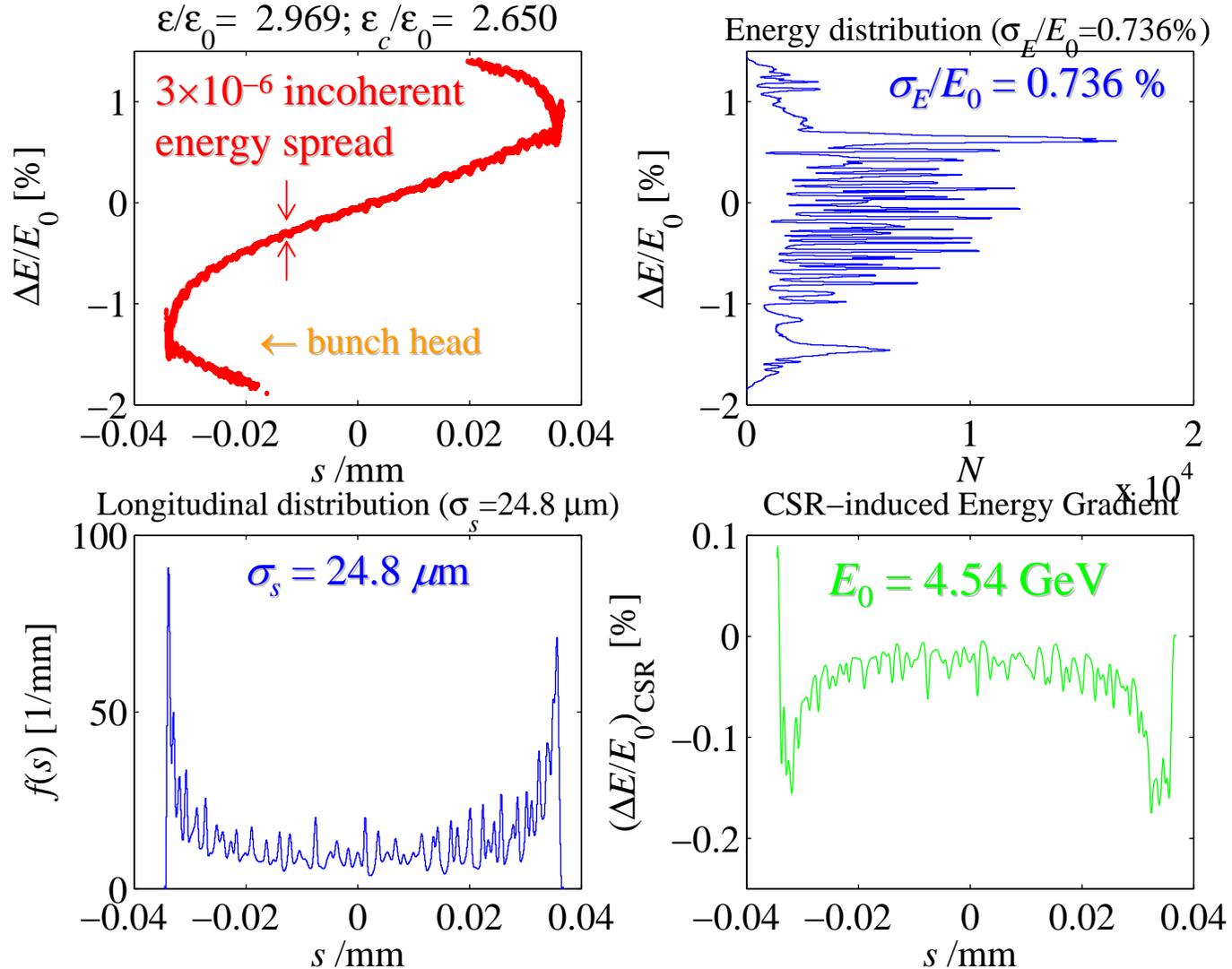
- Similar longitudinal structures at TTF and DUV-FEL



(*Graves et al. PAC 2001*)

x (energy and time)

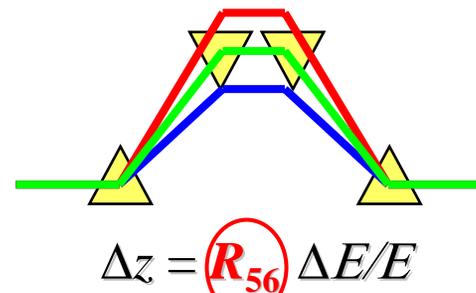
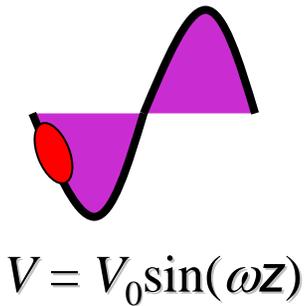
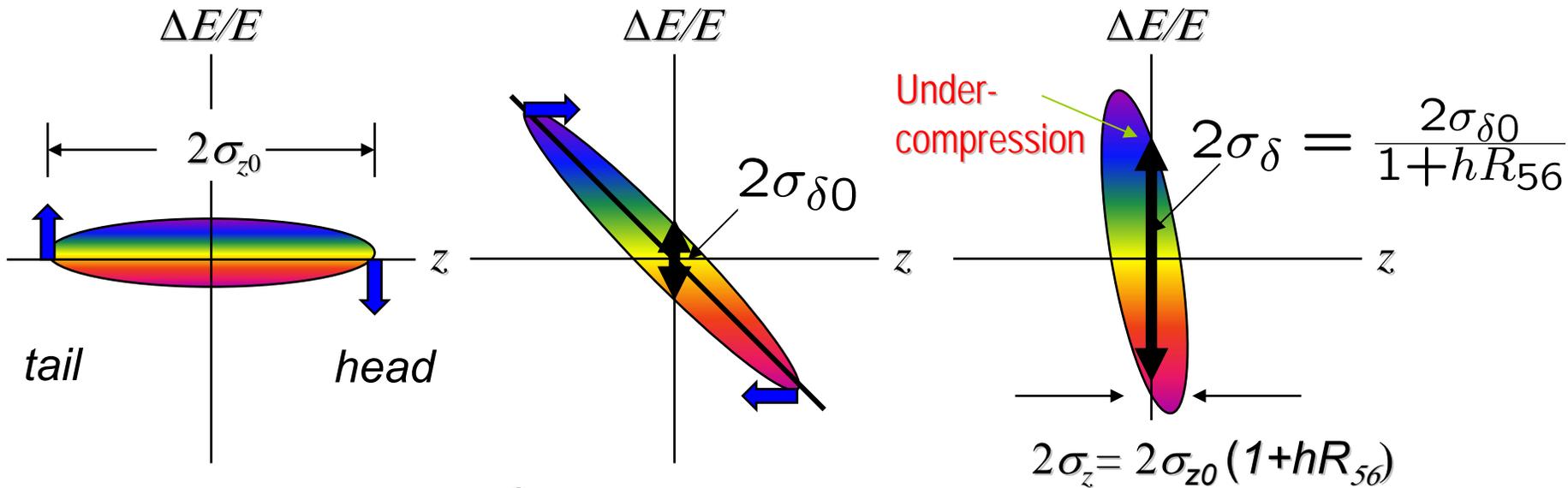
# LCLS Distribution After BC2 Chicane



# Introduction

- FEL interaction in the undulator requires very bright electron beams (high current, small emittance and energy spread)
- Such a bright beam interacting with self-fields in the accelerator may be subject to undesirable instabilities
- Bunch compressors designed to increase the peak current can give rise to a microbunching instability that may degrade the beam quality significantly
- This talk discusses physics of this instability, how to suppress it for short-wavelength FELs, and some experimental evidence relevant to the instability

# Bunch compression



RF Accelerating Voltage

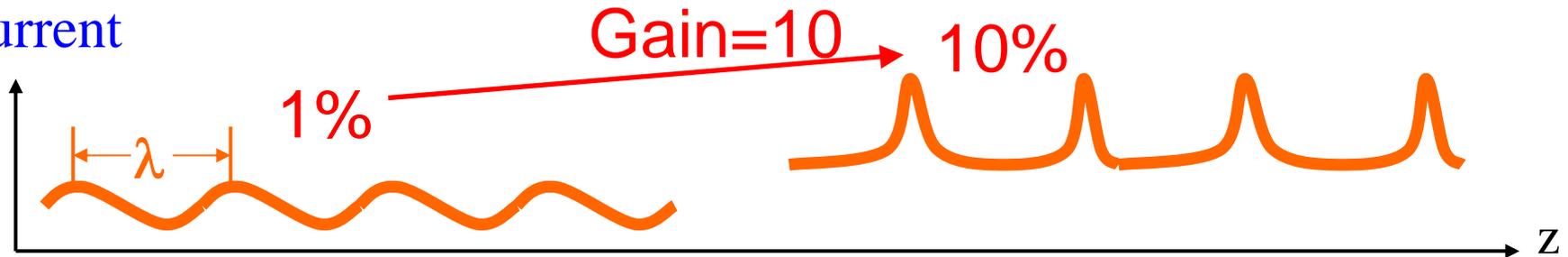
Path Length-Energy Dependent Beamline

linear "chirp"  $h = \frac{\Delta E/E}{\Delta z} < 0$

# Instability mechanism

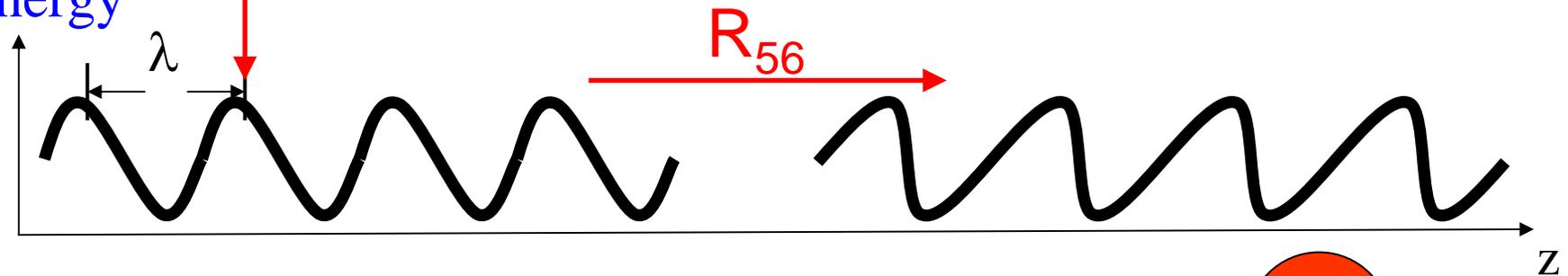
- Initial density modulation induces energy modulation through longitudinal impedance  $Z(k)$ , converted to more density modulation by a compressor (*Saldin, Schneidmiller, Yurkov, NIMA, 2002*)

Current



Impedance

Energy

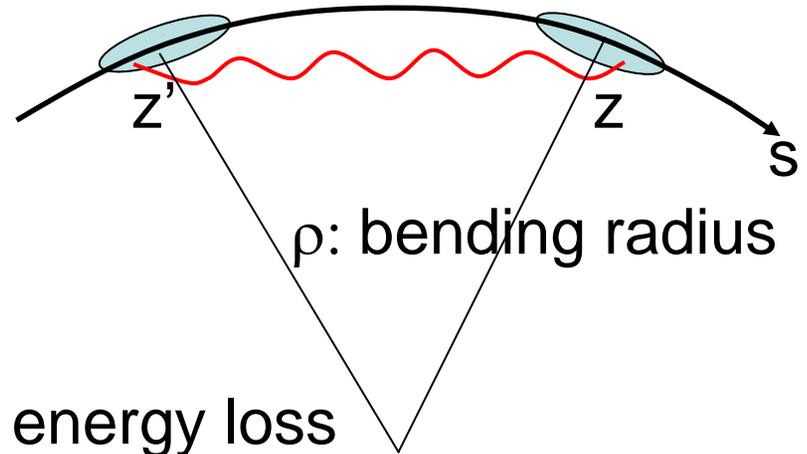


→ growth of slice energy spread (and emittance)



# CSR wake and impedance

- Powerful radiation generated for  $\lambda \sim$  bunch length or bunch micro-structure lengths
- Radiation from bunch tail catch up the head, increase energy spread and emittance



- Steady-state, line-charge CSR energy loss

$$\frac{d(\Delta E)}{ds} = -\frac{e}{4\pi} \int_{-\infty}^z \underbrace{\frac{2Z_0}{3\rho^{2/3}(z-z')^{1/3}}}_{\text{CSR wake}} \frac{dI}{dz'} dz'$$

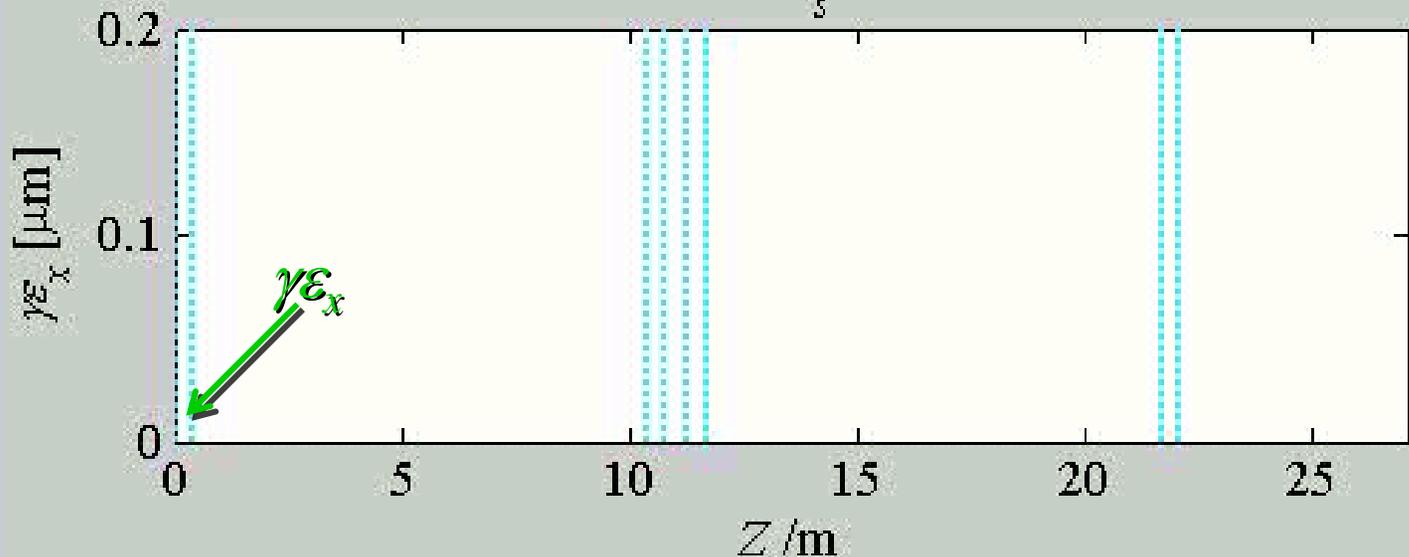
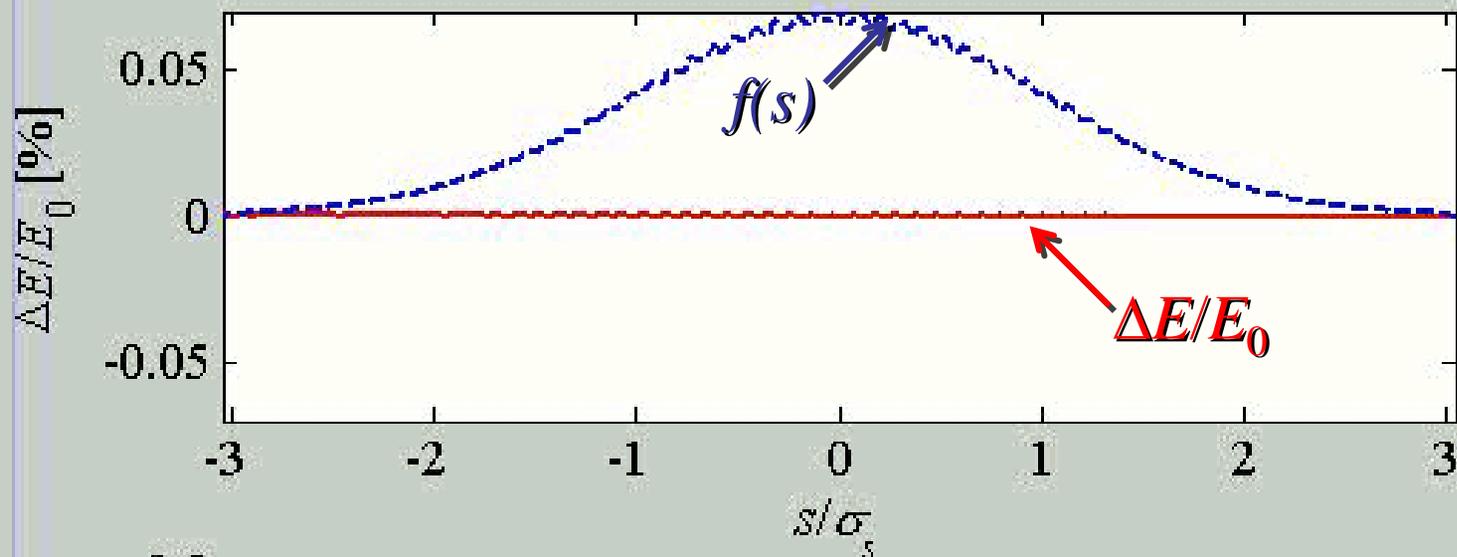
CSR “wake”, stronger at smaller scale

- Longitudinal CSR impedance  $Z(k)$  ( $k = 2\pi/\lambda$ )

$$Z_{CSR} = -iA \frac{cZ_0}{4\pi} \frac{k^{1/3}}{\rho^{2/3}}$$

*Derbenev et al., 1995*  
*Murphy et al., PAC 1995*

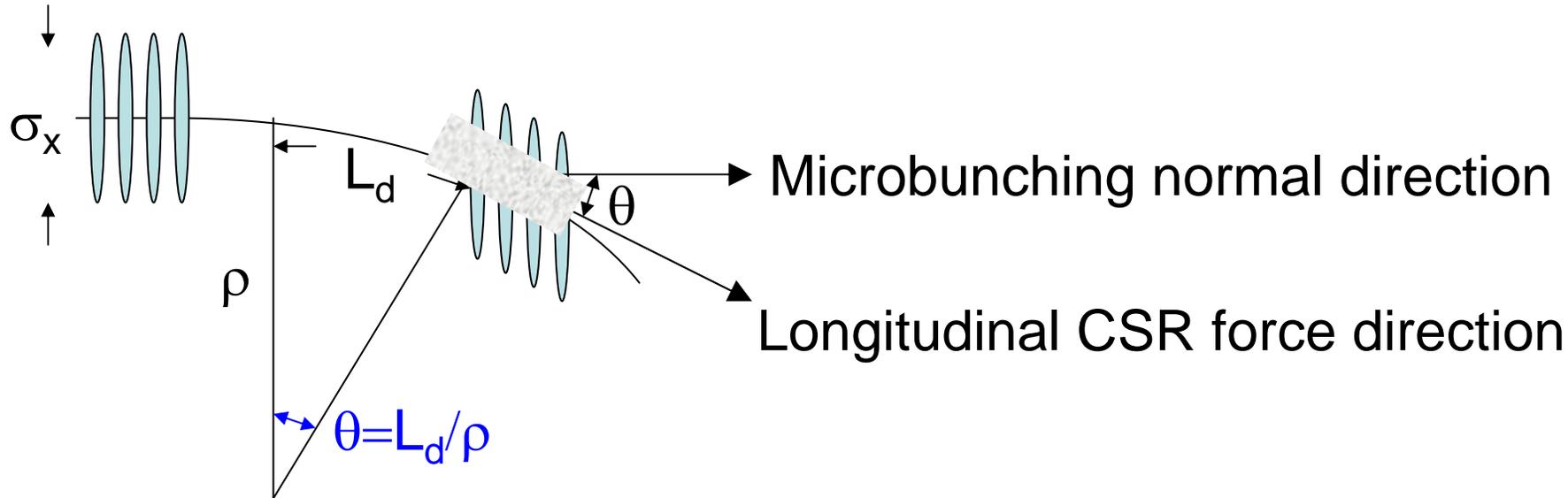
# CSR Microbunching Movie



courtesy P. Emma

# Emittance damping to CSR microbunching

- Consider a microbunched beam moving in a dipole



- Characterize density modulation by a bunching factor

$$b(k) = \frac{1}{N_{ec}} I(k) = \frac{1}{N_{ec}} \int_{-\infty}^{\infty} I(z) e^{-ikz} dz$$

- Smearing of microbunching when projected to longitudinal  $z$  direction in the bend

$$\frac{L_d}{\rho} \sigma_x = \frac{L_d}{\rho} \sqrt{\epsilon_x \beta} \sim \lambda/2\pi$$

# Integral equation and approx. solution

- Linear evolution of  $b(k;s)$  governed by an integral equation

$$b(k(s);s) = b_0(k(s);s) + \int_0^s d\tau K(\tau,s)b(k(\tau);\tau)$$

$$\text{kernel } K(\tau,s) = ik(s)R_{56}(\tau \rightarrow s) \frac{I(\tau)}{\gamma I_A} Z(k(\tau)) \times \underbrace{\exp(\dots \varepsilon, \sigma_\delta \dots)}_{\text{Landau damping}}$$

- Iterative solution for a 3-dipole chicane

$$b(k;s) = b_0(k;s) + \underbrace{\int_0^s ds' K(s',s)b_0(k';s')}_{\text{one - stage amplification}}$$

$$\frac{I_f(1 \rightarrow 3) + I_f(2 \rightarrow 3)}$$

$$+ \underbrace{\int_0^s ds' K(s',s) \int_0^{s'} ds'' K(s'',s') b_0(k'';s'')}_{\text{two - stage amplification}}$$

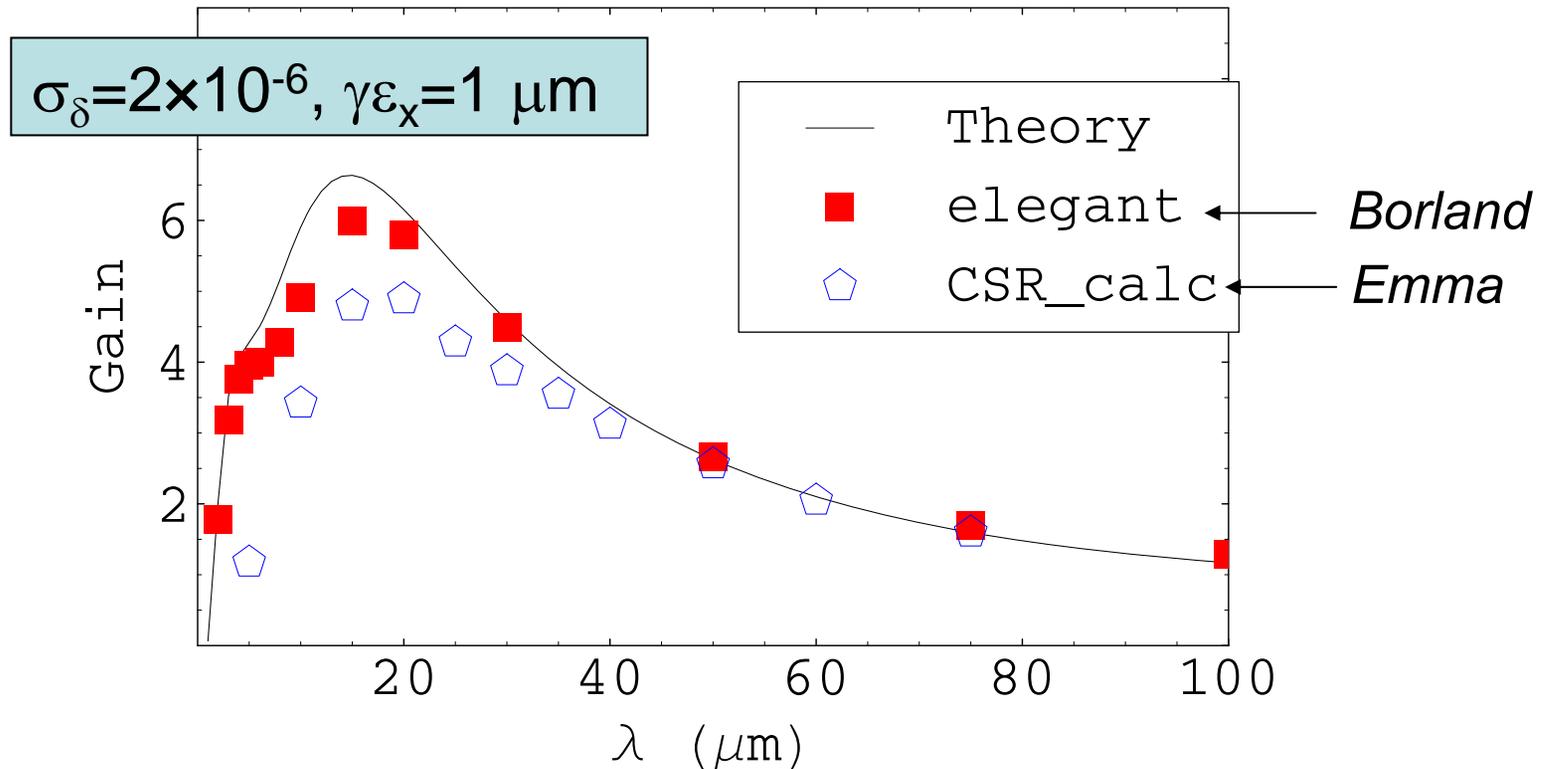
$$I_f^2(1 \rightarrow 2 \rightarrow 3)$$

• Heifets, Stupakov, Krinsky  
PRST, 2002;

• Huang, Kim, PRST, 2002

# Numerical example: Berlin Benchmark

- Elegant and CSR\_calc (matlab based) codes used
- a few million particles are loaded with 6D quiet start
- CSR algorithm based on analytical wake models



- More about CSR, see <http://www.desy.de/csr/>

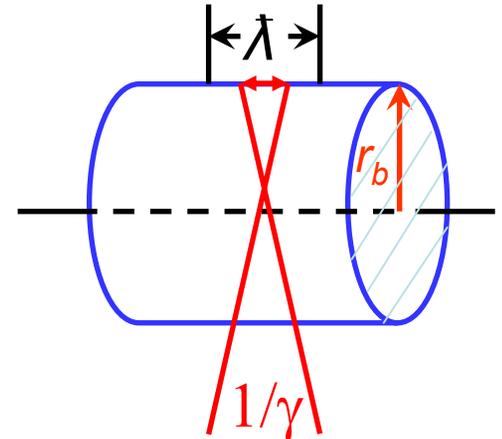
# LSC Impedance

- Free-space longitudinal space charge impedance

$$Z(k) = \frac{4i}{kr_b^2} \left[ 1 - \frac{kr_b}{\gamma} K_1 \left( \frac{kr_b}{\gamma} \right) \right]$$

$$= \frac{4i}{kr_b^2} \text{ if } \frac{kr_b}{\gamma} \gg 1$$

$$= \frac{ik}{\gamma^2} \left( 1 + 2 \ln \frac{\gamma}{r_b k} \right) \text{ if } \frac{kr_b}{\gamma} \ll 1$$



- At low energy in the injector region, space charge oscillation dynamics (typically requires careful SC simulations)
- At higher linac energy, beam density modulation freezes and energy modulation accumulates due to LSC, can dominate microbunching gain at very high frequencies (*Saldin, Schneidmiller, Yurkov, NIMA, 2004*)
- CSR impedance much stronger than LSC, but LSC instability is not subject to emittance damping (chicane is achromat)

# LSC instability gain and Landau damping

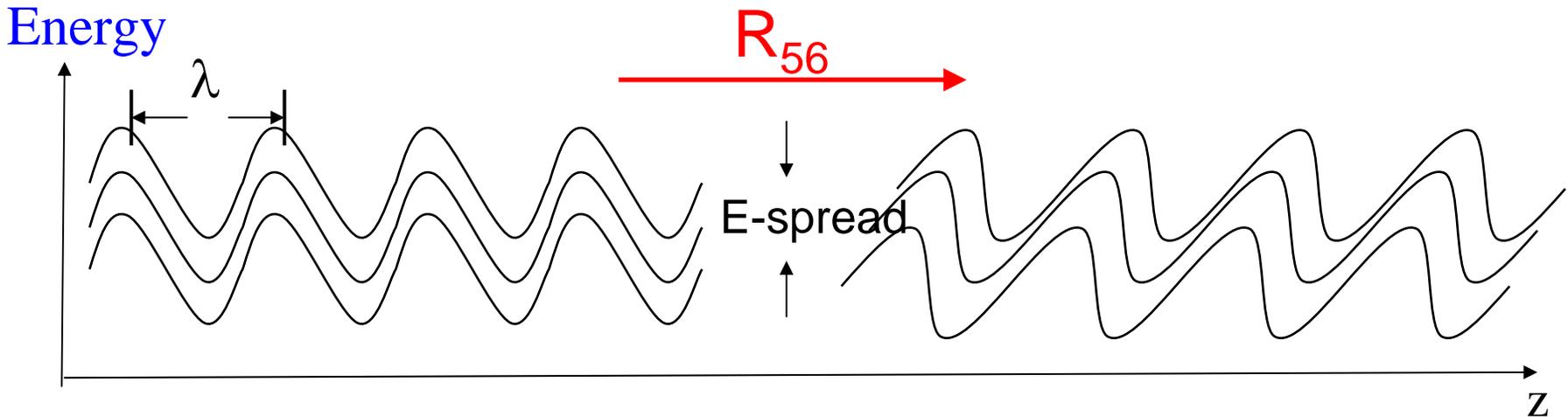
- Gain due to upstream impedances (LSC, linac wake)

$$G \equiv \left| \frac{b_f}{b_0} \right|$$

$$= \frac{I_0}{\gamma I_A} |k_f R_{56} \int_0^L ds Z(k_0; s)| \exp \left( -\frac{1}{2} k_f^2 R_{56}^2 \sigma_\delta^2 \right)$$

- No emittance damping!

local energy spread

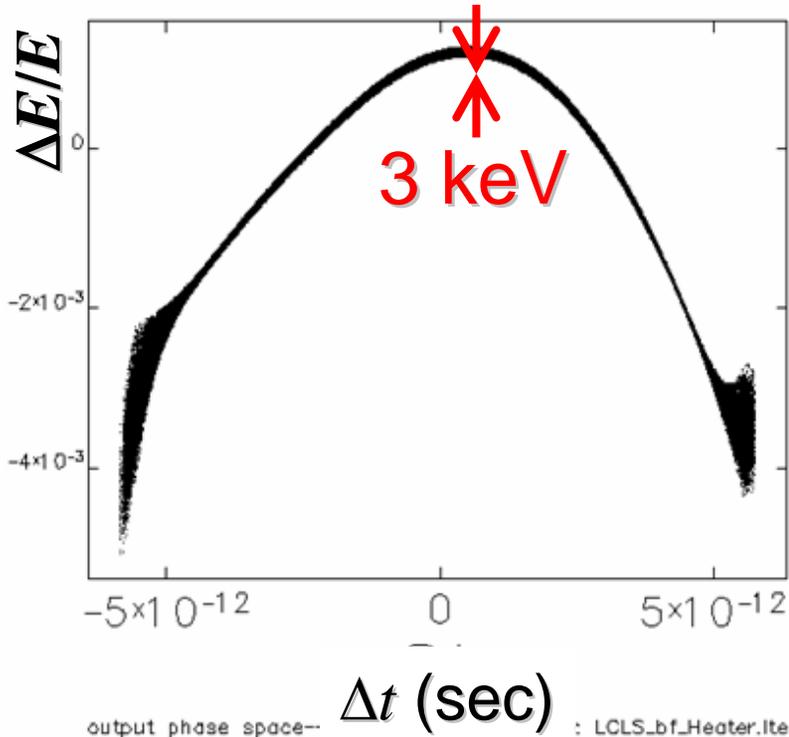


- All beams have finite incoherent (uncorrelated) energy spread, smearing of microbunching occurs if

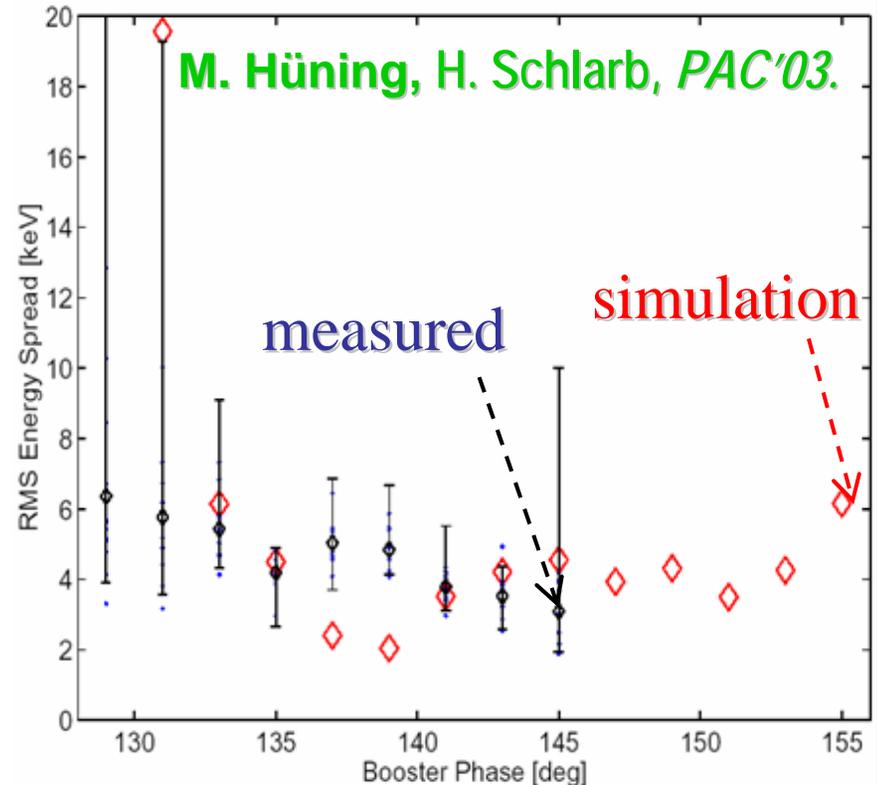
$$R_{56} \left( \frac{\Delta E}{E} \right)_{inc} \sim \lambda / (2\pi)$$

# Uncorrelated energy spread of PC RF gun

Parmela at 1 nC



TTF measurement at 4 nC



- “Intrinsic” energy spread mostly generated from r-dependent LSC force in the gun (*Huang et al., PAC 2005*)
- 3 keV (rms), accelerated to 14 GeV, & compressed  $\times 32$   
 $\Rightarrow 3 \times 10^{-6} \times 32 / 14 < 1 \times 10^{-5}$  relative energy spread

# Heating within FEL tolerance

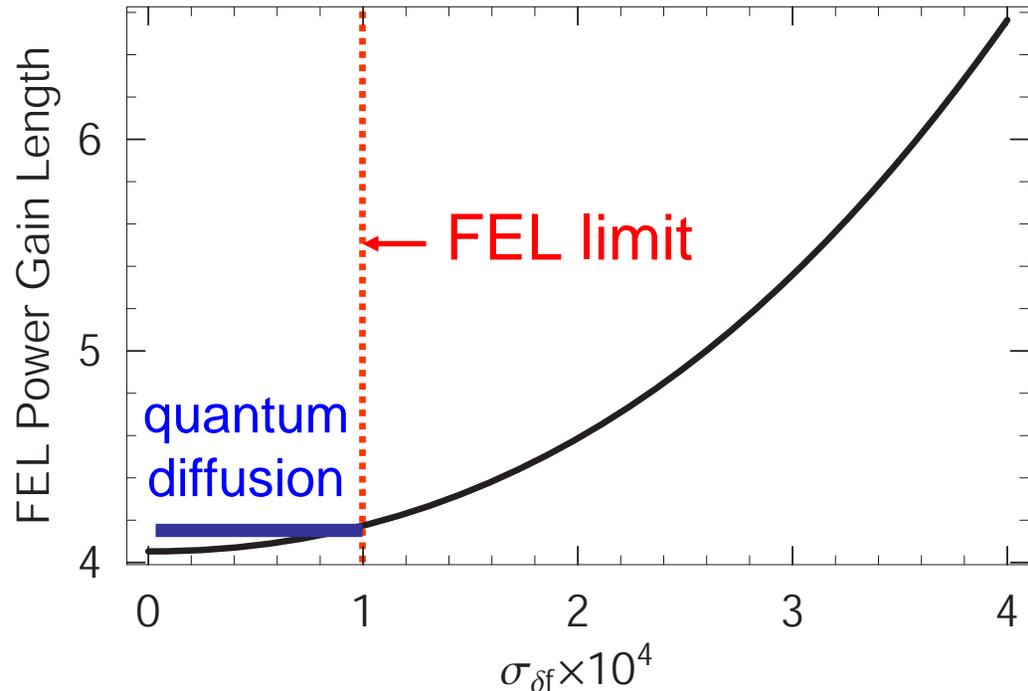
- LCLS FEL parameter  $\rho \sim 5 \times 10^{-4}$ , not sensitive to energy spread until  $\sigma_\delta \sim 1 \times 10^{-4}$

M. Xie's fitting formula

$$\gamma\varepsilon = 1.2 \mu\text{m}$$

$$I_p = 3.4 \text{ kA}$$

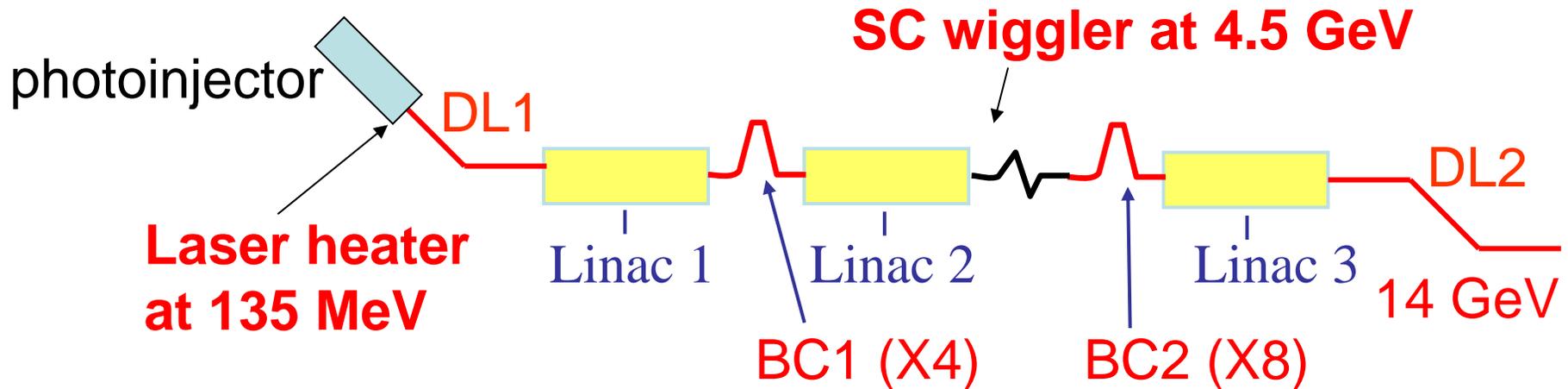
$$\beta = 20 \text{ m}$$



- $10^{-5}$  “intrinsic” energy spread too small and cannot be used in LCLS undulator due to QE (no effect on FEL gain when  $< 10^{-4}$ )

**→ can increase  $\sigma_\delta$  by a factor of 10 without FEL degradation in order to suppress microbunching instability**

# LCLS accelerator systems

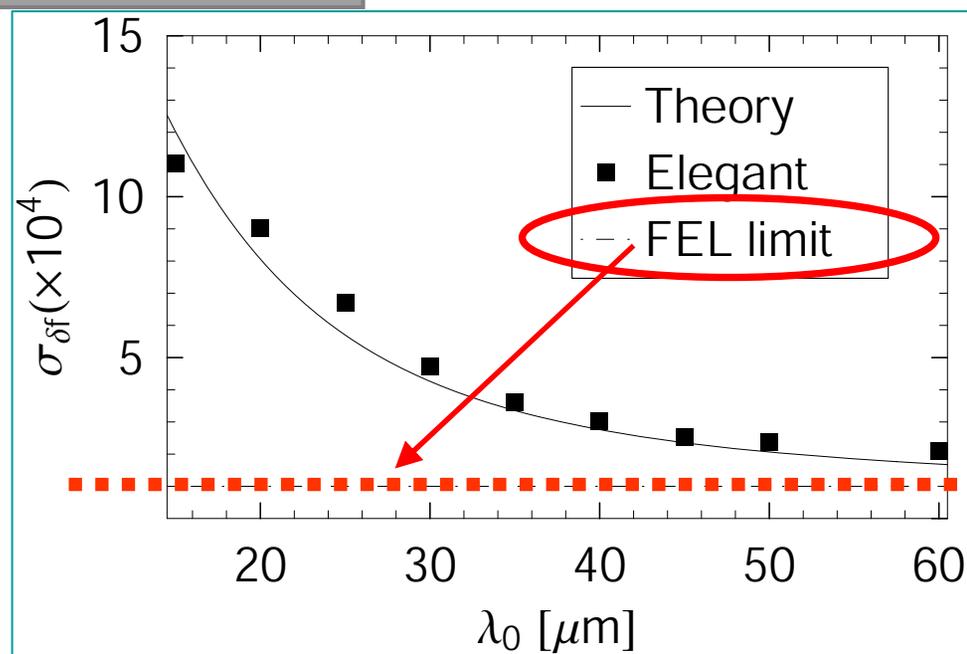
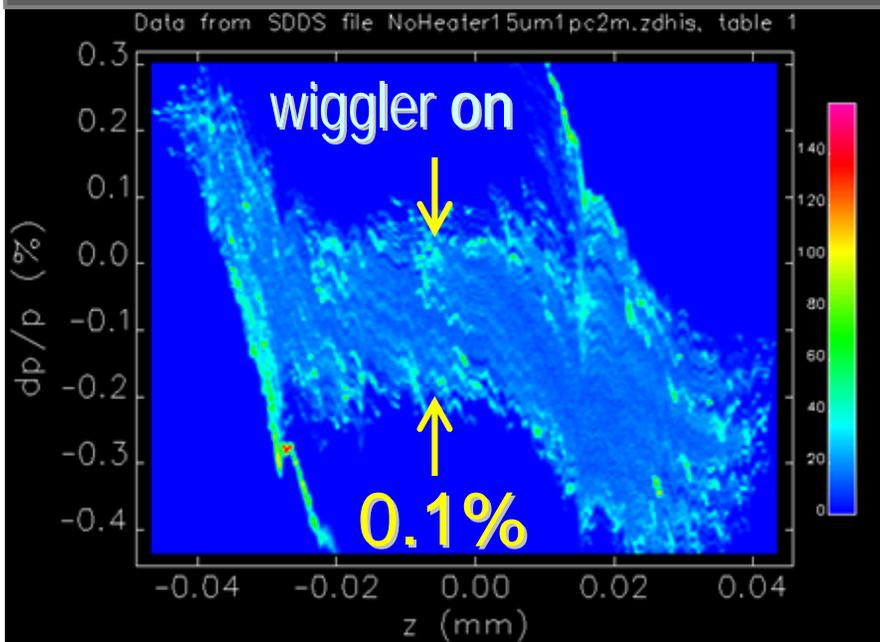


- Two bunch compressors to control jitters and wakefield effect
- Impedance sources: LSC, CSR, and linac wakefields
- Two Landau damping options (to increase E-spread 10X)
  - a SC wiggler before BC2 to suppress CSR microbunching
  - or a laser heater for LSC instability (suggested by Saldin et al.)

# Growth of slice energy spread

- High BC1 gain  $\rightarrow$  significant energy modulation in Linac-2
- $\rightarrow$  temporally smearing in BC2 to become effective slice energy spread ( $\rightarrow$  SC wiggler too late)

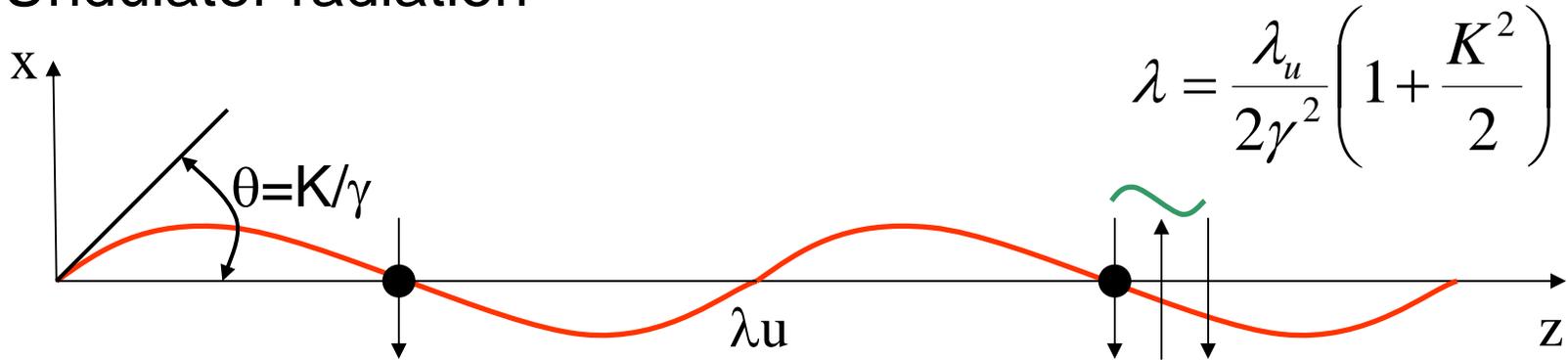
Final long. phase space at 14 GeV for initial 15- $\mu\text{m}$  1% modulation at 135 MeV



**Need  $\sim 0.1\%$  initial density modulation at injector end or suppress BC1 gain effectively**

# Beam-radiation interaction in an undulator

- Undulator radiation



- FEL interaction: energy exchange between e- and field ( $\mathbf{v} \cdot \mathbf{E} = v_x E_x$ ) can be sustained due to the resonant condition
- Some e- loss energy, others gain → energy modulation with a relative amplitude

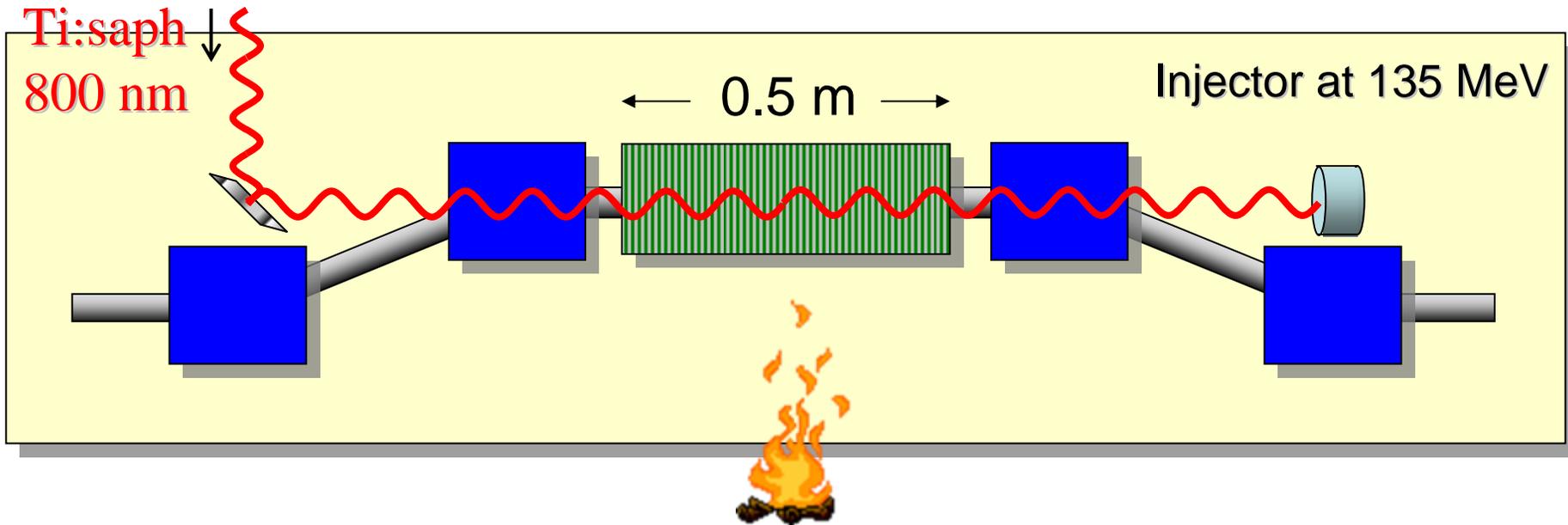
$$\delta_L(r) = \sqrt{\frac{P_L}{P_0} \frac{K L_u}{\gamma_0^2 \sigma_r}} [\text{JJ}] \exp\left(-\frac{r^2}{4\sigma_r^2}\right)$$

laser peak power

8.7 GW

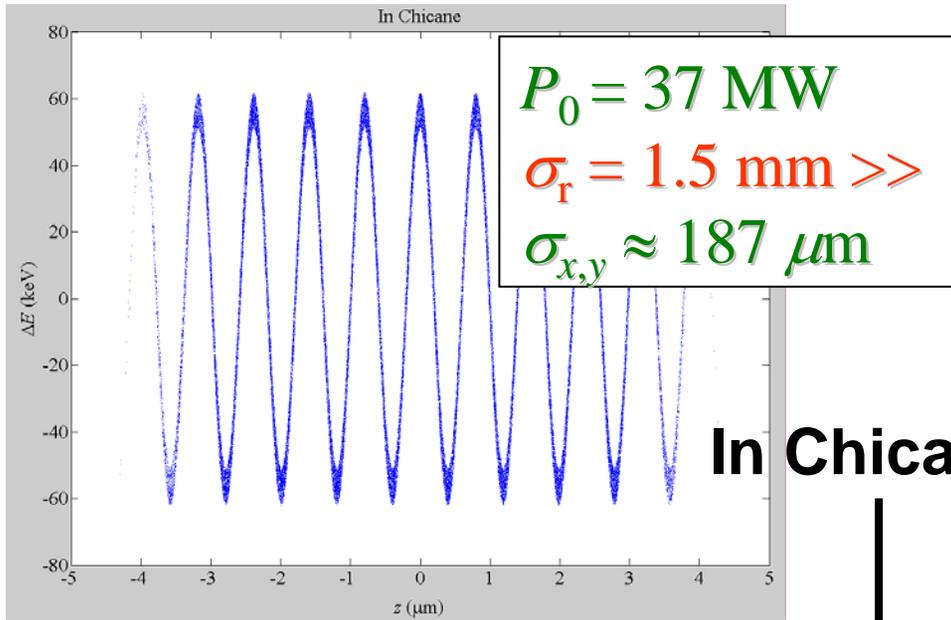
laser rms spot size

# LCLS laser heater design

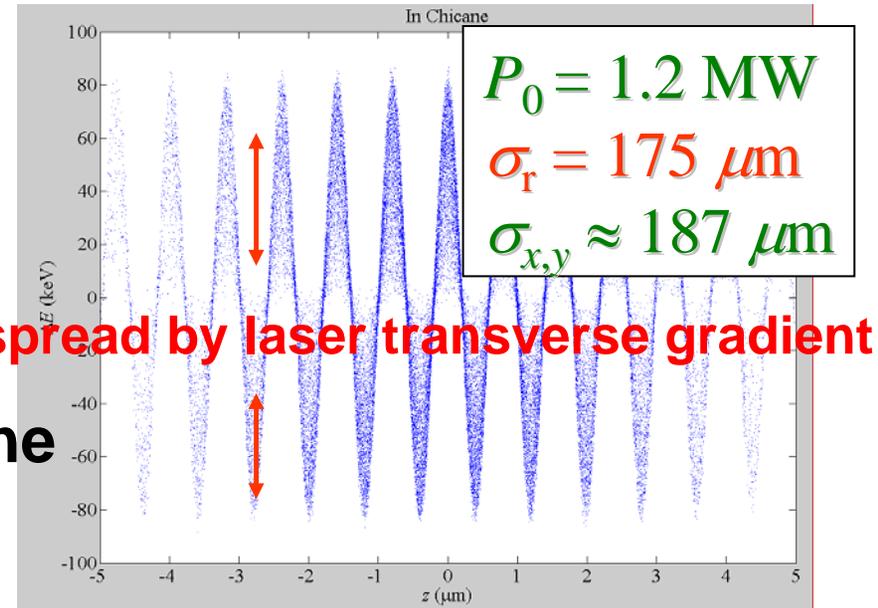


- Laser-electron interaction in an undulator induces rapid energy modulation (at 800 nm), to be used as effective energy spread before BC1 (3 keV  $\rightarrow$  40 keV rms)
- Inside a weak chicane for easy laser access, time-coordinate smearing (Emittance growth is negligible)

# Large laser spot size



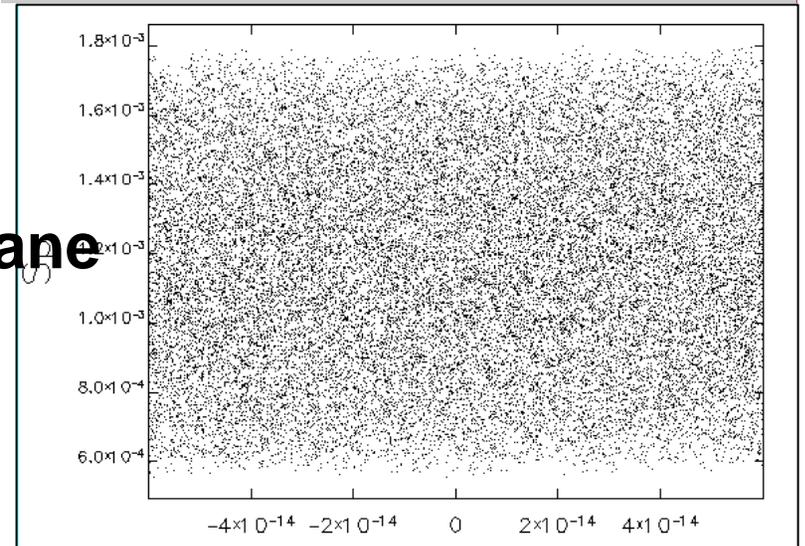
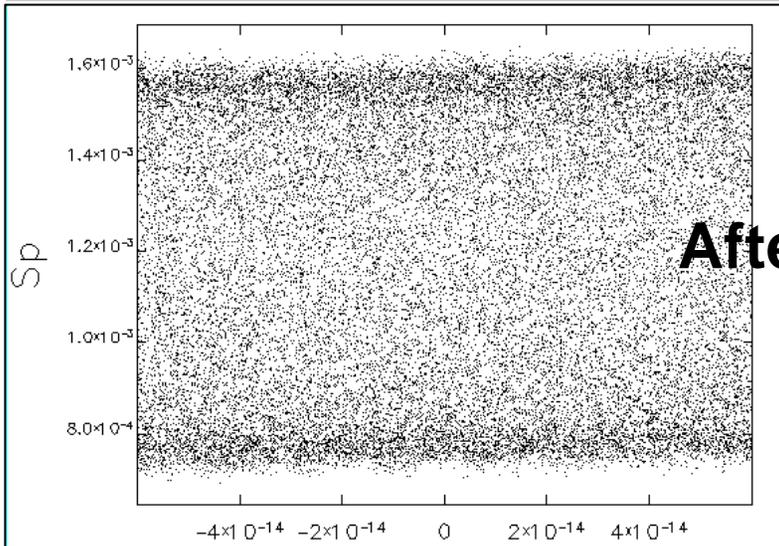
# Matched laser spot size



In Chicane



After Chicane

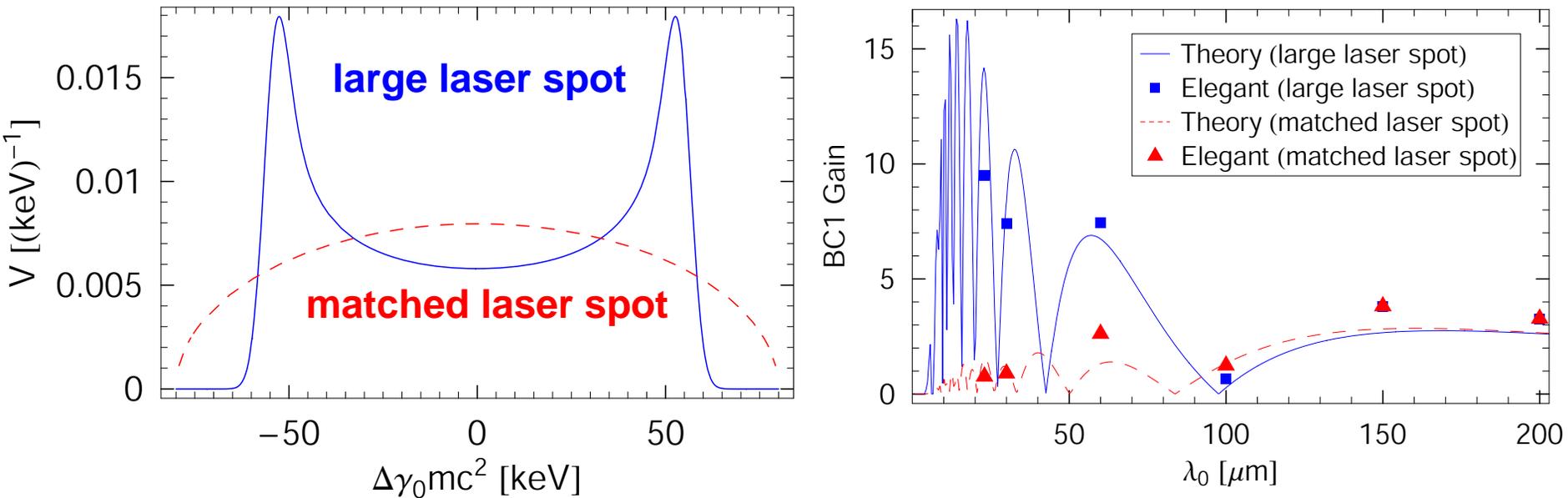


Non-uniform heating

more uniform heating

# Gain suppression depends on laser spot size

- Large laser spot generates “double-horn” energy distribution, ineffective at suppressing short wavelength microbunching
- Laser spot matched to e-beam size creates better heating



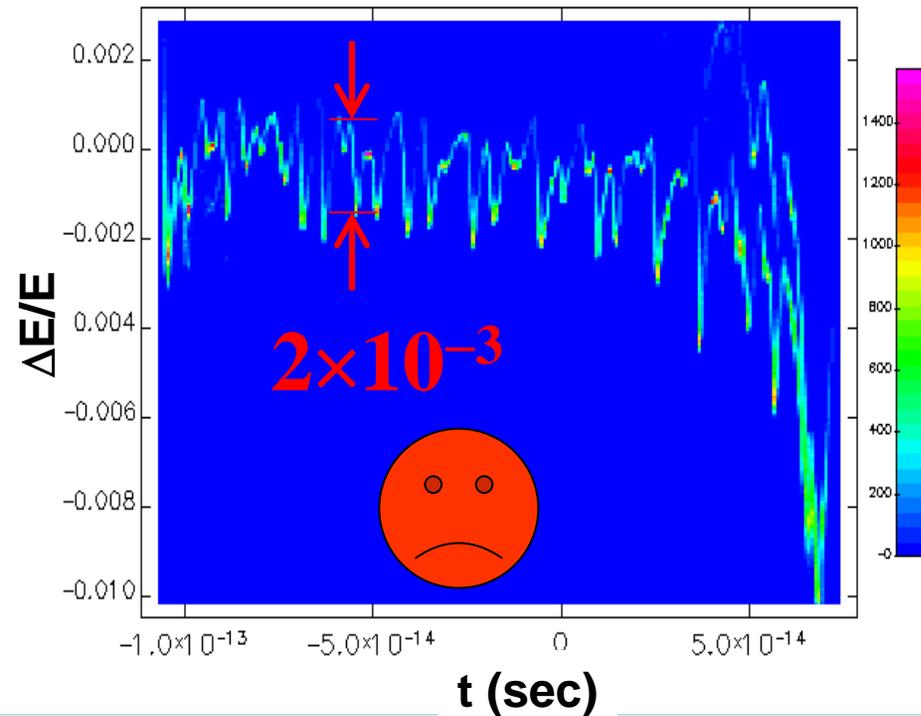
$$\frac{G_L}{G_0} = J_0(k_f R_{56} \delta_L) \sim (k_f R_{56} \delta_L)^{-1/2} \quad \text{when } \sigma_r \gg \sigma_x$$

$$\frac{G_L}{G_0} = 2 \frac{J_1(k_f R_{56} \delta_L)}{k_f R_{56} \delta_L} \sim (k_f R_{56} \delta_L)^{-3/2} \quad \text{when } \sigma_r = \sigma_x$$

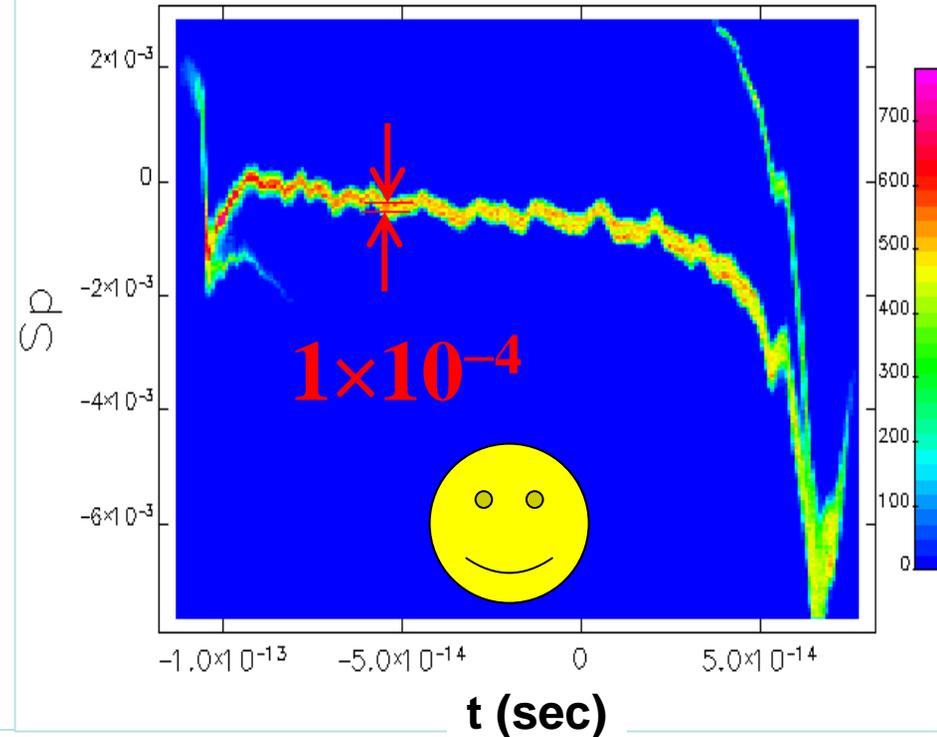
# Start-to-end simulation

- Injector space charge dynamics modeled by ASTRA, Linac by ELEGANT with LSC/CSR/machine impedances

Example: final long. phase space at 14 GeV for initial 8% uv laser intensity modulation at  $\lambda=150 \mu\text{m}$



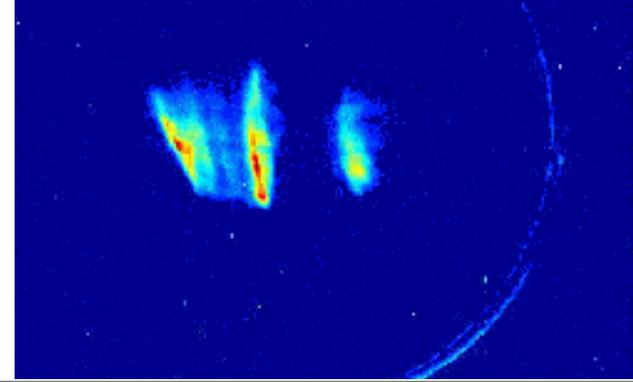
No Laser-Heater



Matched Laser-Heater

# SDL zero-phasing experiment

(Graves et al. PAC01)



RF zero-phase  
time profile

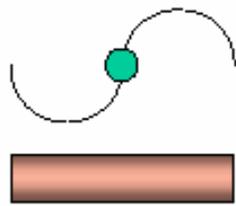
L4 phase =  $-90^\circ$ ,  
amplitude varies  
(adds known  
chirp)

L3 phase =  $+90^\circ$ ,  
amplitude varies  
(removes chirp  
from L2)

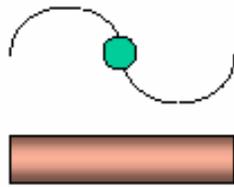
L2 phase varies,  
amplitude  
constant

L1 phase =  $0^\circ$ ,  
amplitude  
constant

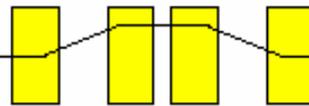
65 MeV  
Energy  
spectrometer



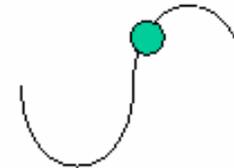
L4



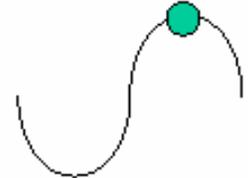
L3



Chicane varies from  
 $0 \text{ cm} < R56 < 10.5 \text{ cm}$

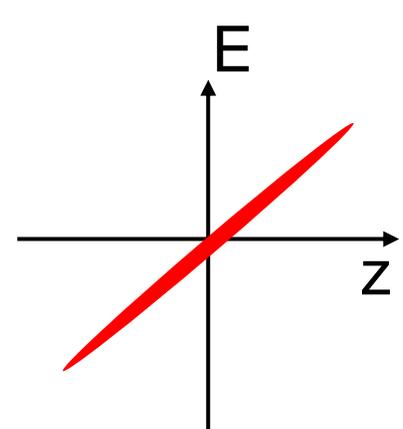
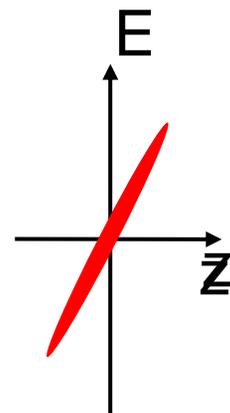
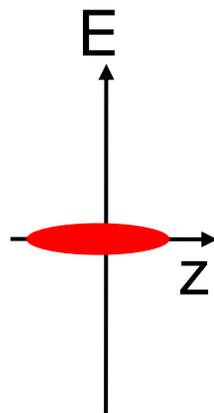
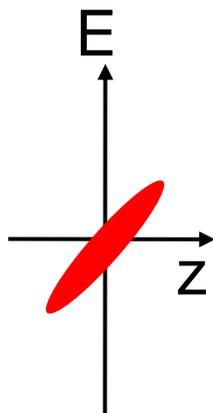
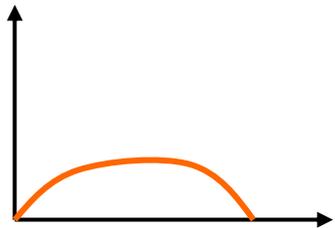


L2



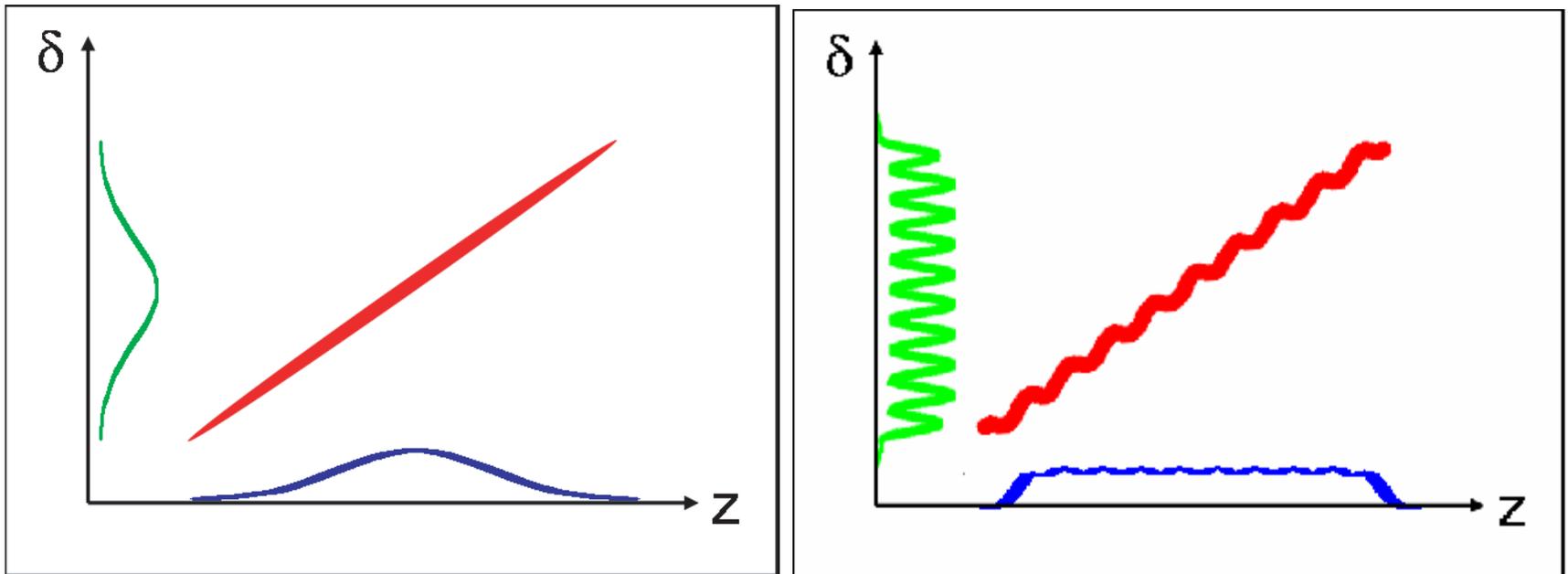
L1

X (E) profile



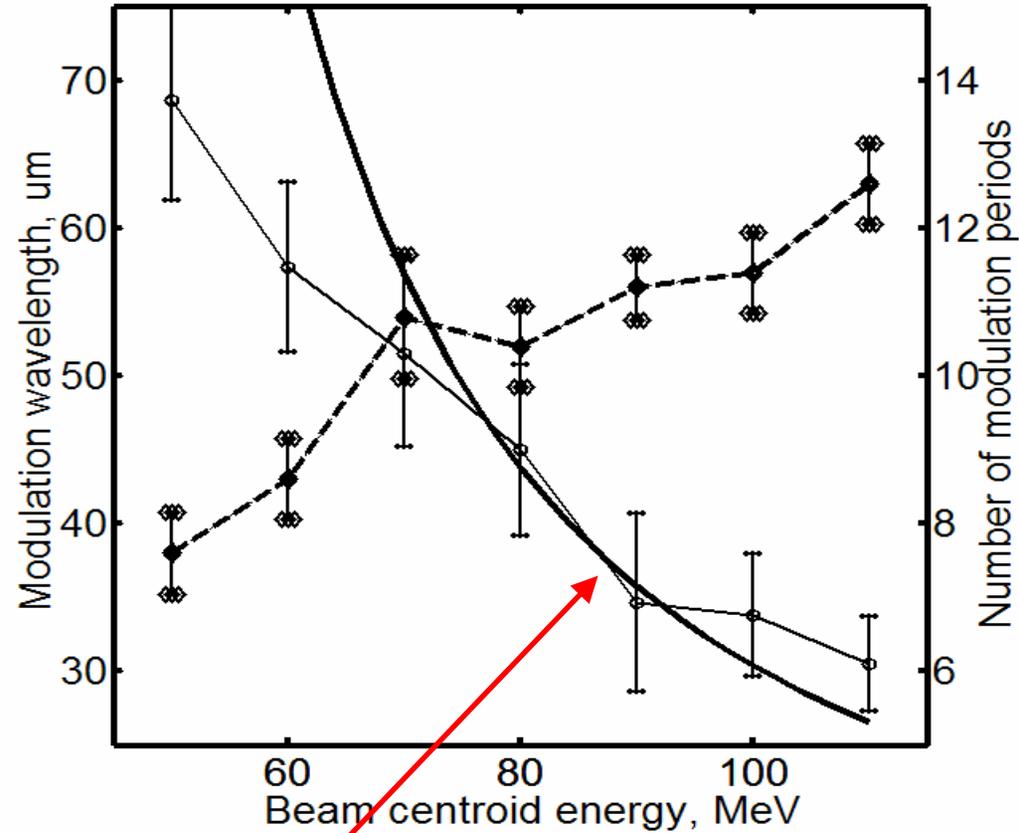
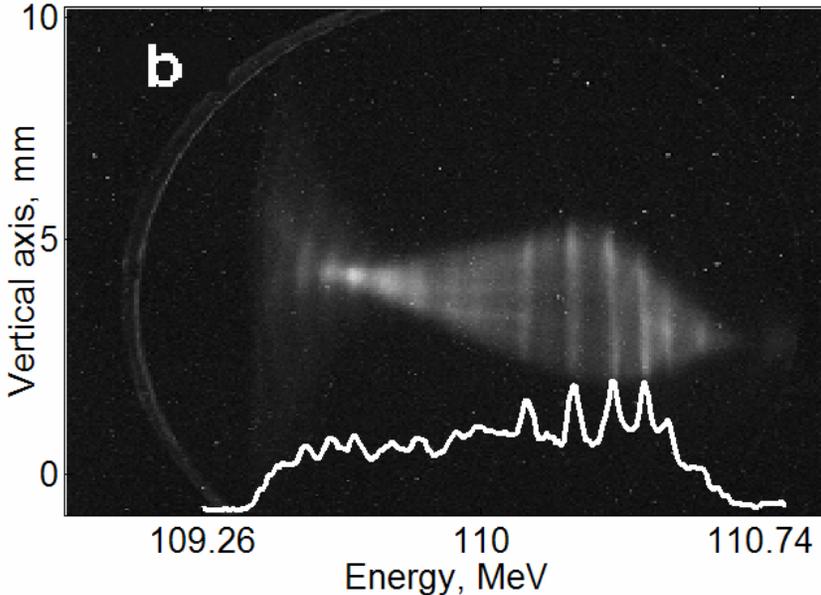
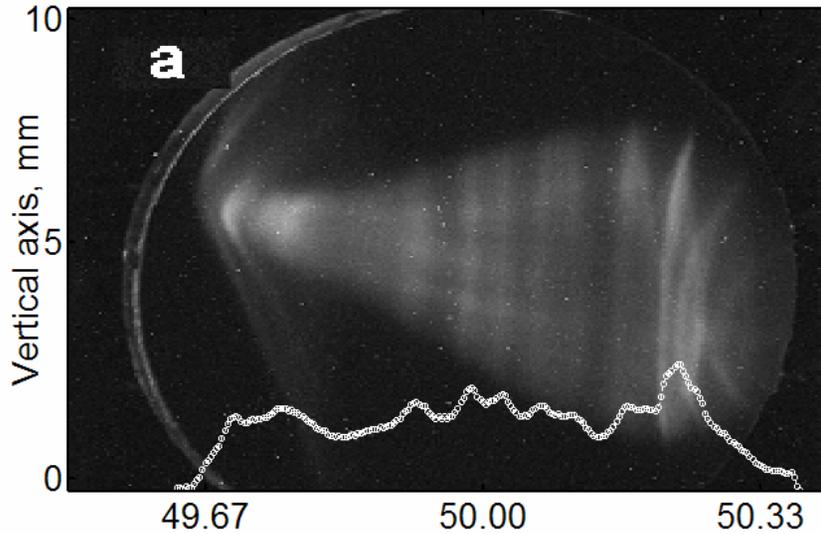
# Zero phasing sensitive to energy modulation

- rf zero phasing energy spectrum is very sensitive to beam energy modulation



- Small energy modulation gets projected to large horizontal density modulation (enhanced by  $\lambda_{rf}/\lambda_m \sim 1000$ )
- Measurement can be used to reveal energy modulations

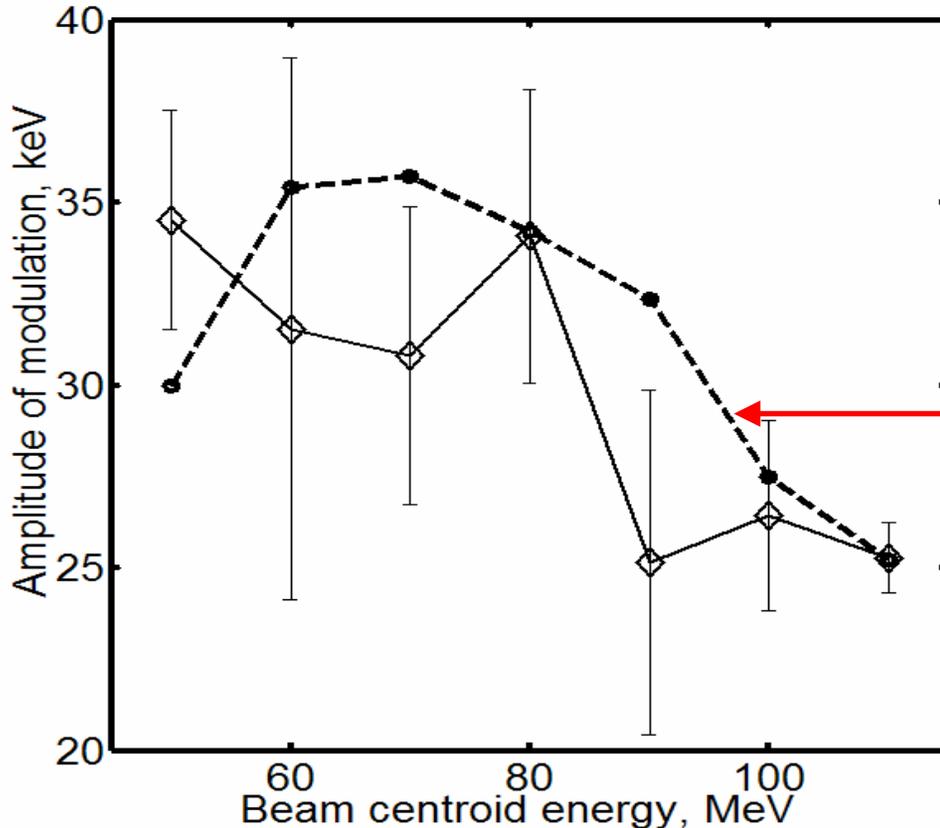
# Modulation wavelength



Wavelengths correspond to calculated maximum energy modulation due to space charge dynamics

# Energy modulation amplitude

- Zero-phasing modulation can be used to extract energy modulation amplitude
  - ➔ (25 – 35 keV at 200 A or  $2 \times 10^{-4}$  at 177 MeV)



Simulated energy modulation assuming 4% initial density modulation after chicane, which is comparable to drive laser modulation amplitude

- Such energy modulations can be converted to large density modulations if a downstream bunch compressor is used, and may hurt a short-wavelength FEL

# Summary

- Microbunching instability driven by LSC, CSR and other machine impedances is a serious concern for short-wavelength FELs
- Strong LSC-induced energy modulation (and maybe density modulation) is characterized in DUV-FEL
- Beams from PC RF gun are too “cold” in energy spread, “heating” within FEL tolerance ( $\sim 10X$ ) to control the instability
- A laser heater with a laser spot matched to the transverse e-beam size is most effective in suppressing microbunching and is designed for LCLS
- It also gives flexible and desirable control of slice energy spread to manipulate FEL signal

**Thanks for your attention!**

**Thank Lia and Alex for  
the invitation!**